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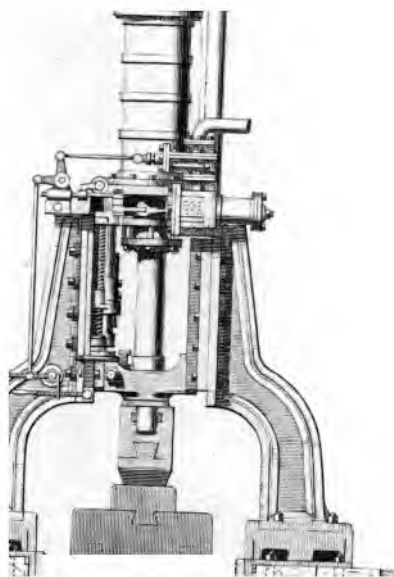












THE
OPERATIVE MECHANIC'S
WORKSHOP COMPANION,

AND

THE SCIENTIFIC GENTLEMAN'S

Practical Assistant;

COMPRISING

A GREAT VARIETY OF THE MOST USEFUL RULES IN
MECHANICAL SCIENCE,

WITH

NUMEROUS TABLES OF PRACTICAL DATA AND CALCULATED RESULTS
FOR FACILITATING MECHANICAL AND COMMERCIAL TRANSACTIONS.

By WILLIAM TEMPLETON.

EIGHTH EDITION, REVISED AND ENLARGED,

WITH THE ADDITION OF

MECHANICAL TABLES FOR THE USE OF OPERATIVE SMITHS,
MILLWRIGHTS, ENGINEERS, ETC.

TO WHICH ALSO HAVE BEEN NOW ADDED

SEVERAL USEFUL AND PRACTICAL RULES IN

HYDRAULICS AND HYDRODYNAMICS,

A VARIETY OF EXPERIMENTAL RESULTS,

AND

AN EXTENSIVE TABLE OF POWERS AND ROOTS.

LONDON:

LOCKWOOD & CO., 7, STATIONERS' HALL COURT.

1864.

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HARRILD, PRINTER, LONDON.



TO THE PUBLIC.

THE subjects of the following pages are chiefly compiled at the instigation of pressing solicitations by numerous individuals, no few of whom complain of the want of a convenient Text Book of Reference in which Mechanical and Commercial demands are judiciously combined. Others, with apparently equal reasons, for the sake of instruction, complain of the want of a compendium in which tuition and practical reference are discriminately arranged; and generally, that for purposes of Estimation, no properly portable work is yet in existence; hence it is with a wish to diminish those wants in some degree that the present attempt has been made to supply the necessary information.

In regard to the selection, great care has been taken that the subjects be not only intimately interwoven, but also of such a nature as business transactions call most frequently into requisition.

The elementary or educational portion will be found exceedingly plain and simple, though compendious. The practical rules, too, are much abbreviated by the application of decimal approximates, by which results are obtained sufficiently

engravings are interspersed, which
value in regard to practical utility;
aims to add the hope, that the Opera
Science, and the intelligent Public,
appreciation to the work, in proportio

W.

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f Operative Smiths, Millwrights,
and the present, which has under
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quares and Cubes, with the correspoi
nd also by additional information
ous kind, on matters of philosop
cal utility.

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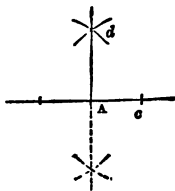
THE WORKSHOP COMPANION.

PRACTICAL GEOMETRY.

GEOMETRY is the science which investigates and demonstrates the properties of lines, surfaces, and solids: hence, **PRACTICAL GEOMETRY** is the method of applying the rules of the science to practical purposes.

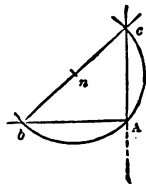
1. *From any given point, in a straight line, to erect a perpendicular; or, to make a line at right angles with a given line.*

On each side of the point A from which the line is to be drawn, take equal distances, as $A b$, $A c$; and from b and c as centres, with any distance greater than $b A$, or $c A$, describe arcs cutting each other at d ; join $A d$, which will be the perpendicular, and it will bisect $b c$.

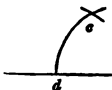


2. *When a perpendicular is to be drawn at or near the end of a given line.*

Take any point n above $A b$, and with centre n and distance $n A$, describe a circle, cutting the given line at b ; through b and the centre n , draw the diameter $b n c$, and join $c A$, which will be the perpendicular required.



From c , cut the arc in c ,
 From c , cut the arc in b ;
 From c and b as centres,
 the same or any other radius,
 describe arcs cutting each other
 then will the line $A b$ be
 perpendicular required.



—When the three sides of a triangle are in
 of 3, 4, and 5 equal parts respectively, two of the
 right angle; and observe that in each of the tri-
 angles, the perpendiculars may be continued be-
 yond, if necessarily required.

To bisect any given angle.

From the point A as a centre, with
 a radius less than the extent of the
 angle, describe an arc, as $c d$; and
 from c and d as centres, describe arcs
 cutting each other at b ; then will
 the line $A b$ bisect the angle as re-

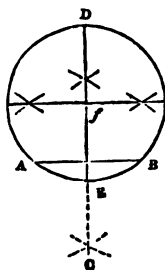


*find the centre of a circle that shall con-
 tain points, not in a direct line.*

intersection of the lines at o is the centre of the circle passing through r , b , t .

6. *To find the centre of a given circle.*

Bisect any chord in the circle, as AB , by a perpendicular CD ; bisect also the diameter ED in f , and the intersection of the lines at f is the centre of the circle required.



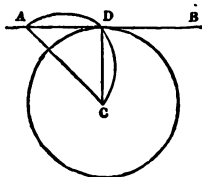
7. *To find the length of any given arc of a circle.*

With the radius AC , equal to $\frac{1}{4}$ th the length of the chord of the arc AB , and from A as a centre, cut the arc in c ; also from B as a centre, with equal radius, cut the chord in b ; draw the line cb , and twice the length of the line is the length of the arc nearly.



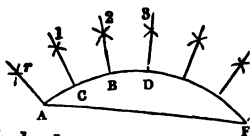
8. *Through any given point, to draw a tangent to a circle.*

Let the given point be at A : draw the line AC , on which describe the semicircle ADC ; join AD , which, produced if necessary, is the tangent required.



9. *To draw from, or to the circumference of a circle*

the desired number of equal parts
 with any radius
 the distance
 divisions, de-
 s cutting each
 A 1, B 1; C 2,
 draw the lines
 D 3, &c., which lead to the centre as



the end lines, as $A r$, $F r$.
 radius c 2, describe the arc r , and with t
 from A or F as centres, cut the form
 r , and the lines $A r$, $F r$, will tend to the
 quired.

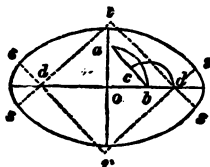
given straight line, to describe an arc c ,
 altitude being given.

the given straight line, $B b$ the given
 $D B$, $B E$, and of any suitable materia



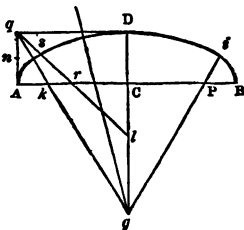
11. *To describe an ellipse, having the two diameters given.*

On the intersection of the two diameters as a centre, with a radius equal to the difference of the semi-diameters, describe the arc $a b$, and from b as a centre, with half the chord $b c a$, describe the arc $c d$; from o , as a centre, with the distance $o d$, cut the diameters in d, r, d, t ; draw the lines $r s, r s, t s, t s$, then from r and t describe the arcs $s s, s s$; also from d and d describe the smaller arcs $s s, s s$, which will complete the ellipse as required.



12. *To describe an elliptic arch, the width and rise of span being given.*

Bisect with a line at right angles the chord or span $A B$, erect the perpendicular $A q$, and draw the line $q D$ equal and parallel to $A C$; bisect $A C$ and $A q$ in r and n , and draw the line $q r l$; and though not in the cut, draw also the line $n s D$; bisect $s D$ with a line at right angles, and meeting the line $C D$ produced in g ; draw the line $g q$, make $C P$ equal to $C k$, and draw the line $g P i$; then from g as a centre, with the radius $g D$, describe the arc $s D i$, and from k and P as centres, with the radius $A k$, describe the arcs $A s$ and $B i$, which completes the arch as required. Or,



13. Bisect the chord $A B$, and fix at right angles any straight guide, as $b c$; prepare of any suitable

of the arch,
 and at the ex-
 tracer f ; move
 keeping its end
 and the fixed pin to the chord, and
 describe one-half the arch required.
 describe a parabola, the dimensions be
 equal the length, and $c d$ the breadth

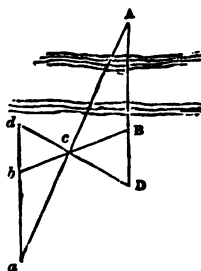


parabola: divide $c A$, $c B$ into an-
 equal parts, also divide the perpendicular
 into the same number of equal parts;
 and d draw lines meeting each division
 $c B$, and a curve line drawn through
 ion will form the parabola required.
 in by measurement the length of any d :
 the intercent d

convenient radius, describe the arc $c c$, make the arc twice the radius in length, through which draw the line $d c e$, and on e describe another arc equal in length to once that radius, as $f f$; draw the line $e f r$ equal to $e f d$; on r describe the arc $j j$, in length twice the radius; continue the line through r, j , which will be a right line, and $d e$ or $e r$, will equal the distance between d, r , by which the distance between A and B is obtained as required.

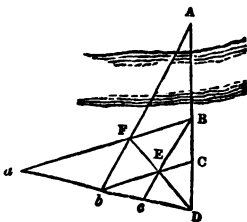
16. *To ascertain the distance geometrically, of any inaccessible object on an equal plane.*

Let it be required to find the distance between A and B , A being inaccessible: produce the line in the direction of $A B$ to any point, as D ; draw the line $D d$ at any angle to the line $A B$; bisect the line $D d$ in c , through which draw the line $B b$, making $c b$ equal to $B c$; join $A c$, and draw $d b a$ meeting $A c$, produced in a . Then $b a$, equal to $A B$, is the distance required.

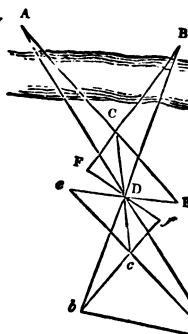


17. *Or otherwise,*

Produce $A B$ to any point D , and bisect $B D$ in C ; through D draw $D a$, making any angle with $D A$, and take $D c, D b$, equal to $D C$ and $D B$ respectively; join $B c, c b$, and $A b$. Through E , the intersection of $B c, c b$, draw $D E F$ meeting $A b$ in



... inaccessible. ... between two
 from any point c draw
 line $c c$, and bisect it
 take any point E in
 prolongation of $A c$,
 draw the line $E e$,
 make $D e$ equal to $D E$;
 in manner take any
 point in the prolongation
 and make $D f$ equal
 to $D e$. Produce $A D$ and
 they meet in a , and
 and $f c$ till they
 meet in b ; then $a b$ is
 the distance between the object.



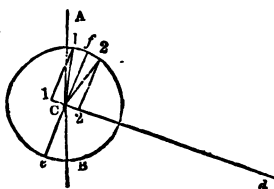
round piece of timber being given, out
 a beam of strongest section.

into three equal parts any
 the circle, as $A d$, $d e$, $e c$;
 e , erect a perpendicular



of eccentric rod and travel of the valve being given.

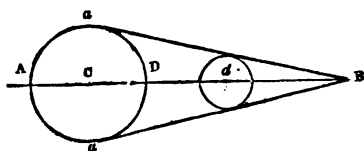
Draw the right line $A B$, as the situation of the crank at commencement of the stroke; draw also the line $C D$, at the proper given angle of eccentric rod with the crank; then from C as centre, describe a circle



equal to the travel of the valve; draw the line ef at right angles to the line $C D$; draw also the lines $1 1$, and $2 2$, parallel to the line ef ; and at a distance from ef on each side, equal to the lap and lead of the valve, draw the angular lines $c 1$, $c 2$, which are the angles of eccentric with the crank, for forward or backward motion, as may be required.

21. *The throw of an eccentric, and the travel of the valve in a steam engine, also the length of one lever for communicating motion to the valve, being given, to determine the proper length for the other.*

On any right line, as $A B$, describe a circle $A D$, equal to the throw of eccentric and travel of valve; then from

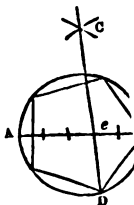


C as a centre, with a radius equal to the length of lever given, cut the line $A B$, as at d , on which describe a circle, equal to the throw of eccentric or travel of valve, as may be required; draw the tangents $B a$, $B a$, cutting each other in the line $A B$, and $d B$ is the length of the lever as required.

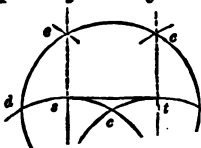
area of a valve is equal to the sum of the areas of the two steam openings, and the excess of length more than just sufficient to pass.



Inscribe any regular polygon in a given circle, and draw a diameter, as A B, into equal parts as the polygon is to have sides; from A and B, with a radius equal to the radius of the circle, describe arcs cutting the diameter in C; draw the line C D to the second point of intersection of the arcs, and the line C D is the side of the polygon required.



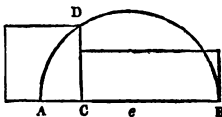
Construct a square upon a given right line, and B as centres, with radius A B, describe arcs A C and A D, and from B, B C D, and from A, A E F, and from the intersection of the arcs, describe a portion of a circle from b, d, cut the



and describe the semicircle $e n c$; erect the perpendicular $A s$, or side of the square, then $A s t x$ is the square of equal area as required.

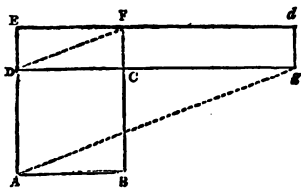
25. *To form a square equal in area to a given rectangle.*

Let the line $A B$ equal the length and breadth of the given rectangle: bisect the line in e , and describe the semicircle $A D B$; then from A with the breadth, or from B with the length of the rectangle, cut the line $A B$ at C , and erect the perpendicular $C D$, meeting the curve at D , and $C D$ is equal to a side of the square required.



26. *To find the length for a rectangle whose area shall be equal to that of a given square, the breadth of the rectangle being also given.*

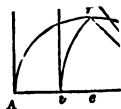
Let $A B C D$ be the given square, and $D E$ the given breadth of rectangle. Through E draw $E F$ parallel to $A B$ or $D C$; produce $B C$ to F , and join $D F$. Through A draw $A g$ parallel to $D F$, cutting $D C$ produced in g , through which draw $g d$ parallel to $D E$, meeting $E F$ produced in d . $E D g d$ is the rectangle required.



27. *To bisect any given triangle.*

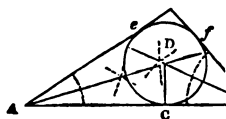
Suppose $A B C$ the given triangle: bisect one of

to $A C$, which will bisect angle as required.



To describe a circle of greatest diameter

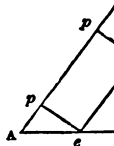
in a triangle. Bisect the angles A and C , draw the intersecting lines $A D$, $C D$, cutting each other in D ; then



with D as centre, with distance $D C$, which is drawn perpendicular to AC , describe the circle, $c e f$, as required.

To form a rectangle of greatest area in a given triangle.

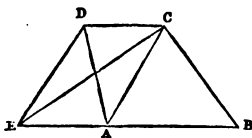
Let $A B C$ be the given triangle: bisect any two of its sides, as $A B$ in e and $A C$ in d ; draw the line $e d$; draw right angles with the line $e d$, as lines $e p$, $d p$, and $e p p d$ rectangle required.



To make a rectangle equal to a given triangle.

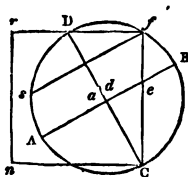
31. To make a triangle equal to a given quadrilateral, as $A B C D$.

Prolong the line $B A$, and draw the line $A C$; draw also the line $D E$ parallel to $A C$, and cutting the line $B A$ in E ; then draw the line $E C$, and $E B$ is the triangle required.



32. To form a square nearly equal in area to a given circle.

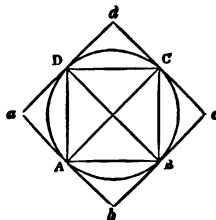
Let $A C B D$ be the given circle: draw the diameters $A B$ and $C D$ at right angles to each other, bisect the radius $d B$ in e , and draw the line $c e f$; draw also at right angles the lines $c n$ and $f r$, making each equal to $c f$; join $n r$, and $n c f r$ is the square as required.



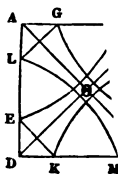
Note.—The line $s f$ is equal to one-fourth the circumference of the circle nearly.

33. To inscribe or describe a square within or without a given circle: also to form an octagon from a given square.

1. Let $A B C D$ be the given circle: draw the diameters $A C$, $B D$, at right angles to each other, and join $A B$, $B C$, $C D$, $D A$, which will complete the inscribed square: through the extremities of the same diameters draw $a b$, $c d$, parallel



Let $A B C D$ be the given square. Draw diagonal lines $A C$ and $B D$ intersecting in O ; then with a compass, taking $A O$, or half the diagonal, and with A as a centre, describe the arc $E F$, cutting the sides of the square in E and F ; from B as a centre, describe the arc $G H$, and in the same manner from C and D describe the arcs $I K$ and $L M$, and draw the lines $L G$, $F I$, $H M$, and $K E$, which, together with $G F$, $I H$, $M K$, and $E L$, form the octagon.

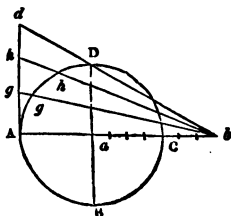


Problem 12. To form a square equal to two given squares.
Problem 13. To form a square equal to two given circles.

Let $A B$ and $C D$ be the sides of the two given squares, or diameters of the two given circles: make the angle $A C D$ at C , and draw the line $C E$, which is the side of a square equal to both the squares.

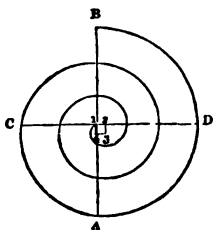


ference of which is required : draw at right angles the diameters $A C$, $B D$, divide the radius $a c$ into four equal parts, and make $c b$ equal to three of them ; draw the tangent $A d$ parallel to $B D$, draw the line $b D d$, then will $A d$ be nearly a fourth of the whole circumference ; and if lines be drawn from b , through points in the circumference, meeting the line $A d$, as $g g$, $h h$, &c., the corresponding parts will be equal to each other nearly.

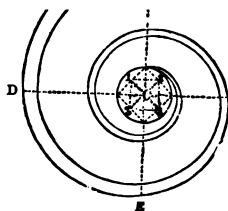


36. *To draw a spiral with spaces of uniform distance.*

Bisect the height of the spiral, as $A B$, and divide either half into the number of spaces or revolutions required ; then again subdivide any one space into four equal parts, one of which add to half the height of the spiral, and through the termination draw $C D$ at right angles to $A B$, thus forming the centre of the spiral, around which and equal to one of the subdivisions form a square, its sides being parallel with the lines $A B$ and $C D$, the angles of which are the centres from whence to describe the various curves ; as from 1, with the distance 1 B , describe the curve $B D$; from 2, with the distance 2 D , describe $D A$; from 3, with the distance 3 A , describe $A C$, &c., &c., and from the same centres the spiral may be continued to any extent required.



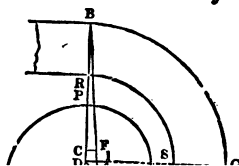
from a square in
 the diagonals of
 respond with or
 meters A D, E B;
 square with lines
 each other in the
 and parallel with
 of the square; di-



into six equal parts, which are the centre
 of the volute is to be described: thus, from
 the distance 1 B, describe the curve B I
 with 2 D, describe D E; from 3, with 3 I
 A, &c., approaching the centre by degrees
 the volute is completed as required.

draw a scroll for the termination of
&c.

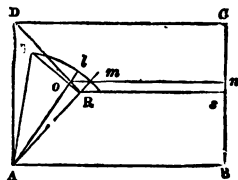
equal the given
 draw A E perpen-
 dicular to B, which divide
 into equal parts, and
 bisect one of them;
 bisect A B in C



$D O K, I O L$, perpendicular to $D O K$; draw $I K$ parallel to $B A$, $K L$ parallel to $I D$, &c., meeting the diagonals; from D as a centre, with the distance $D B$, describe the arc $B G$; from I as a centre, with the distance $I G$, describe $G E$; from K , with the distance $K E$, describe $K H$, &c., proceeding in the same manner until the outside of the scroll is completed; make $B R$ equal to the breadth of the rail; then from D , with the distance $D R$, describe the arc $R S$; from I , and distance $I S$, describe $S T$; and from T , with $K T$, describe $T U$, which completes the scroll as required.

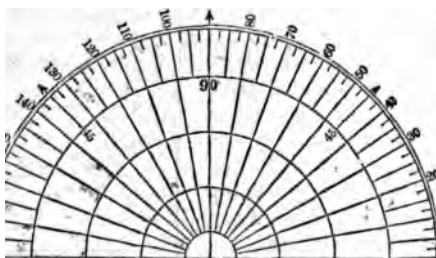
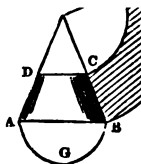
39. *To find the various angles and proper dimensions of materials whereby to construct any figure whose form is the frustum of a proper or inverted pyramid, as hipped roofs, mill hoppers, &c., &c.*

Let $A B C D$ be the given dimensions of plan for a roof, the height $R T$ also being given; draw the diagonal $A R$, meeting the top or ridge $R s$ on plan; from R , at right angles with $A R$ and equal to the required



height, draw the line $R T$, then $T A$, equals the length of the struts or corners of the roof; from A , with the distance $A T$, describe an arc $T l$, continue the diagonal $A R$ until it cuts the arc $T l$, through which, and parallel with the ridge $R s$, draw the line $m n$, which determines the required breadth for each side of the roof: from A , meeting the line $m n$, draw the line $A o$, or proper angle for the end of each board by which the roof might require to be covered; and the angle at T is what the boards require to be made in the direction of their thickness, when the corners or angles require to be mitred.

rom **E** as centre, with the
E C, describe the arc **C H**;
 om **E**, with the radius **E B**,
 e the arc **B I**; make **B I**
 in length to twice **A G B**,
 he line **E I**, and **B C I H** is
 m of plate as required.



Sector from which angles may be obtained.

GEOMETRY APPLIED TO MECHANICS.

To delineate a vee-threaded screw, the

Fig. 1.

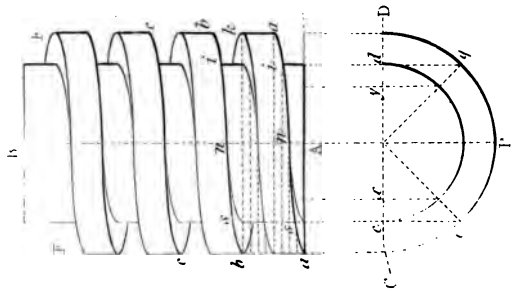


Fig. 3.

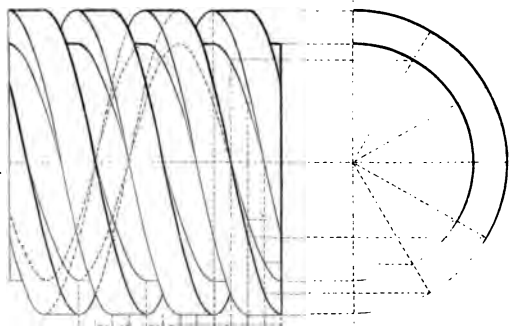
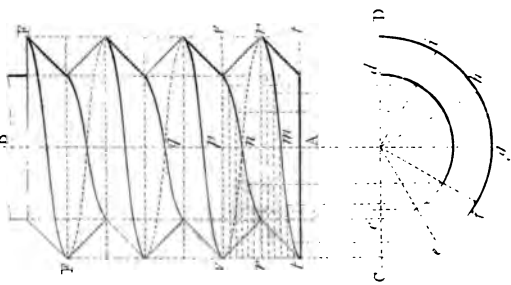


Fig. 1.



London, University of London, University of London

into any number of equal parts, as *c, e, f, g, h, i, d*, from which draw lines parallel to the line *A B*; divide the lines *C F, D F*, into equal divisions of half the required pitch or consecutive threads, as *t, r, v, &c.*; draw the lines *t t, r r, v v, &c.*, parallel with the diameter *C D*, and subdivide any two connected divisions into the same number of equal parts contained in both semicircles, from which draw lines meeting the vertical lines; then by hand, or otherwise, and through the intersections, draw the waved lines, *m, n, p, q, &c.*, and a thread of the screw is delineated as required.

Note.—The same process might be continued throughout the whole length of the screw, but it is much more convenient, when the proper curves are obtained, to form a suitable ruler: lay it in its proper situation upon each division, and draw the lines as required.

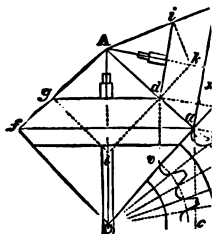
42. *To delineate a square-threaded screw, the pitch and diameter of screw being given.* (See Plate A, fig. 2.)

On the line *A B* representing the centre of the screw, describe the semicircles *C D, c d*, equal to the diameters at the tops and bottoms of the threads; divide each semi-circumference into four equal parts, draw lines from each and parallel to the line *A B*; draw also the lines *C F, D F*, which divide into the proper required pitch, as *a a, b b, c c, &c.*; divide any two connected pitches or divisions, as *a, b*, into four equal parts, from which draw lines parallel to the diameter *C D*, meeting the vertical lines *o, p, q*, and forming intersections through which the waved lines *s, n, i, s, n, i*, or tops of the threads, must be traced by hand or otherwise; draw also the lines *x, y*, forming intersections through which to trace the curve surface exhibited between and caused by the angular return

that of fig. 2, but intended, by displacing the cylinder, to delineate a continuous vein of its proper form around the whole circumference, being deemed by the preceding figure sufficiently described, further elucidation considered unnecessary.

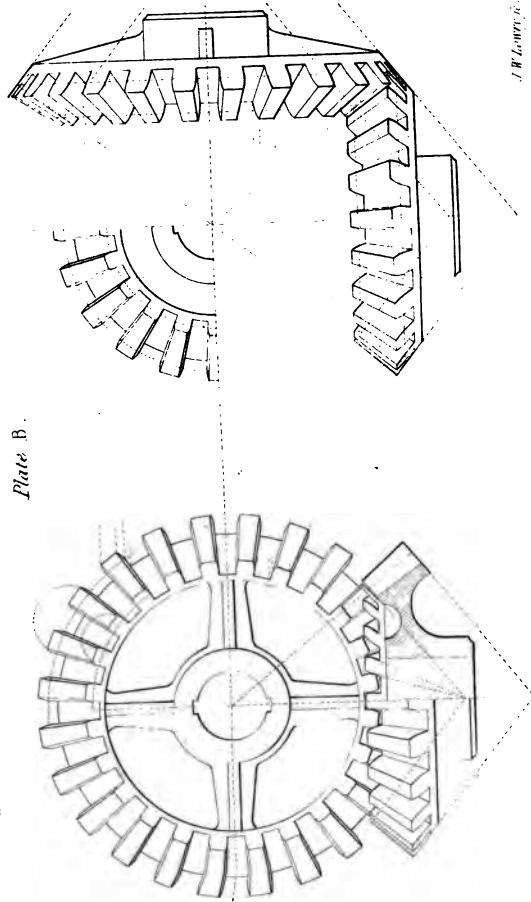
43. *To determine the proper forms for wheel wheels, the required angle of the shaft centers of the wheels being given.*

Draw at the given angles lines representing shafts on which the wheels are to be fixed; make the lines AB and AC parallel with each other at a distance from each other equal to the radius of each respective wheel at the greatest diameter; draw the line AD through the intersection of the shafts at d ; then draw the line AE at right angles to AD .



ILLUSTRATIONS TO THE DRAWING OF LEVEL WHEELS.

Plate B.



J. W. L. 1877, N. 1.

U. S. PATENT OFFICE, WASHINGTON, D. C.

the radius $B a$, $C a$, describe portions of circles, as $a G$, $a H$, on which describe the greatest dimensions of, and proper form of the teeth; then from d , and parallel with $A B$, $A C$, draw the lines $a v$, $a x$, cutting the line $c b$ in v and x ; from B and C , with the distances $c v$, $B x$, describe the portions of circles, which determines the dimensions of the teeth on the interior pitch circle, and completes the proper forms of the wheels as required.

Proportions for the construction of toothed wheels.

- Length of the teeth $= \frac{1}{4}$ of the pitch.
 Thickness „ $= \frac{1}{8}$ do.
 Breadth on face $= 2\frac{1}{2}$ times the pitch.
 Edge of the rim
 Projecting rib inside do. } each $\frac{1}{4}$ of the pitch.
 Thickness of flat arms
 Breadth of arms at rim $= 2$ teeth and $\frac{1}{4}$ the pitch,
 increasing in breadth towards the centre of the wheel,
 in the proportion of $\frac{1}{2}$ an inch for every foot in length.
 Thickness of the ribs or feathers on the arms $= \frac{1}{4}$
 of the pitch.
 Thickness of metal around the eye, or centre, $= \frac{1}{8}$
 of the pitch.

Wheels and other circular bodies are very conveniently transferred from plan to that of a projected perspective by means of a peculiar appropriation of straight lines, commonly called orthographic projection, the principle of which will be readily understood by reference to the diagrams and illustrations given for the purpose in Plate C.

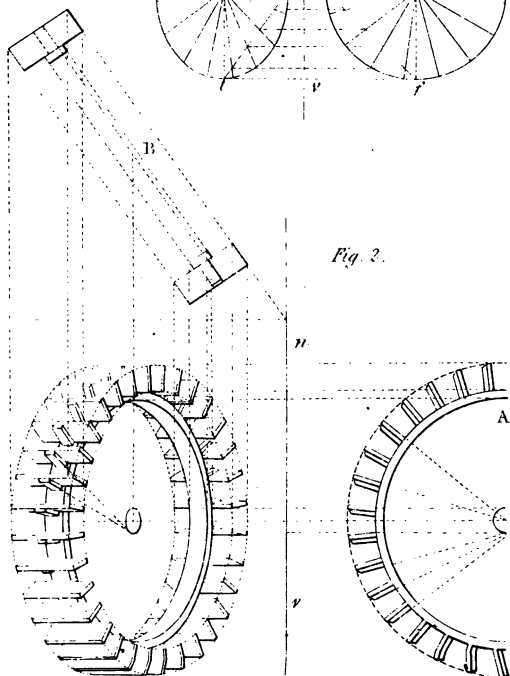
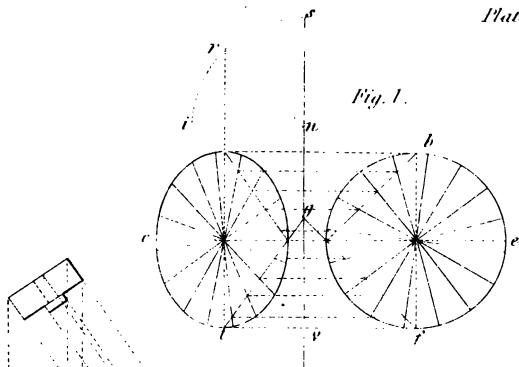
Fig. 1 is a circle divided into equal parts, and its form in projection is required, vn being supposed the line of intersection: parallel with the diameter of the

... which determines the breadth of the projected form of the circle, and which is as described (page 5, fig. 12): hence the lines being so distinctly described, by the construction of the diagrams, further explanation is unnecessary.

Fig. 2 is a projected representation of an untruncated wheel, of which A is the plan, v n the section, and B the diameter and breadth, perpendicular angle or inclination, as determined by the principles of the diagrams: the breadth of the wheel is found and formed as there described, and the illustration, or fig. 2, whereby to obtain the proper angles for projection, render sufficient the proper mode by which the representation is made.

ORTHOGRAPHIC PROTECTION.

Plate V.



London: Lockwood & Co Stationers Hall Court.

J. W. Lawrence, Jr.

DECIMAL ARITHMETIC.

DECIMAL ARITHMETIC is the most simple and explicit mode of performing practical calculations; on account of its doing away with the necessity of fractional parts in the fractional form, thereby reducing long and tedious operations to a few figures, arranged and worked in all respects according to the usual rules of common arithmetic.

Decimals simply signify tenths: thus, the decimal of a foot is the tenth part of a foot, the decimal of that tenth is the hundredth of a foot, the decimal of that hundredth is the thousandth of a foot, and so might the divisions be carried on and lessened to infinity; but in practice it is seldom necessary to take into account any degree of less measure than a one-hundredth part of the integer or whole number. And, as the entire system consists in supposing the whole number divided into tenths, hundredths, thousandths, &c., no peculiarity of notation is required, otherwise than placing a mark or dot, to distinguish between the whole and any part of the whole: thus 34·25 gallons signify 34 gallons 2 tenths and 5 hundredths of a gallon; 11·04 yards signify 11 yards and 4 hundredths of a yard; 16·008 shillings signify 16 shillings and 8 thousandth parts of a shilling: from which it must appear plain, that ciphers on the right hand of decimals are of no value whatever; but placed on the left hand, they diminish the decimal value in a ten-fold proportion,—for ·6 signifies 6 tenths; ·06 signifies 6 hundredths; and ·006 signifies 6 thousandths, of the integer or whole number.

REDUCTION.

Reduction means the construing or changing of

valent value.

Rule 2. Multiply the decimal by successive numbers, such as to cause the decimals in the product to be all 0. The integer prefixed to the decimal be the numerator, and the product of the decimal be the denominator of the equal fraction. For the figures of the decimal write 1, followed by as many 0's.

1. Required the decimal equivalent of equal value, to $\frac{2}{12}$ of a foot.

$$\frac{2 \cdot 00}{12} = \cdot 25, \text{ the decimal required.}$$

2. Reduce the fraction $\frac{1}{8}$ of an inch to its decimal equivalent.

$$\frac{1 \cdot 000}{8} = \cdot 125, \text{ the decimal required.}$$

3. What is the decimal equivalent to $\frac{7}{8}$?

$$\frac{7 \cdot 000}{8} = \cdot 875, \text{ the decimal equivalent.}$$

Ex. 5. What is the value of $\cdot 625$ of a cwt.?

$$\begin{array}{r}
 \cdot 625 \\
 \text{Multiply by 4 qrs.} \quad 4 \\
 \hline
 2 \cdot 500 \\
 \times 28 \text{ lbs.} \quad 28 \\
 \hline
 14 \cdot 000 = 2 \text{ quarters and 14 lbs., the value} \\
 \hline \hline
 \text{required.}
 \end{array}$$

Ex. 6. Ascertain the value of $\cdot 875$ of an imperial gallon.

$$\begin{array}{r}
 \cdot 875 \\
 \text{Multiply by 4 quarts} \quad 4 \\
 \hline
 3 \cdot 500 \\
 \times 2 \text{ pints} \quad 2 \\
 \hline
 1 \cdot 000 = 3 \text{ quarts and 1 pint, the value} \\
 \hline \hline
 \text{required.}
 \end{array}$$

Ex. 7. What is the value of $\cdot 525$ of a £. sterling?

$$\begin{array}{r}
 \cdot 525 \\
 \text{Multiply by 20 sh.} \quad 20 \\
 \hline
 10 \cdot 500 \\
 \times 12 \text{ pence} \quad 12 \\
 \hline
 6 \cdot 000 = 10 \text{ shillings and 6 pence, the} \\
 \hline \hline
 \text{'value required.}
 \end{array}$$

Independent of the mark or dot which distinguishes between integers and decimals, the fundamental rules, viz., Addition, Subtraction, Multiplication, and Division, are in all respects the same as in Simple Arithmetic; and an example in each, illustrative of placing the separating point, will no doubt render the whole system sufficiently intelligible, even to the dullest capacity.

$$\begin{array}{r}
 16.625 \\
 11.4 \\
 20.7831 \\
 12.125 \\
 8.04 \\
 7.002 \\
 \hline
 \end{array}$$

$$\underline{\underline{75.9751}} = \text{the sum required}$$

Ex. 2. Subtract 119.80764 from

$$\begin{array}{r}
 234.98276 \\
 119.80764 \\
 \hline
 \end{array}$$

$$\underline{\underline{115.17512}} = \text{the remainder}$$

Ex. 3. Multiply 62.10372 by 16

$$\begin{array}{r}
 62.10372 \\
 16.732 \\
 \hline
 12420744 \\
 18631116 \\
 48472604 \\
 37262232
 \end{array}$$

Ex. 4. Divide 39.375 by 9.25.

9.25) 39.375 (4.256 = the quotient required.

$$\begin{array}{r}
 3700 \\
 \underline{2375} \\
 1850 \\
 \underline{5250} \\
 4625 \\
 \underline{6250} \\
 5550 \\
 \underline{700} \\
 \hline
 \hline
 \end{array}$$

Observe that the number of decimals in the divisor and quotient together, must be equal to the number in the dividend.

Note.—The operation might be still continued, so as to reduce the quotient to a degree of greater exactitude, but in practice it is quite unnecessary, being even now reduced to a measure of greater nicety than is commonly required.

Definitions of Arithmetical signs employed in the following calculations, which ought to be particularly attended to.

= sign of equality, and signifies equal to, as 3 added 4 = 7.

+ " addition " plus or more, as 5 + 3 = 8.

− " subtraction " minus or less, as 8 − 3 = 5.

× " multiplication " multiplied by, as 8 × 3 = 24.

÷ " division " divided by, $24 \div 4 = 6$ or $\frac{24}{4} = 6$.

: :: : proportion " that 2 is to 3 as 4 is to 6, &c.

√ " square root " evolution, or the extr^d. of roots;

$\sqrt[3]{}$ " cube root " thus, $\sqrt{64} = 8$ and $\sqrt[3]{64} = 4$.

4^2 " to be squared " involution, or the raising of powers;

4^3 " to be cubed " thus, $4^2 = 16$, and $4^3 = 64$.

$3 + 5 \times 4 = 32$ { that, 3 plus 5, or 8 multiplied by 4 = 32.

$\sqrt{5^2 - 3^2} = 4$ 5 squared, minus 3 squared, the square root of the remainder = 4.

$\sqrt[3]{\frac{20 \times 12}{30}} = 2$, 20 multiplied by 12, and divided by 30, the cube root of the quotient = 2.

.....	= 1 fu
3 furlongs, 1760 yards, or 5280 feet ...	= 1 m

Measures of surface, or square measur

144 square inches	= 1 sq
9 square feet	= 1 sq
10 $\frac{1}{4}$ square yards ...	= 1 sq
40 square poles	= 1 roc
roods, or 4840 square yards	= 1 acr

Measures of solidity, or cubic measure.

728 cubic inches	= 1 cub
7 cubic feet	= 1 cub

Measures of capacity.

LIQUIDS.

365 cubic inches	= 1 gill.
gills	= 1 pint
pints	= 1 quar
quarts, or 277 $\frac{1}{4}$ cubic inches	= 1 gallo

GRAIN, FRUITS, &c.

allons	= 1 peck
ecks, or 2218·192 cubic inches.....	= 1 bush
ushels	= 1 quar
uarters.....	= 1 load.

Measures of weight.

TROY.

ains	—
------------	---

BRITISH SPECIAL MEASURES.

1. *Lineal measures for land.*

7·92 inches	= 1 link.
100 links, or 22 yards.....	= 1 chain.
80 chains	= 1 mile.
69·121 miles.....	= 1 geog. degree.

2. *Square measures for land.*

62·7264 square inches.....	= 1 square link.
10,000 square links	= 1 square chain.
10 square chains	= 1 acre.

3. *Nautical measures.*

6082·66 feet	= 1 nautical mile.
3 miles	= 1 league.
20 leagues.....	= 1 degree.
360 degrees	= the earth's circumference.

Miscellaneous special measures.

6 lineal feet	= 1 fathom.	
100 square feet	= 1 square of flooring.	
272 sq. feet, at 1½ in. in thickness	= 1 rod of brick-work.	
600 square feet of inch boards...	= 1 load.	
40 cubic feet of round timber	} = 1 ton or load.	
50 cubic feet of hewn timber		
40 cubic feet	= 1 ton of shipping.	
120 deals.....	= 1 hundred.	
120 nails.....	= 1 hundred.	
1200 do.	= 1 thousand.	
500 bricks	= 1 load.	
32 bushels of lime.....	= 1 do.	
36 do. sand	= 1 do.	
19½ cwt.	= 1 fother of lead.	
108 cubic feet.....	= 1 stack of wood.	
42 gallons	= 1 tierce	} old wine measure.
63 do.	= 1 hogshead	
84 do.	= 1 puncheon	
126 do.	= 1 pipe	
252 do.	= 1 tun	} old ale measure.
36 do.	= 1 barrel	
54 do.	= 1 hogshead	
72 do.	= 1 puncheon	
108 do.	= 1 butt	

Square inches	„	•007	= square feet
„ yards	„	•0002067	= acres.
Circular inches	„	•00546	= square feet
Cylindrical inches	„	•0004544	= cubic feet.
„ feet	„	•02909	= cubic yard.
Cubic inches	„	•00058	= cubic feet.
„ feet	„	•03704	= cubic yard.
„ „	„	6•232	= imperial ga
„ inches	„	•003607	= „ „
Cylindrical feet *	„	4•895	= „ „
„ inches	„	•002832	= „ „
Cubic inches	„	•263	= lbs. av. of
„ „	„	•281	= „ wrought
„ „	„	•283	= „ steel.
„ „	„	•3225	= „ copper
„ „	„	•3037	= „ brass.
„ „	„	•26	= „ zinc.
„ „	„	•4103	= „ lead.
„ „	„	•2636	= „ tin.
„ „	„	•4908	= „ mercury
Cylindrical inches	„	•2065	= „ cast ir
„ „	„	•2168	= „ wrought
„ „	„	•2223	= „ steel.
„ „	„	•2533	= „ copper
„ „	„	•2385	= „ brass.
„ „	„	•2042	= „ zinc.
„ „	„	•3223	= „ lead.
„ „	„	•207	= „

IMAL EQUIVALENTS TO FRACTIONAL PARTS OF LINEAL MEASURES.

One inch, the integer or whole number.					
875	$\frac{7}{8} \& \frac{5}{16}$	•625	$\frac{5}{8}$	•28125	$\frac{1}{4} \& \frac{1}{16}$
75	$\frac{3}{4} \& \frac{1}{8}$	•59375	$\frac{1}{4} \& \frac{3}{8}$	•25	$\frac{1}{4}$
625	$\frac{5}{8} \& \frac{1}{16}$	•5625	$\frac{1}{4} \& \frac{1}{8}$	•21875	$\frac{1}{8} \& \frac{3}{16}$
5	$\frac{1}{2}$	•53125	$\frac{1}{4} \& \frac{1}{16}$	•1875	$\frac{1}{8} \& \frac{1}{16}$
375	$\frac{3}{8} \& \frac{3}{16}$	•5	$\frac{1}{2}$	•15625	$\frac{1}{8} \& \frac{1}{16}$
25	$\frac{1}{4} \& \frac{1}{8}$	•46875	$\frac{3}{8} \& \frac{3}{16}$	•125	$\frac{1}{8}$
125	$\frac{1}{4} \& \frac{1}{8}$	•4375	$\frac{3}{8} \& \frac{1}{8}$	•09375	$\frac{3}{16}$
	are equal to	•40625	$\frac{3}{8} \& \frac{1}{16}$	•0625	$\frac{1}{16}$
875	$\frac{5}{8} \& \frac{3}{16}$	•375	$\frac{3}{8}$	•03125	$\frac{1}{16}$
75	$\frac{3}{8} \& \frac{1}{8}$	•34375	$\frac{1}{4} \& \frac{3}{8}$		
625	$\frac{5}{8} \& \frac{1}{16}$	•3125	$\frac{1}{4} \& \frac{1}{8}$		
One foot, or 12 inches, the integer.					
66	11 inches.	•4166	5 in.	•0625	$\frac{1}{4}$ of in.
38	10 "	•3333	4 "	•05208	$\frac{1}{8}$ "
	are equal to	•25	3 "	•04166	$\frac{1}{8}$ "
66	8 "	•1666	2 "	•03125	$\frac{1}{8}$ "
33	7 "	•0833	1 "	•02083	$\frac{1}{8}$ "
	are equal to	•07291	$\frac{1}{4}$ "	•01041	$\frac{1}{8}$ "
One yard, or 36 inches, the integer.					
22	35 inches.	•6389	23 inches.	•3055	11 inches.
44	34 "	•6111	22 "	•2778	10 "
67	33 "	•5833	21 "	•25	9 "
89	32 "	•5556	20 "	•2222	8 "
11	31 "	•5278	19 "	•1944	7 "
33	30 "	•5	18 "	•1667	6 "
56	29 "	•4722	17 "	•1389	5 "
78	28 "	•4444	16 "	•1111	4 "
	are equal to	•4167	15 "	•0833	3 "
22	27 "	•3889	14 "	•0555	2 "
44	26 "	•3611	13 "	•0278	1 "
67	25 "	•3333	12 "		

MENSURATION.

MENSURATION is that branch of which is employed in ascertaining the solidities, and capacities of bodies, capable of being measured.

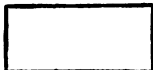
1. MENSURATION OF SURFACES.

To measure or ascertain the quantity of any right-lined figure whose opposite sides are parallel to each other, as a

Square,



Rectangle,



Rhomboid.



Rule.—Multiply the length by the breadth; the product is the area or superficial contents.

Application of the rule to practical purposes.

. The side of a square piece of board is 4 feet.
Another piece is 6 feet long and 3 feet wide.

3. Required the number of square yards in a floor whose length is $13\frac{1}{2}$, and breadth $9\frac{3}{4}$ feet.

$$13.5 \times 9.75 = 131.625 \div 9 = 14.625 \text{ square yards.}$$

Note 1.—The above rule is rendered equally applicable to figures whose sides are not parallel to each other, by taking the mean breadth as that by which the contents are to be estimated.

2. The square root of any given sum equals the side of a square of equal area.

3. Any square whose side is equal to the diagonal of another square, contains double the area of that square.

4. Any sum or area (of which to form a rectangle) divided by the breadth, the quotient equals the length; or divided by the length, the quotient equals the breadth of the rectangle required.

TRIANGLES.

Any two sides of a right-angled triangle being given, to find the third side.

Rule 1.—Add together the squares of the base and perpendicular, and the square root of the sum is the hypotenuse or longest side.

Rule 2.—Add together the hypotenuse and any one side, multiply the sum by their difference, and the square root of the product equals the other side.

Application to practical purposes.

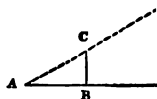
1. Wanting to prop a building with raking shores, the top ends of which to be 25 feet from the ground, and the bottom ends, 16 feet from the base of the building; what must be their length, independent of any extra length allowed below the surface of the ground?

$$25^2 + 16^2 = \sqrt{881} = 29.6816 \text{ feet, or } .6816 \times 12 = 8 \text{ inches; consequently, 29 feet 8 inches nearly.}$$

2. From the top of a wall 18 feet in height, a line was stretched across a canal for the purpose of ascer-

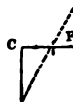
angles similar to each other are proportional; hence their utility in ascertaining heights and distances of inaccessible objects.

Now, suppose the height of an inaccessible object D is required, I find by means of a staff or otherwise, the height of the perpendicular BC and the length of the line AB ; also the distance from A to the object GD ;

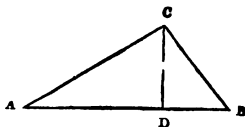


then $AB : BC :: AG : GD$. And suppose $AB = 150$ feet, $BC = 2$ feet, and $AG = 150$; then $6 : 2 :: 150 : 50$ feet, the height of D from G

Now, suppose the inaccessible distance AB be required, make the line BC at right angles, and BC of four equal parts of any constant distance, through one of which C draw a line with the object A , determine the triangle CDP , then the proportion will be as



1. The base of the triangle ADB is $11\frac{3}{8}$ inches in length, and the height DC , $3\frac{3}{8}$ inches; required the area.



$\frac{3}{8} = .09375$ and $\frac{3}{8} = .375$ (see page 31):

$$\text{hence } \frac{11.09375 \times 3.375}{2} = 18.72075 \text{ square inches, the area.}$$

2. The base of a triangle is 53 feet 3 inches, and the perpendicular 7 feet 9 inches; required the area or superficies.

$$\frac{53.25 \times 7.75}{2} = 206.84375 \text{ square feet, the area.}$$

When only the three sides of a triangle can be given, to find the area.

Rule.—From half the sum of the three sides, subtract each side severally; multiply the half sum and the three remainders together, and the square root of the product is equal to the area required.

Required the area of a triangle whose three sides are respectively 50, 40, and 30 feet.

$$\frac{50 + 40 + 30}{2} = 60, \text{ or half the sum of the three sides.}$$

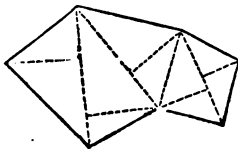
$$60 - 30 = 30, \text{ first difference,}$$

$$60 - 40 = 20, \text{ second difference,}$$

$$60 - 50 = 10, \text{ third difference;}$$

$$\text{then } 30 \times 20 \times 10 \times 60 = \sqrt{360000} = 600, \text{ the area required.}$$

Triangles are employed to great advantage in determining the area of any rectilinear figure, as the annexed, and by which the measurement is rendered comparatively simple.



es, and half the product is the area.

Angle at centre.	Angle at circum.	Perpen. side being 1.	Length of side, radius being 1.	Radius of circle, side being 1.	Radius of circle, per. being 1.	Area, side being 1.
0°	60°	0.2886	1.73	.579	2	0.4330
30	90	0.5	1.412	.705	1.41	1
45	108	0.6882	1.174	.852	1.238	1.7204
60	120	0.8660	1	1	1.156	2.5980
75	128½	1.0382	.867	1.16	1.11	3.6339
90	135	1.2071	.765	1.307	1.08	4.8284
105	140	1.3737	.681	1.47	1.062	6.1818
120	144	1.5388	.616	1.625	1.05	7.6942

Application of the Table.

1. The radius of a circle being $6\frac{1}{2}$ feet, required the side of the greatest heptagon that may be inscribed therein.

$$\cdot 867 \times 6\cdot 5 = 5\cdot 6355, \text{ or } 5 \text{ feet } 7\frac{1}{2} \text{ inches nearly.}$$

2. Each side of a pentagon is required to be 9 feet; required the radius of circumscribing circle.

$$\cdot 852 \times 9 = 7\cdot 668, \text{ or } 7 \text{ feet } 8 \text{ inches.}$$

3. A perpendicular from the centre to either side of an octagon is required to be 12 feet; what must be the radius of circumscribing circle?

$$1\cdot 08 \times 12 = 12\cdot 96, \text{ or } 12 \text{ feet } 11\frac{1}{2} \text{ inches.}$$

4. Each side of a hexagon is $4\frac{1}{2}$ yards; required its superficial contents.

$$4\frac{1}{2}^2 \times 2\cdot 598 = 52\cdot 6095 \text{ square yards.}$$

THE CIRCLE AND ITS SECTIONS.

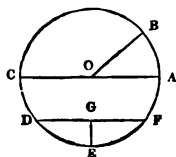
Observations and Definitions.

1. The circle contains a greater area than any other plane figure bounded by the same perimeter or outline.

2. The areas of circles are to each other as the squares of their diameters; any circle twice the diameter of another contains four times the area of the other.

3. The radius of a circle is a straight line drawn from the centre to the circumference, as O B.

4. The diameter of a circle is a straight line drawn through the centre, and terminated both ways at the circumference, as C O A.



... as $C E A$.

A segment is any portion of a circle cut off by a chord, as $D E F$.

A sector is a part of a circle cut off by two radii, as $A O B$.

General rules in relation to the circle.

Multiply the diameter by 3.1416 , the product is the circumference.

Multiply the circumference by $.31831$, the product is the diameter.

Multiply the square of the diameter by $.7854$, the product is the area.

Multiply the square root of the area by 1.128 , the product is the diameter.

Multiply the diameter by $.7854$, the product is the area of a square of equal area.

Multiply the side of a square by 1.128 , the product is the diameter of a circle of equal area.

Application of the rules as to purposes of practice.

being 274·89 inches, required the circle's diameter corresponding thereto.

$$\cdot 274 \cdot 89 \times \cdot 31831 = 87 \cdot 5 \text{ inches diameter.}$$

Or, what is the diameter of a circle when the circumference is 39 feet ?

$$\cdot 31831 \times 39 = 12 \cdot 41409 \text{ feet, and } \cdot 41409 \times 12 = 4 \cdot 96908 \text{ inches,}$$

or 12 feet 5 inches, very nearly the diameter.

3. The diameter of a circle is $3\frac{1}{2}$ inches; what is its area in square inches ?

$$3 \cdot 75^2 = 14 \cdot 0625 \times \cdot 7854 = 11 \cdot 044, \text{ \&c. inches area.}$$

Or, suppose the diameter of a circle 25 feet 6 inches, required the area.

$$25 \cdot 5^2 = 650 \cdot 25 \times \cdot 7854 = 510 \cdot 706, \text{ \&c. feet, the area.}$$

4. What must the diameter of a circle be, to contain an area equal to 706·86 square inches ?

$$\sqrt{706 \cdot 86} = 26 \cdot 586 \times 1 \cdot 12837 = 29 \cdot 998 \text{ or } 30 \text{ inches, the diameter required.}$$

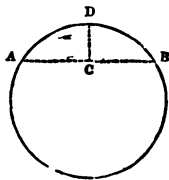
5. The diameter of a circle is $14\frac{1}{2}$ inches; what must I make each side of a square, to be equal in area to the given circle ?

$$14 \cdot 25 \times \cdot 8862 = 12 \cdot 62835 \text{ inches, length of side required.}$$

A chord and versed sine given to find the diameter.

Rule.—Divide the sum of the squares of half the chord and versed sine, by the versed sine; the quotient is the diameter.

1. The chord of a circle AB equal $6\frac{1}{2}$ feet, and the versed sine CD equal 2 feet; required the circle's diameter.



$$\frac{1}{2} (6 \cdot 5)^2 = 3 \cdot 25, \text{ and } 3 \cdot 25^2 + 2^2 = 7 \cdot 28125 \text{ feet diameter.}$$

$$1.25 \times 2$$

to find the length of any given arc of a circle.

Rule.—From eight times the chord of half the arc, subtract the chord of the whole arc, and one-third of the remainder is equal the length of the arc.

Example.—Required the length of the arc A B C, the

chord A B of half the arc

is 4 feet, 3 inches, and

the chord A C of the whole arc 8 feet 4 inches.

$25 \times 8 = 34$, and $34 - 8.333 = \frac{25.667}{3} = 8.555$ feet the length of the arc.



to find the area of the sector of a circle.

Rule.—Multiply the length of the arc by its radius, and half the product is the area.

Example.—Required the area of the sector A C B

where the radius is 9½ feet, and the radii F A,

equal each 7 feet; required the area.

$\frac{1}{2} \times 7 = 65.5 \div 2 = 32.75$ the area



Thus, suppose the area of the segment $A O B A$ is required, and that the length of the arc $A O B$ equal $9\frac{3}{4}$ feet, $F A$ and $F B$ each equal 7 feet, and the chord $A B$ equal 8 feet 4 inches, also the perpendicular $e F$ equal $3\frac{3}{4}$ feet.

$$\frac{9.75 \times 7}{2} = 34.125 \text{ feet, the area of the sector.}$$

$$\frac{8.333 \times 3.75}{2} = 15.624 \text{ feet, area of the triangle.}$$

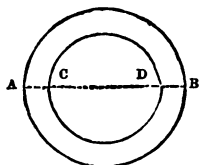
And $34.125 - 15.624 = 18.501$ feet, the area of the segment.

To find the area of the space contained between two concentric circles.

Rule.—Multiply the sum of the inside and outside diameters by their difference, and by $\cdot 7854$; the product is the area.

1. Suppose the external circle $A B$ equal 32 inches, and internal circle $C D$ equal 28 inches; required the area of the space contained between them.

$32 + 28 = 60$, and $32 - 28 = 4$; hence $60 \times 4 \times \cdot 7854 = 188.496$ in. the area.



2. The exterior diameter of the fly-wheel of a steam engine is 20 feet, and the interior diameter $18\frac{1}{2}$ feet; required the area of the surface or rim of the wheel.

$20 + 18.5 = 38.5$, and $20 - 18.5 = 1.5$; hence $38.5 \times 1.5 \times \cdot 7854 = 45.35$, &c. feet, the area.

To find the area of an ellipse or oval.

Rule.—Multiply the longest diameter by the shortest, and the product by $\cdot 7854$; the result is the area.

An oval is 25 inches by 16.5; what are its superficial contents?

... multiply the base by the perpendicular height, and two-thirds of the product is the area.
 What is the area of a parabola whose base and height 12?

$$20 \times 12 = \frac{240 \times 2}{3} = 160 \text{ feet, the area.}$$

etc.—Although the whole of the preceding propositions or examples are given in measures of feet, these being considered as the most generally familiar, the rules are equally applicable to any other measurement whatever, as yards, chains, acres, &c. &c.

MENSURATION OF THE SUPERFICIES, SOLIDITIES, AND CAPACITIES OF BODIES.

To find the solidity or capacity of any figure of a cubical form.

Rule.—Multiply the length of any one side by its breadth and by the depth or distance to its opposite side; the product is the solidity or capacity, in cubic feet, of measurement.

Application of the rule to question 1.

capacity in cubic feet, also its capacity in British imperial gallons.

$8.5 \times 5.25 \times 4 = 178.5$ cubic feet, and 178.5×6.232 (see Table of Decimal Approximations, p. 30) $= 1112.412$ gallons.

3. A rectangular cistern capable of containing 520 imperial gallons is to be $7\frac{1}{4}$ feet in length, and $4\frac{1}{2}$ feet in width; it is required to ascertain the necessary depth.

$7.25 \times 4.5 \times 6.232 = 203.318$, and $\frac{520.000}{203.318} = 2.557$ feet, or 2 feet $6\frac{3}{4}$ inches nearly.

4. A rectangular piece of cast iron, 20 inches long and 6 inches broad, is to be formed of sufficient dimensions to weigh 150 lbs.; what will be the depth required?

$20 \times 6 \times .263$ (see Table of Decimal Approximations, Cast Iron, p. 30) $= 31.96$, and $\frac{150}{31.96} = 4.69$ in., or 4 and $\frac{11}{16}$ in., the thickness required.

To find the convex surface, and solidity or capacity of a cylinder.

Rule. 1.—Multiply the circumference of the cylinder by its length or height; the product is the convex surface.

Rule 2.—Multiply the area of the base into the length or height; and the product is the cylinder's solidity or capacity, as may be required.

Application of the rules.

1. The circumference of a cylinder is $37\frac{1}{2}$ inches, and its length $54\frac{3}{4}$ inches; required the convex surface in square feet.

$54.75 \times 37.5 \times .007$ (see Table of Approximations) $= 14.371$ square feet.

2. A cylindrical piece of timber is 9 inches dia-

and $10\frac{1}{2}$ feet from the bottom to the surface; how many imperial gallons are contained?

$$4.75^2 \times 16.5 \times 4.895 = 1822.162 \text{ gallons}$$

4. Again, suppose the well's diameter and its entire depth 35 feet; required the cubic yards of material excavated in its

$$4.75^2 \times 35 \times .02909 = 22.973 \text{ cubic yard}$$

5. I have a cylindrical cistern capable of holding 7068 gallons, and its depth is 10 feet; want to replace it with one of an equal capacity capable of holding 12,500 gallons; what is its diameter?

$$4.895 \times 10 = 48.95, \text{ and } \frac{12500}{48.95} = \sqrt{255.3} = 15.9 \text{ feet } 11\frac{1}{8} \text{ inches.}$$

6. A cylindrical piece of lead is required to weigh 168 lbs. in weight; what is its length in inches?

$$7.5^2 \times .3223 = 18, \text{ and } \frac{168}{18} = 9.3 \text{ inches.}$$

Application of the rule.

1. Required the length of the thread or screw twisting round a cylinder 22 inches in circumference $3\frac{1}{2}$ times, and extending along the axis 16 inches.

$22 \times 3.5 = 77^2 = 5929$, and $16^2 = 256$; then $\sqrt{5929 + 256} = 78.64$ inches.

2. The well of a winding staircase is 5 feet diameter, and height to the top landing 25 feet, the hand-rail is to make $2\frac{1}{2}$ revolutions; required its length.

5 feet diameter = 15.7 feet circumference.

$15.7 \times 2.5 = 39.25^2 = 1540.5625$, and $25^2 = 625$; then

$\sqrt{1540 + 625} = 46.5$ feet, the length required.

To find the convex surface, solidity, or capacity of a cone or pyramid.

Rule 1.—Multiply the circumference of the base by the slant height, and half the product is the slant surface.

Rule 2.—Multiply the area of the base by the perpendicular height, and one-third of the product is the solidity or capacity, as may be required.

Application of the rules.

1. Required the area in square inches of the slant surface of a cone whose slant height equals $18\frac{3}{4}$ inches, and diameter at the base $6\frac{1}{4}$ inches.

$6.25 \times 3.1416 = 19.635$, circumference of the base; and

$$\frac{19.635 \times 18.75}{2} = 184.078125$$
 square inches.

2. Required the quantity of lead, in square feet, sufficient to cover the slant surface of a hexagonal pyramid whose slant height is 42 feet, and the breadth of each side at the base 4 feet 9 inches.

$$\frac{4.75 \times 42 \times 6 \text{ sides}}{2} = 598.5$$
 square feet.

. In a square solid pyramid of stone 67 feet high, and 16½ feet at the base, how many cubic feet?

$$\frac{16.5 \times 16.5 \times 67}{3} = 6080.25 \text{ cubic feet.}$$

To find the solidity or capacity of any frustum of a cone or pyramid.

Rule.—If the base be a circle, add into the square of the diameter two diameters, or, if a regular polygon, add into the square of one side at the top and at the bottom two sides; if the square of the sum subtract the square of the sum of the diameters or breadths; multiply the remainder by .7854, if a circle, or by the tabular multiplier of Polygons, p. 36) and by one-third the height, and the product is the content in cubic feet.

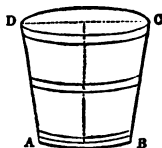
Note.—Where the whole height of the cone or cylinder is not obtained, of which the given frustum forms a part, the most simple method is first to find the whole height, then the contents extending beyond the frustum, and subtracting the less from the greater, leaves the content of the frustum required.

$3.75 + 2.5 = 6.25$, and $6.25 \times 6.25 = 39.0625$; then $3.75 \times 2.5 = 9.375$, and $39.0625 - 9.375 = 29.6875 \times 2.598$ (tabular area, p. 36) $= 77.138 \times 2.5$ or $\frac{1}{4}$ of the height $= 192.845$ cubic feet.

2. Required the solidity of the frustum of a cone, the top diameter of which is 7 inches, the base diameter $9\frac{1}{2}$, and the perpendicular height 12.

$(7 + 9.5) \div 2 = 272.25$, and $7 \times 9.5 = 66.5$; then $272.25 - 66.5 = 205.75 \times 7854 = 161.576 \times 4$ or $\frac{1}{4}$ of the height $= 646.3$ cubic inches.

3. A vessel in the form of an inverted cone, as $A B C D$, is 5 feet in diameter at the top, 4 feet at the bottom, and 6 feet in depth; required its capacity in imperial gallons.



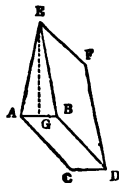
$5 + 4 = 9^2 = 81$, and $5 \times 4 = 20$; hence $81 - 20 = 61 \times .7854$, and by 2 or $\frac{1}{4}$ of the depth $= 95.8188$ cubic feet, and $\times 6.232 = 597.1427$ gallons.

To find the solid contents of a wedge.

Rule.—To twice the length of the base add the length of the edge; multiply the sum by the breadth of the base, and by the perpendicular height from the base, and one-sixth of the product is the solid contents.

Application of the rule.

Required the solidity of a wedge in cubic inches, the base $A B C D$ being 9 inches by $3\frac{1}{2}$, the edge $E F$, 7 inches, and the perpendicular height $G E$, 15.



$$\frac{18 + 7 \times 3.5 \times 15}{6} = 218.75 \text{ cubic inches.}$$

of the product is the solid contents.

Rule 3.—Multiply the cube of the diameter in inches by .001888, the product is the capacity in imperial gallons.

Application of the rules.

Required the convex surface, the solid weight in cast iron, of a sphere or ball 10 inches in diameter.

$$\times 8.1416 = 346.3614 \text{ square inches.}$$

$$\times .5236 = 606.132, \text{ \&c. cubic inches, and}$$

$$32 \times .263 \text{ (see Table of Approximations, p. 30) =}$$

A hollow or concave copper ball is 10 inches diameter, and in weight just sufficient to its centre in common water; what is the thickness of copper of which it is made?

$$\begin{array}{l} \text{Weight of a cubic inch of water} = .03617 \text{ lbs.} \\ \text{Weight of a cubic inch of copper} = .3225 \text{ lbs.} \end{array} \left. \vphantom{\begin{array}{l} \text{Weight of a cubic inch of water} \\ \text{Weight of a cubic inch of copper} \end{array}} \right\} \text{see}$$

$$\frac{236 \times .03617}{2} = 4.84828 \text{ cub. in. of water to be displaced}$$

$$\frac{4.84828}{.3225} = 15.0334 \text{ cubic inches of copper in the shell}$$

To ascertain the amount of convex surface, also the solid contents, of the segment of a globe.

Rule 1.—Multiply the circumference of the globe or sphere by the height of the segment, and the product is the convex surface.

Rule 2.—To three times the square of the segment's radius add the square of its height, multiply the sum by the height, and by $\cdot 5236$; the product is the solid contents.

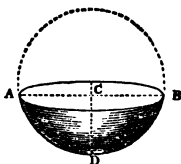
Application of the Rules.

1. Required the number of square feet in the convex surface of a sphere, the height of which is $9\frac{1}{2}$ feet, and the circumference of the sphere of which it is a part equal $70\frac{1}{2}$ feet.

$$70\cdot 5 \times 9\cdot 5 = 669\cdot 75 \text{ square feet.}$$

2. The radius $A C$ or $B C$ of the spherical segment $A D B$ equal 48 inches, and the height $D C$ equal 12 inches; required its solidity in cubic inches.


$$\begin{aligned} 48^2 \times 3 &= 6912, \text{ and } 12^2 = 144; \text{ then} \\ \frac{6912 + 144 \times 12 \times \cdot 5236}{\text{cubic inches.}} &= 44334\cdot 75 \end{aligned}$$



To find the convex surface and solidity of a cylindrical ring.

Rule 1.—To the sectional diameter of the ring add the inner diameter of the circle, multiply the sum by the sectional diameter, and by $9\cdot 8696$; the product is the convex surface.

Rule 2.—To the sectional diameter of the ring add the inner diameter of the circle, multiply the sum by the square of the sectional diameter, and by $2\cdot 4674$; the product is the solid contents.

required the convex surface  and solidity of the ring.

18 feet \times 12 = 216 inches, and

$216 + 9 \times 9 \times 2.8696 = 19985.94$

square inches.

$216 + 9 \times 9^2 \times 2.4674 = 44968.365$ cubic inches.

In the formation of a hoop or ring of w it is found in practice, that in bending t side or edge which forms the interior diam hoop is upset or shortened, while at the the exterior diameter is drawn or lengthen fore, the proper diameter by which to det length of the iron in an unbent state, is t from centre to centre of the iron of whic is composed: *hence the rule to determin of the iron.* If it is the interior diameter (that is given, add the thickness of the i the exterior diameter, subtract from the meter the thickness of the iron, multiply remainder by 3.1416, and the product is of the iron.

Supposing the interior diameter of a

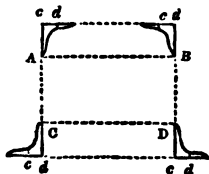
tain, let it be required to form a hoop of iron 1 in thickness, and $16\frac{1}{2}$ inches outside diameter.

$16.5 - .875 = 15.625$, or 1 foot $3\frac{1}{8}$ inches;

site to which, in the Table of Circumferences, feet 1 inch, independent of any allowance for ing.

the length for angle iron, of which to form a ring given diameter, varies according to the strength of the iron at the root; and the rule is, for a ring with the flange outside, *add* to its required interior diameter, twice the extreme strength of the iron at the root; or, for a ring with the flange inside, *subtract* twice the extreme strength; and the sum or difference is the diameter by which to determine the length of the angle iron. Thus,

use two angle iron rings as to the following be read, the exterior diameter A B, and interior diameter C D, to be 1 foot $10\frac{1}{2}$ inches, the extreme length of the iron at the root $c d$, $c d$, &c. $\frac{1}{4}$ inch.



$\frac{1}{4} = 1\frac{1}{4}$, and $1 \text{ ft. } 10\frac{1}{2} \text{ in.} + 1\frac{1}{4} = 2 \text{ ft. } \frac{1}{2} \text{ in.}$, opposite to which, in the Table of Circumferences, is 6 ft. $4\frac{1}{2}$ in., the length of the iron for C D; and $1 \text{ ft. } 10\frac{1}{2} \text{ in.} - 1\frac{1}{4} = 1 \text{ ft. } 8\frac{3}{4} \text{ in.}$, opposite to which is 5 ft. $5\frac{1}{2}$ in., the length of the iron for A B.

observe as before, that the necessary allowance for cutting must be added to the length of the iron, in addition to the length as expressed by the Table.

owing, with reference to the annexed plan.

Length, or dist. between A and B	= 10 ft.	2 $\frac{3}{4}$ in. or
Breadth	0 " D = 6 "	7 $\frac{1}{2}$ "
Length	1 " g = 3 "	10 $\frac{3}{4}$ "
Mean breadth of coke space or	} lm " = 3 "	1 $\frac{1}{2}$ "
Diameter of circle		rn " = 2 "
" "	ps " = 1 "	6 $\frac{1}{2}$ "
Radius of back corners	vx " =	4 "

Then, $122.75 \times 79.5 = 9758.525$ square inches, as:

And $18.5^2 \times .7854 = 268.8$ " " are formed by the two ends.

Total $\frac{10027.325}{}$ " " from deduct the area of the coke space, and the difference between the semicircle formed by the two back corners of a rectangle of equal length and breadth;

Then $46.75 \times 37.25 = 1731.4375$ area of r, n, s, t.

$\frac{32.25^2 \times .7854}{2} = 408.4$ area of half the

Radius of back corners = 4 inches; consequently $8^2 \times .7854 = 25.13$, the semicircle and $8 \times 4 = 32 - 25.13 = 6.87$ inches taken off by the corners.

Hence, $1731.4375 + 408.4 + 6.87 = 2146.707$, as

standard of comparison, or 1000.

Names.	Specific gravity.	Melting points in degrees of Fahrenheit.	Contraction in parts of an in. per lineal ft. from the fluid to the solid state.	Ultimate cohesive strength of an inch sq. prism in tons.	Scale of wire-drawing ductility.	Scale of laminae ductility.	Ratio of hardness.	Scale as conductors of electricity.	Ratio of power in the conduction of heat.	Names.	Specific gravity.	Weight of a cubic foot in lbs.	Cubic feet in a ton.	Tons required to crush 14-inch cubes.	STONES, EARTHS, &c.
Platinum	19500	3280	—	—	3	5	—	—	3·8	Marble, average	2720	170·00	13	9·25	
Pure Gold	19258	2016	—	—	1	1	1·8	3	10·0	Granite, do. . .	2651	165·68	13½	6·2	
Mercury	13500	—	—	—	8	7	—	6	1·8	Purbeck stone .	2601	162·56	13½	9·0	
Lead	11353	612	·319	·81	2	2	1·0	2	9·7	Portland do. . .	2370	160·62	14	4·5	
Pure Silver	10474	1873	—	—	2	2	2·4	—	—	Bristol do. . . .	2554	160·62	14	—	
Bismuth	9823	476	·156	1·45	—	—	2·0	—	—	Millstone	2484	155·25	14½	—	
Copper, cast . . .	8788	1996	·193	8·51	5	3	2·8	1	8·9	Paving stone . .	2415	150·93	14½	5·7	
" wrought	8910	—	15·08	15·08	—	—	{ to any degree	—	—	Craighleith do. .	2363	147·62	15	5·0	
Brass, cast	7824	1900	·210	8·01	—	—	{ to any degree	—	—	Grindstone . . .	2143	133·93	16½	6·6	
" sheet	8396	—	—	12·23	6	6	—	—	8·6	Chalk, Brit. . . .	2781	173·81	12½	0·5	
Iron, cast	7864	2786	·125	7·87	—	—	{ to any degree	—	—	Brick	2000	125·00	17	0·8	
" bar	7700	—	·137	25·00	4	8	4·7	4	—	Coal, Scotch . .	1300	81·15	27½	—	
Steel, soft	7833	—	·133	53·91	—	—	—	—	—	" Newcastle . .	1270	79·37	27½	—	
" hard	7816	—	—	—	—	—	{ to any degree	—	—	" Staffordsh. . .	1240	77·50	29	—	
Tin, cast	7291	443	·278	3·11	8	4	1·2	—	—	" Cannel	1238	77·37	29	—	
Zinc, cast	7190	773	·329	5·06	7	8	1·6	7	3·6						

Names.	Specific gravity, 10	Average cubic foot	Cubic feet a ton.	Ultimate strength in inch square	Stiffness
English oak	934	58	38 $\frac{1}{2}$	11880	100
Riga do.	872	54	41 $\frac{1}{2}$	12888	92
Dantzic do.	756	47	48	12780	117
American do.	672	42	53	10253	114
Beech	852	48	45	12225	77
Alder	800	46	48 $\frac{1}{2}$	9540	63
Plane	640	40	55	10935	78
Sycamore	604	38	59	9630	55
Chestnut	610	38	59	10656	67
Ash	845	52	43	14130	89
Elm	673	42	53	9720	78
Mahog. Spanish . .	800	50	45	7560	73
„ Honduras	637	40	55	11475	92
Walnut	671	42	53	8800	49
Teak	750	46	48 $\frac{1}{2}$	12915	126
Poona	640	40	55	12350	99
African oak	944	59	38	17200	101
Poplar	383	34	66	5928	44
Cedar	561	33	68	7420	28
Riga fir	753	47	48	9540	98
Memel do.	546	34	66	9540	114
Scotch do.	528	33	68	7110	55
Christ. wh ^{te} . deal .	590	37	60	12346	104

LIQUIDS.			GASES.	
Names.	Specific grav., water, 1000.	Weight of an Imperial gall. in lbs.	Atmospheric air being the standard of comparison, or 1000.	
			Names.	Specific gravity.
Acid, sulphuric ..	1850	18·5	Hydriodic acid gas	4340
" nitric	1271	12·7	Chlorine acid "	2500
" muriatic ...	1200	12·0	Carbonic acid "	1527
" fluoric.....	1060	10·6	Nitrous oxide "	1527
" citric.....	1034	10·3	Cyanogen "	1805
" acetic	1062	10·6	Oxygen "	1111
Water from the			Carbonic oxide "	972
Baltic	1015	10·2	Carburetted hydrogen	
Water from the			gas	972
Dead Sea	1240	12·4	Prussic acid "	937
Water from the			Ammoniacal do. "	590
Mediterranean .	1029	10·3	Steam of water "	623
Water, distilled ..	1000	10·0	Hydrogen "	69
Oils, expressed :			Weight of water at the com- mon temperature :	
" linseed	940	9·4		
" sweet almond	932	9·3	1 cubic inch =	·03617 lb.
" whale	923	9·2	1 " foot =	62·5 "
" hempseed...	926	9·3	1 " " =	6·25 imp. galls.
" olive.....	915	9·2	1·8 " " =	1 cwt.
Oils, essential :			1 cylindrical inch =	·02842 lb.
" cinnamon...	1043	10·4	1 " foot =	49·1 "
" lavender....	894	8·9	1 " " =	5 imp. galls.
" turpentine ..	870	8·7	2·282 feet =	1 cwt.
" amber.....	868	8·7	11·2 imp. gallons =	1 cwt.
Alcohol	825	8·2	224 " " =	1 ton.
Ether, nitric	908	9·1		
Proof spirit.....	922	9·2		
Vinegar	1009	10·1		

1-2	1000	1-2	1000	1-2	1000
$\frac{1}{2}$	208	2	13.33	$\frac{1}{2}$	163
$\frac{1}{3}$	325	$2\frac{1}{2}$	15.05	$\frac{1}{3}$	255
$\frac{1}{4}$	468	$2\frac{1}{2}$	16.87	$\frac{1}{4}$	368
$\frac{1}{5}$	638	$2\frac{3}{4}$	18.80	$\frac{1}{5}$	501
$\frac{1}{6}$	833	$2\frac{1}{2}$	20.81	$\frac{1}{6}$	654
$\frac{1}{7}$	1.05	$2\frac{3}{4}$	22.96	$\frac{1}{7}$	828
$\frac{1}{8}$	1.30	$2\frac{3}{4}$	25.20	$\frac{1}{8}$	1.02
$\frac{1}{9}$	1.57	$2\frac{3}{4}$	27.55	$\frac{1}{9}$	1.23
$\frac{1}{10}$	1.87	3	30.00	$\frac{1}{10}$	1.47
$\frac{1}{11}$	2.20	$3\frac{1}{2}$	32.55	$\frac{1}{11}$	1.72
$\frac{1}{12}$	2.55	$3\frac{1}{2}$	35.20	$\frac{1}{12}$	2.00
$\frac{1}{13}$	2.92	$3\frac{3}{4}$	37.96	$\frac{1}{13}$	2.30
1	3.33	$3\frac{1}{2}$	40.80	1	2.61
$1\frac{1}{10}$	3.76	$3\frac{3}{4}$	43.81	$1\frac{1}{10}$	2.95
$1\frac{1}{8}$	4.21	$3\frac{3}{4}$	46.87	$1\frac{1}{8}$	3.31
$1\frac{3}{10}$	4.70	$3\frac{3}{4}$	50.05	$1\frac{3}{10}$	3.69
$1\frac{1}{4}$	5.20	4	53.33	$1\frac{1}{4}$	4.09
$1\frac{5}{10}$	5.74	$4\frac{1}{2}$	60.20	$1\frac{5}{10}$	4.51
$1\frac{1}{2}$	6.30	$4\frac{1}{2}$	67.50	$1\frac{1}{2}$	4.95
$1\frac{7}{10}$	6.88	$4\frac{1}{2}$	75.20	$1\frac{7}{10}$	5.40
$1\frac{3}{4}$	7.50	5	83.33	$1\frac{3}{4}$	5.89
$1\frac{9}{10}$	8.15	$5\frac{1}{2}$	92.43	$1\frac{9}{10}$	6.40
$1\frac{1}{2}$	8.80	$5\frac{1}{2}$	101.03	$1\frac{1}{2}$	6.91
$1\frac{11}{10}$	9.50	$5\frac{1}{2}$	110.40	$1\frac{11}{10}$	7.46
$1\frac{3}{4}$	10.20	6	120.21	$1\frac{3}{4}$	8.01
$1\frac{13}{10}$	10.69	6.1	130.20	$1\frac{13}{10}$	8.60

WEIGHTS OF IRON.

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WEIGHT OF A LINEAL FOOT OF FLAT BAR IRON IN POUNDS.

Breadth in inches.	Thickness in parts of an inch.						
	$\frac{1}{8}$	$\frac{5}{16}$	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{9}{16}$	$\frac{5}{8}$
$\frac{1}{8}$	·417	·52	—	—	—	—	—
$\frac{3}{16}$	·52	·65	·78	·91	—	—	—
$\frac{1}{4}$	·625	·785	·93	1·09	1·25	1·40	—
$\frac{5}{16}$	·725	·91	1·09	1·27	1·46	1·64	1·82
1	·834	1·04	1·25	1·45	1·67	1·87	2·08
$1\frac{1}{8}$	·937	1·17	1·40	1·64	1·87	2·10	2·34
$1\frac{1}{4}$	1·04	1·30	1·56	1·82	2·08	2·34	2·60
$1\frac{3}{8}$	1·14	1·43	1·71	2·00	2·29	2·57	2·86
$1\frac{1}{2}$	1·25	1·56	1·87	2·18	2·50	2·81	3·12
$1\frac{5}{8}$	1·35	1·69	2·03	2·36	2·70	3·04	3·38
$1\frac{3}{4}$	1·45	1·82	2·18	2·55	2·91	3·28	3·64
$1\frac{7}{8}$	1·56	1·95	2·34	2·73	3·12	3·51	3·90
2	1·66	2·08	2·50	2·91	3·33	3·75	4·16
$2\frac{1}{8}$	1·77	2·21	2·65	3·09	3·54	3·98	4·42
$2\frac{1}{4}$	1·87	2·34	2·81	3·28	3·75	4·21	4·68
$2\frac{3}{8}$	1·97	2·47	2·96	3·46	3·95	4·45	4·94
$2\frac{1}{2}$	2·08	2·60	3·12	3·64	4·16	4·68	5·20
$2\frac{5}{8}$	2·18	2·73	3·28	3·82	4·37	4·92	5·46
$2\frac{3}{4}$	2·29	2·86	3·43	4·01	4·58	5·15	5·72
$2\frac{7}{8}$	2·39	2·99	3·59	4·19	4·79	5·39	5·98
3	2·50	3·12	3·75	4·37	5·00	5·62	6·25
$3\frac{1}{8}$	2·70	3·38	4·06	4·73	5·41	6·09	6·77
$3\frac{1}{4}$	2·91	3·64	4·37	5·10	5·83	6·56	7·29
$3\frac{3}{8}$	3·12	3·90	4·68	5·46	6·25	7·03	7·81
4	3·33	4·16	5·00	5·83	6·66	7·50	8·33
$4\frac{1}{8}$	3·54	4·42	5·31	6·19	7·08	7·96	8·85
$4\frac{1}{4}$	3·75	4·68	5·62	6·56	7·50	8·43	9·37
$4\frac{3}{8}$	3·95	4·94	5·93	6·92	7·91	8·90	9·89
5	4·17	5·20	6·25	7·29	8·33	9·37	10·41
$5\frac{1}{8}$	4·37	5·46	6·56	7·65	8·75	9·84	10·93
$5\frac{1}{4}$	4·58	5·72	6·87	8·02	9·16	10·31	11·45
$5\frac{3}{8}$	4·79	5·98	7·18	8·38	9·58	10·78	11·97
6	5·	6·26	7·50	8·75	10·00	11·25	12·50

$1\frac{1}{8}$	2·57	2·81	3·04	—	—	—
$1\frac{1}{4}$	2·86	3·12	3·38	3·64	3·90	—
$1\frac{3}{8}$	3·15	3·43	3·72	4·01	4·29	4·
$1\frac{1}{2}$	3·43	3·75	4·06	4·37	4·68	5·
$1\frac{5}{8}$	3·72	4·06	4·40	4·73	5·07	5·
$1\frac{3}{4}$	4·01	4·37	4·73	5·10	5·46	5·
$1\frac{7}{8}$	4·29	4·68	5·07	5·46	5·85	6·
2	4·58	5·00	5·41	5·83	6·25	6·
$2\frac{1}{8}$	4·86	5·31	5·75	6·19	6·64	7·
$2\frac{1}{4}$	5·15	5·62	6·09	6·56	7·03	7·
$2\frac{3}{8}$	5·44	5·93	6·43	6·92	7·42	7·
$2\frac{1}{2}$	5·72	6·25	6·77	7·29	7·81	8·
$2\frac{5}{8}$	6·01	6·56	7·10	7·65	8·20	8·
$2\frac{3}{4}$	6·30	6·87	7·44	8·02	8·59	9·
$2\frac{7}{8}$	6·58	7·18	7·78	8·38	8·98	9·
3	6·87	7·50	8·12	8·75	9·37	10·
$3\frac{1}{8}$	7·44	8·12	8·80	9·47	10·15	10·
$3\frac{1}{4}$	8·02	8·75	9·47	10·20	10·93	11·
$3\frac{3}{8}$	8·59	9·37	10·15	10·93	11·71	12·
4	9·16	10·00	10·83	11·66	12·50	13·
$4\frac{1}{8}$	9·73	10·62	11·51	12·39	13·28	14·
$4\frac{1}{4}$	10·31	11·25	12·18	13·12	14·06	15·
$4\frac{3}{8}$	10·88	11·87	12·86	13·85	14·84	15·
5	11·45	12·50	13·54	14·58	15·62	16·

WEIGHT OF FLAT BAR IRON—*continued.*

Breadth in inches.	Thickness in inches.					
	1 $\frac{1}{4}$	1 $\frac{3}{8}$	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{2}$
1 $\frac{1}{8}$	6·24	6·86	—	—	—	—
1 $\frac{3}{8}$	7·28	8·02	8·74	—	—	—
2	8·32	9·16	10·00	11·66	—	—
2 $\frac{1}{4}$	9·36	10·30	11·24	13·12	15·00	—
2 $\frac{1}{2}$	10·40	11·44	12·50	14·58	16·66	—
2 $\frac{3}{4}$	11·44	12·60	13·74	16·04	18·32	22·88
3	12·50	13·74	15·00	17·50	20·00	25·00
3 $\frac{1}{4}$	13·54	14·88	16·24	18·94	21·66	27·08
3 $\frac{1}{2}$	14·58	16·04	17·50	20·40	23·32	29·16
3 $\frac{3}{4}$	15·62	17·18	18·74	21·86	25·00	31·24
4	16·66	18·32	20·00	23·32	26·66	33·32
4 $\frac{1}{4}$	17·70	19·46	21·24	25·78	28·32	35·40
4 $\frac{1}{2}$	18·74	20·62	22·50	26·24	30·00	37·48
4 $\frac{3}{4}$	19·78	21·76	23·74	27·70	31·67	39·56
5	20·82	22·90	25·00	29·16	33·32	41·64
5 $\frac{1}{4}$	21·86	24·06	26·24	30·62	35·00	43·72
5 $\frac{1}{2}$	22·90	25·20	27·50	32·08	36·66	45·80
5 $\frac{3}{4}$	23·94	26·34	28·74	33·54	38·32	47·88
6	25·00	27·50	30·00	35·00	40·00	50·00
6 $\frac{1}{2}$	27·08	29·76	32·48	37·88	43·32	54·16
7	29·16	32·08	35·00	40·80	46·64	58·32
7 $\frac{1}{2}$	31·24	34·36	37·48	43·72	50·00	62·48
8	33·32	36·64	40·00	46·64	53·32	66·64
8 $\frac{1}{2}$	35·40	38·92	42·48	51·56	56·64	70·80
9	37·48	41·24	45·00	52·48	60·00	74·96

MECHANICAL TABLES

FOR THE USE OF OPERATIVE SMITHS, MILLWRIGHTS, AND
ENGINEERS.

The following Tables, originally dedicated to 'the National Association of the Forgers of Iron-Work,' are, with permission, added to the present edition: they will be found extremely useful to Smiths generally, and are accompanied by Observations and Practical Examples.

0	$3\frac{1}{8}$	$5\frac{1}{8}$	1	4	0	$9\frac{1}{8}$	2	$4\frac{1}{8}$
0	$3\frac{3}{8}$	$5\frac{3}{8}$	1	$4\frac{3}{8}$	0	$9\frac{3}{8}$	2	5
0	$4\frac{1}{8}$	$5\frac{5}{8}$	1	$4\frac{5}{8}$	0	$9\frac{5}{8}$	2	$5\frac{5}{8}$
0	$4\frac{3}{8}$	$5\frac{7}{8}$	1	$5\frac{1}{8}$	0	$9\frac{7}{8}$	2	$5\frac{7}{8}$
0	5	$5\frac{9}{8}$	1	$5\frac{3}{8}$	0	$9\frac{9}{8}$	2	$6\frac{1}{8}$
0	$5\frac{1}{8}$	$5\frac{1}{8}$	1	6	0	$9\frac{3}{8}$	2	$6\frac{3}{8}$
0	$5\frac{3}{8}$	$5\frac{3}{8}$	1	$6\frac{1}{8}$	0	$9\frac{5}{8}$	2	7
0	$6\frac{1}{8}$	6	1	$6\frac{3}{8}$	0	10	2	$7\frac{1}{8}$
0	$6\frac{3}{8}$	$6\frac{1}{8}$	1	$7\frac{1}{8}$	0	$10\frac{1}{8}$	2	$7\frac{3}{8}$
0	7	$6\frac{3}{8}$	1	$7\frac{3}{8}$	0	$10\frac{3}{8}$	2	$8\frac{1}{8}$
0	$7\frac{1}{8}$	$6\frac{5}{8}$	1	8	0	$10\frac{5}{8}$	2	$8\frac{3}{8}$
0	$7\frac{3}{8}$	$6\frac{7}{8}$	1	$8\frac{1}{8}$	0	$10\frac{7}{8}$	2	$8\frac{5}{8}$
0	$8\frac{1}{8}$	$6\frac{7}{8}$	1	$8\frac{3}{8}$	0	$10\frac{9}{8}$	2	$9\frac{1}{8}$
0	$8\frac{3}{8}$	$6\frac{3}{4}$	1	$9\frac{1}{8}$	0	$10\frac{3}{4}$	2	$9\frac{3}{8}$
0	9	$6\frac{7}{8}$	1	$9\frac{3}{8}$	0	$10\frac{5}{8}$	2	$10\frac{1}{8}$
0	$9\frac{1}{8}$	7	1	$9\frac{5}{8}$	0	11	2	$10\frac{3}{8}$
0	$9\frac{3}{8}$	$7\frac{1}{8}$	1	$10\frac{3}{8}$	0	$11\frac{1}{8}$	2	$10\frac{5}{8}$
0	$10\frac{1}{8}$	$7\frac{3}{8}$	1	$10\frac{5}{8}$	0	$11\frac{3}{8}$	2	$11\frac{1}{8}$
0	$10\frac{3}{8}$	$7\frac{5}{8}$	1	$11\frac{1}{8}$	0	$11\frac{5}{8}$	2	$11\frac{3}{8}$
0	$10\frac{5}{8}$	$7\frac{7}{8}$	1	$11\frac{3}{8}$	0	$11\frac{7}{8}$	3	0
0	$11\frac{1}{8}$	$7\frac{5}{8}$	1	$11\frac{5}{8}$	0	$11\frac{9}{8}$	3	$0\frac{1}{8}$
0	$11\frac{3}{8}$	$7\frac{3}{4}$	2	$0\frac{1}{4}$	0	$11\frac{3}{4}$	3	$0\frac{3}{8}$
1	$0\frac{1}{8}$	$7\frac{5}{8}$	2	$0\frac{3}{8}$	0	$11\frac{5}{8}$	3	$1\frac{1}{8}$
1	$0\frac{3}{8}$	8	2	$1\frac{1}{8}$	1	0	3	$1\frac{3}{8}$

CIRCLES ADVANCING BY AN EIGHTH.

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
ft.	in.	ft.	in.	ft.	in.	ft.	in.	ft.	in.	ft.	in.	ft.	in.	ft.	in.
1	5	4	5	1	9	5	7	2	1	6	8	2	6	7	10
1	5 $\frac{1}{2}$	4	5 $\frac{1}{2}$	1	9 $\frac{1}{2}$	5	7 $\frac{1}{2}$	2	1 $\frac{1}{2}$	6	9 $\frac{1}{2}$	2	6 $\frac{1}{2}$	7	11
1	5 $\frac{1}{4}$	4	6	1	9 $\frac{1}{4}$	5	8	2	2	6	9 $\frac{1}{4}$	2	6 $\frac{3}{4}$	7	11 $\frac{1}{2}$
1	5 $\frac{3}{4}$	4	6 $\frac{1}{4}$	1	9 $\frac{3}{4}$	5	8 $\frac{1}{4}$					2	6 $\frac{1}{2}$	7	11 $\frac{1}{4}$
1	5 $\frac{1}{2}$	4	6 $\frac{1}{2}$	1	9 $\frac{1}{2}$	5	8 $\frac{1}{2}$	2	2 $\frac{1}{2}$	6	10	2	6 $\frac{3}{4}$	8	0 $\frac{1}{2}$
1	5 $\frac{3}{8}$	4	7	1	10	5	9	2	2 $\frac{1}{2}$	6	10 $\frac{1}{2}$	2	6 $\frac{3}{4}$	8	0 $\frac{1}{2}$
1	5 $\frac{1}{4}$	4	7 $\frac{1}{4}$					2	2 $\frac{3}{4}$	6	10 $\frac{3}{4}$	2	6 $\frac{3}{4}$	8	0 $\frac{3}{4}$
1	5 $\frac{3}{8}$	4	7 $\frac{3}{8}$					2	2 $\frac{1}{2}$	6	11 $\frac{1}{2}$	2	6 $\frac{1}{2}$	8	0 $\frac{1}{2}$
1	5 $\frac{1}{2}$	4	8	1	10 $\frac{1}{2}$	5	9 $\frac{1}{2}$	2	2 $\frac{1}{2}$	6	11 $\frac{1}{4}$	2	7	8	1
1	6	4	8 $\frac{1}{2}$	1	10 $\frac{1}{4}$	5	9 $\frac{1}{4}$	2	2 $\frac{1}{2}$	6	11 $\frac{1}{8}$				
				1	10 $\frac{3}{4}$	5	10 $\frac{3}{4}$	2	2 $\frac{3}{4}$	7	0	2	7 $\frac{1}{8}$	8	1 $\frac{1}{8}$
1	6 $\frac{1}{2}$	4	9 $\frac{1}{2}$	1	10 $\frac{1}{2}$	5	10 $\frac{1}{2}$	2	2 $\frac{3}{4}$	7	0 $\frac{1}{2}$	2	7 $\frac{1}{4}$	8	2 $\frac{1}{4}$
1	6 $\frac{1}{4}$	4	9 $\frac{1}{4}$	1	10 $\frac{3}{4}$	5	11	2	3	7	0 $\frac{1}{4}$	2	7 $\frac{1}{2}$	8	2 $\frac{1}{2}$
1	6 $\frac{3}{4}$	4	10	1	10 $\frac{3}{4}$	5	11 $\frac{3}{4}$	2	3 $\frac{1}{2}$	7	1 $\frac{1}{2}$	2	7 $\frac{3}{4}$	8	3 $\frac{1}{4}$
1	6 $\frac{1}{2}$	4	10 $\frac{1}{2}$	1	10 $\frac{1}{2}$	5	11 $\frac{1}{2}$	2	3 $\frac{1}{4}$	7	1 $\frac{1}{4}$	2	7 $\frac{1}{2}$	8	3 $\frac{1}{2}$
1	6 $\frac{3}{8}$	4	10 $\frac{3}{8}$	1	11	6	0 $\frac{1}{4}$	2	3 $\frac{1}{2}$	7	2	2	7 $\frac{3}{8}$	8	4 $\frac{1}{8}$
1	6 $\frac{1}{4}$	4	10 $\frac{1}{4}$	1	11 $\frac{1}{8}$	6	0 $\frac{1}{8}$	2	3 $\frac{1}{2}$	7	2 $\frac{1}{2}$	2	8	8	4 $\frac{1}{2}$
1	6 $\frac{3}{8}$	4	11 $\frac{1}{8}$	1	11 $\frac{1}{4}$	6	1	2	3 $\frac{1}{2}$	7	2 $\frac{3}{4}$	2	8 $\frac{1}{4}$	8	5 $\frac{1}{4}$
1	7	4	11 $\frac{1}{2}$	1	11 $\frac{3}{8}$	6	1 $\frac{3}{8}$	2	3 $\frac{3}{4}$	7	3 $\frac{1}{4}$	2	8 $\frac{1}{2}$	8	5 $\frac{1}{2}$
				1	11 $\frac{1}{2}$	6	2 $\frac{1}{2}$	2	4	7	3 $\frac{3}{4}$	2	8 $\frac{3}{4}$	8	6
1	7 $\frac{1}{2}$	5	0	1	11 $\frac{1}{2}$	6	2 $\frac{1}{2}$	2	4 $\frac{1}{2}$	7	4 $\frac{1}{2}$	2	8 $\frac{1}{2}$	8	6 $\frac{1}{2}$
1	7 $\frac{1}{4}$	5	0 $\frac{1}{4}$	1	11 $\frac{3}{4}$	6	3	2	4 $\frac{1}{4}$	7	5 $\frac{1}{4}$	2	8 $\frac{3}{4}$	8	6 $\frac{3}{4}$
1	7 $\frac{1}{8}$	5	0 $\frac{1}{8}$	2	0	6	3 $\frac{3}{8}$	2	4 $\frac{1}{4}$	7	5 $\frac{1}{2}$	2	8 $\frac{1}{2}$	8	7 $\frac{1}{2}$
1	7 $\frac{3}{8}$	5	1 $\frac{1}{8}$	2	0 $\frac{1}{4}$	6	4 $\frac{1}{4}$	2	4 $\frac{1}{2}$	7	5 $\frac{3}{4}$	2	9		
1	7 $\frac{1}{2}$	5	1 $\frac{1}{2}$	2	0 $\frac{1}{2}$	6	4 $\frac{1}{2}$	2	4 $\frac{1}{2}$	7	6 $\frac{1}{2}$	2	9 $\frac{1}{2}$	8	8
1	7 $\frac{3}{8}$	5	1 $\frac{3}{8}$	2	0 $\frac{3}{4}$	6	4 $\frac{3}{4}$	2	4 $\frac{3}{4}$	7	6 $\frac{3}{4}$	2	9 $\frac{3}{4}$	8	8 $\frac{3}{4}$
1	7 $\frac{1}{4}$	5	2	2	0 $\frac{1}{2}$	6	5 $\frac{1}{2}$	2	5	7	7	2	9 $\frac{1}{4}$	8	9 $\frac{1}{4}$
1	7 $\frac{3}{8}$	5	2 $\frac{1}{8}$	2	0 $\frac{3}{8}$	6	5 $\frac{3}{8}$	2	5 $\frac{1}{4}$	7	7 $\frac{1}{4}$	2	9 $\frac{1}{8}$	8	9 $\frac{1}{8}$
1	8	5	3	2	0 $\frac{1}{4}$	6	5 $\frac{1}{4}$	2	5 $\frac{1}{2}$	7	7 $\frac{1}{2}$	2	9 $\frac{1}{2}$	8	10
				2	0 $\frac{1}{2}$	6	5 $\frac{1}{2}$	2	5 $\frac{3}{4}$	7	8 $\frac{1}{4}$	2	9 $\frac{3}{4}$	8	10 $\frac{1}{4}$
1	8 $\frac{1}{2}$	5	3 $\frac{1}{2}$	2	0 $\frac{3}{4}$	6	6	2	5 $\frac{1}{2}$	7	8 $\frac{1}{2}$	2	10		
1	8 $\frac{1}{4}$	5	3 $\frac{1}{4}$	2	0 $\frac{1}{4}$	6	6 $\frac{1}{4}$	2	5 $\frac{3}{4}$	7	9 $\frac{1}{4}$	2	10 $\frac{1}{4}$	8	11 $\frac{1}{4}$
1	8 $\frac{3}{8}$	5	4 $\frac{1}{8}$	2	0 $\frac{1}{2}$	6	6 $\frac{1}{2}$	2	5 $\frac{1}{4}$	7	9 $\frac{1}{2}$	2	10 $\frac{1}{2}$	8	11 $\frac{1}{2}$
1	8 $\frac{1}{2}$	5	4 $\frac{1}{2}$	2	0 $\frac{3}{8}$	6	6 $\frac{3}{8}$	2	5 $\frac{3}{8}$	7	9 $\frac{3}{8}$	2	10 $\frac{3}{8}$	8	11 $\frac{3}{8}$
1	8 $\frac{3}{4}$	5	5 $\frac{1}{4}$	2	1	6	6 $\frac{1}{2}$	2	6	7	10 $\frac{1}{2}$	2	10 $\frac{1}{2}$	8	11 $\frac{1}{2}$
1	8 $\frac{1}{4}$	5	5 $\frac{1}{4}$	2	1 $\frac{1}{4}$	6	7 $\frac{1}{4}$	2	6			2	10 $\frac{1}{4}$	8	11 $\frac{1}{4}$
1	9	5	5 $\frac{3}{4}$	2	1 $\frac{1}{2}$	6	7 $\frac{1}{2}$	2	6			2	10 $\frac{1}{2}$	8	11 $\frac{1}{2}$
				2	1 $\frac{3}{4}$	6	8 $\frac{1}{4}$								
1	9 $\frac{1}{2}$	5	6 $\frac{1}{2}$	2	1 $\frac{1}{2}$	6	8								
1	9 $\frac{1}{4}$	5	6 $\frac{1}{4}$	2	1 $\frac{3}{4}$	6	8 $\frac{1}{4}$								

9	2 $\frac{1}{2}$	3	3 $\frac{1}{2}$	10	3 $\frac{1}{2}$	3	7 $\frac{1}{2}$	11	5 $\frac{1}{2}$	—
9	2 $\frac{3}{8}$	3	3 $\frac{3}{8}$	10	4	3	7 $\frac{3}{8}$	11	5 $\frac{3}{8}$	4
9	3	3	3 $\frac{5}{8}$	10	4 $\frac{1}{8}$	3	8	11	6 $\frac{1}{8}$	4
9	3 $\frac{1}{4}$	3	3 $\frac{3}{4}$	10	4 $\frac{1}{4}$					4
9	3 $\frac{1}{2}$	3	3 $\frac{1}{2}$	10	5 $\frac{1}{4}$	3	8 $\frac{1}{4}$	11	6 $\frac{1}{4}$	4
9	3 $\frac{3}{8}$	3	3 $\frac{3}{8}$	10	5 $\frac{3}{8}$	3	8 $\frac{3}{8}$	11	7 $\frac{3}{8}$	4
9	4 $\frac{1}{8}$					3	8 $\frac{5}{8}$	11	7 $\frac{5}{8}$	4
9	4 $\frac{1}{4}$					3	8 $\frac{1}{2}$	11	7 $\frac{1}{2}$	4
9	4 $\frac{3}{8}$	3	4 $\frac{1}{8}$	10	6	3	8 $\frac{3}{4}$	11	8 $\frac{1}{4}$	4
9	5	3	4 $\frac{1}{4}$	10	6 $\frac{1}{4}$	3	8 $\frac{1}{2}$	11	8 $\frac{1}{2}$	4
		3	4 $\frac{3}{8}$	10	6 $\frac{3}{8}$	3	8 $\frac{3}{8}$	11	8 $\frac{3}{8}$	4
9	5 $\frac{1}{8}$	3	4 $\frac{1}{2}$	10	7 $\frac{1}{8}$	3	8 $\frac{1}{2}$	11	8 $\frac{1}{2}$	4
9	5 $\frac{1}{4}$	3	4 $\frac{3}{4}$	10	7 $\frac{1}{4}$	3	9	11	9 $\frac{1}{4}$	4
9	5 $\frac{3}{8}$	3	4 $\frac{5}{8}$	10	7 $\frac{3}{8}$					4
9	6 $\frac{1}{8}$	3	4 $\frac{1}{2}$	10	8	3	9 $\frac{1}{8}$	11	9 $\frac{1}{8}$	4
9	6 $\frac{1}{4}$	3	4 $\frac{3}{4}$	10	8 $\frac{1}{4}$	3	9 $\frac{1}{4}$	11	10 $\frac{1}{4}$	4
9	7	3	4 $\frac{7}{8}$	10	8 $\frac{3}{8}$	3	9 $\frac{3}{8}$	11	10 $\frac{3}{8}$	4
9	7 $\frac{1}{8}$	3	5	10	8 $\frac{1}{2}$	3	9 $\frac{1}{2}$	11	10 $\frac{1}{2}$	4
9	7 $\frac{1}{4}$					3	9 $\frac{3}{4}$	11	10 $\frac{3}{4}$	4
9	8 $\frac{1}{8}$	3	5 $\frac{1}{8}$	10	9 $\frac{1}{8}$	3	9 $\frac{5}{8}$	11	11 $\frac{1}{8}$	4
		3	5 $\frac{1}{4}$	10	9 $\frac{1}{4}$	3	9 $\frac{3}{4}$	11	11 $\frac{1}{4}$	4
9	8 $\frac{1}{4}$	3	5 $\frac{3}{8}$	10	9 $\frac{3}{8}$	3	9 $\frac{1}{2}$	12	0	4
9	9	3	5 $\frac{1}{2}$	10	10 $\frac{1}{8}$	3	10	12	0 $\frac{1}{8}$	4
9	9 $\frac{1}{8}$	3	5 $\frac{1}{4}$	10	10 $\frac{1}{4}$					4
9	9 $\frac{1}{4}$	3	5 $\frac{3}{8}$	10	11 $\frac{1}{8}$	3	10 $\frac{1}{8}$	12	0 $\frac{1}{8}$	4
9	10 $\frac{1}{8}$	3	5 $\frac{1}{2}$	10	11 $\frac{1}{4}$	3	10 $\frac{1}{4}$	12	1 $\frac{1}{4}$	4
9	10 $\frac{1}{4}$	3	5 $\frac{3}{4}$	10	11 $\frac{3}{8}$	3	10 $\frac{3}{8}$	12	1 $\frac{3}{8}$	4
9	10 $\frac{3}{8}$					3	10 $\frac{1}{2}$	12	2	4
9	10 $\frac{1}{2}$	3	6	10	11 $\frac{1}{2}$	3	10 $\frac{3}{4}$	12	2 $\frac{1}{4}$	4
9	11 $\frac{1}{8}$	3	6 $\frac{1}{4}$	11	0 $\frac{1}{2}$	3	10 $\frac{1}{2}$	12	2 $\frac{1}{2}$	4

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
t.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
1	3 $\frac{1}{8}$	13	6 $\frac{7}{8}$	4	8 $\frac{1}{8}$	14	8 $\frac{1}{8}$	5	0 $\frac{1}{2}$	15	10	5	4 $\frac{7}{8}$	16	11 $\frac{1}{2}$
1	4	13	7 $\frac{1}{4}$	4	8 $\frac{1}{4}$	14	8 $\frac{1}{4}$	5	0 $\frac{3}{4}$	15	10 $\frac{1}{2}$	5	5	17	0 $\frac{1}{2}$
1	4 $\frac{1}{8}$	13	7 $\frac{3}{8}$	4	8 $\frac{3}{8}$	14	9	5	0 $\frac{1}{4}$	15	10 $\frac{3}{4}$	5	5 $\frac{1}{8}$	17	0 $\frac{3}{8}$
1	4 $\frac{1}{4}$	13	8 $\frac{1}{4}$	4	8 $\frac{1}{2}$	14	9 $\frac{1}{2}$	5	0 $\frac{1}{2}$	15	11 $\frac{1}{8}$	5	5 $\frac{1}{4}$	17	1
1	4 $\frac{1}{2}$	13	8 $\frac{1}{2}$	4	8 $\frac{3}{4}$	14	10 $\frac{1}{4}$	5	1	15	11 $\frac{1}{4}$	5	5 $\frac{1}{2}$	17	1 $\frac{1}{8}$
1	4 $\frac{3}{4}$	13	9 $\frac{1}{4}$	4	9	14	11	5	1 $\frac{1}{8}$	16	0	5	5 $\frac{3}{4}$	17	1 $\frac{1}{4}$
1	4 $\frac{7}{8}$	13	9 $\frac{3}{8}$	4	9 $\frac{1}{4}$	14	11 $\frac{1}{4}$	5	1 $\frac{1}{4}$	16	0 $\frac{1}{4}$	5	5 $\frac{7}{8}$	17	2 $\frac{1}{8}$
1	5	13	10 $\frac{1}{2}$	4	9 $\frac{3}{8}$	14	11 $\frac{3}{8}$	5	1 $\frac{1}{2}$	16	0 $\frac{1}{2}$	5	5 $\frac{1}{4}$	17	2 $\frac{1}{4}$
1	5 $\frac{1}{8}$	13	10 $\frac{3}{8}$	4	9 $\frac{1}{2}$	15	0 $\frac{1}{2}$	5	1 $\frac{3}{4}$	16	1 $\frac{1}{8}$	5	5 $\frac{1}{2}$	17	2 $\frac{3}{8}$
1	5 $\frac{1}{4}$	13	11 $\frac{1}{4}$	4	9 $\frac{3}{4}$	15	0 $\frac{3}{4}$	5	2	16	2 $\frac{1}{8}$	5	6	17	3 $\frac{1}{4}$
1	5 $\frac{1}{2}$	14	0	4	10	15	2 $\frac{1}{8}$	5	2 $\frac{1}{8}$	16	3 $\frac{1}{8}$	5	6 $\frac{1}{8}$	17	4 $\frac{1}{8}$
1	5 $\frac{3}{4}$	14	0 $\frac{1}{8}$	4	10 $\frac{1}{8}$	15	2 $\frac{1}{8}$	5	2 $\frac{1}{4}$	16	3 $\frac{1}{4}$	5	6 $\frac{1}{4}$	17	4 $\frac{1}{4}$
1	5 $\frac{7}{8}$	14	1 $\frac{1}{8}$	4	10 $\frac{1}{4}$	15	2 $\frac{1}{4}$	5	2 $\frac{1}{2}$	16	4 $\frac{1}{8}$	5	6 $\frac{1}{2}$	17	5 $\frac{1}{8}$
1	6	14	1 $\frac{1}{4}$	4	10 $\frac{1}{2}$	15	3 $\frac{1}{8}$	5	2 $\frac{3}{8}$	16	4 $\frac{1}{4}$	5	6 $\frac{3}{8}$	17	5 $\frac{1}{4}$
1	6 $\frac{1}{8}$	14	2	4	10 $\frac{3}{4}$	15	3 $\frac{1}{4}$	5	2 $\frac{1}{2}$	16	5 $\frac{1}{8}$	5	6 $\frac{1}{2}$	17	6
1	6 $\frac{1}{4}$	14	2 $\frac{1}{4}$	4	11	15	5 $\frac{1}{4}$	5	3	16	5 $\frac{3}{4}$	5	7	17	6 $\frac{1}{4}$
1	6 $\frac{1}{2}$	14	3 $\frac{1}{2}$	4	11 $\frac{1}{8}$	15	5 $\frac{1}{8}$	5	3 $\frac{1}{4}$	16	6 $\frac{1}{4}$	5	7 $\frac{1}{8}$	17	7 $\frac{1}{8}$
1	6 $\frac{3}{4}$	14	4	4	11 $\frac{1}{4}$	15	6 $\frac{1}{4}$	5	3 $\frac{1}{2}$	16	7 $\frac{1}{8}$	5	7 $\frac{1}{4}$	17	8
1	6 $\frac{7}{8}$	14	4 $\frac{1}{8}$	4	11 $\frac{1}{2}$	15	6 $\frac{1}{2}$	5	3 $\frac{3}{4}$	16	8 $\frac{1}{4}$	5	7 $\frac{3}{4}$	17	8 $\frac{1}{2}$
1	7	14	4 $\frac{1}{4}$	4	11 $\frac{3}{4}$	15	7 $\frac{1}{4}$	5	4	16	9	5	8	17	9 $\frac{1}{4}$
1	7 $\frac{1}{8}$	14	5 $\frac{1}{8}$	4	12	15	8	5	4 $\frac{1}{8}$	16	9 $\frac{1}{8}$	5	8 $\frac{1}{8}$	17	10
1	7 $\frac{1}{4}$	14	5 $\frac{1}{4}$	4	12 $\frac{1}{4}$	15	8 $\frac{1}{4}$	5	4 $\frac{1}{4}$	16	9 $\frac{1}{4}$	5	8 $\frac{1}{4}$	17	10 $\frac{1}{4}$
1	7 $\frac{1}{2}$	14	6	5	0	15	8 $\frac{1}{2}$	5	4 $\frac{1}{2}$	16	10 $\frac{1}{2}$	5	8 $\frac{1}{2}$	17	11 $\frac{1}{2}$
1	7 $\frac{3}{4}$	14	6 $\frac{3}{4}$	5	0 $\frac{1}{4}$	15	9 $\frac{1}{4}$	5	4 $\frac{3}{4}$	16	11 $\frac{1}{4}$	5	8 $\frac{3}{4}$	17	11 $\frac{3}{4}$
1	7 $\frac{7}{8}$	14	7 $\frac{1}{8}$	5	0 $\frac{1}{2}$	15	9 $\frac{1}{2}$	5	5	16	12	5	9	18	0
1	8	14	7 $\frac{1}{2}$	5	0 $\frac{3}{4}$	15	9 $\frac{3}{4}$	5	5 $\frac{1}{4}$	16	13	5	9 $\frac{1}{4}$	18	0 $\frac{1}{4}$

9 _上	18	2 _上	6	2	19	4 _上	6	6 _上	20	5 _上
9 _中	18	3					6	6 _中	20	6 _上
9 _下	18	3 _中	6	2 _上	19	4 _中	6	6 _中	20	6 _中
10	18	3 _下	6	2 _中	19	5 _上	6	6 _中	20	7
			6	2 _下	19	5 _中	6	6 _中	20	7 _上
10 _上	18	4 _上	6	2 _上	19	6	6	6 _中	20	7 _中
10 _中	18	4 _中	6	2 _中	19	6 _上	6	6 _中	20	7 _中
10 _下	18	5	6	2 _中	19	6 _中	6	7	20	8 _上
10 _上	18	5 _上	6	2 _中	19	7 _上				
10 _中	18	5 _中	6	3	19	7 _中	6	7 _上	20	8 _上
10 _下	18	6 _上	6				6	7 _中	20	8 _中
10 _上	18	6 _中	6	3 _上	19	8	6	7 _中	20	9 _上
11	18	7	6	3 _中	19	8 _上	6	7 _中	20	9 _中
			6	3 _下	19	8 _中	6	7 _中	20	10 _上
11 _上	18	7 _上	6	3 _上	19	9 _上	6	7 _中	20	10 _中
11 _中	18	7 _中	6	3 _中	19	9 _中	6	7 _中	20	10 _中
11 _下	18	8 _上	6	3 _中	19	9 _中	6	8	20	11 _上
11 _上	18	8 _中	6	3 _中	19	10 _上				
11 _中	18	8 _中	6	3 _中	19	10 _中	6	8 _上	20	11 _中
11 _下	18	9 _上	6	4	19	10 _中	6	8 _中	21	0
11 _上	18	9 _中					6	8 _中	21	0 _上
11 _中	18	9 _中	6	4 _上	-19	11 _上	6	8 _中	21	0 _中
0	18	10 _上	6	4 _中	19	11 _中	6	8 _中	21	1 _上
			6	4 _中	20	0 _上	6	8 _中	21	1 _中
0 _上	18	10 _中	6	4 _中	20	0 _中	6	8 _中	21	2
0 _中	18	11 _上	6	4 _中	20	1	6	9	21	2 _上
0 _下	18	11 _中	6	4 _中	20	1 _上				

CIRCLES ADVANCING BY AN EIGHTH.

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
7	2 $\frac{1}{2}$	22	7 $\frac{1}{2}$	7	6 $\frac{1}{2}$	23	9 $\frac{1}{2}$	7	11 $\frac{1}{2}$	24	10 $\frac{1}{2}$	8	3 $\frac{1}{2}$	26	0
7	2 $\frac{3}{4}$	22	8 $\frac{1}{4}$	7	7	23	9 $\frac{3}{4}$	7	11 $\frac{1}{4}$	24	11 $\frac{1}{4}$	8	3 $\frac{3}{4}$	26	0
7	2 $\frac{1}{2}$	22	8 $\frac{1}{2}$					7	11 $\frac{3}{4}$	24	11 $\frac{3}{4}$	8	3 $\frac{1}{2}$	26	1
7	2 $\frac{3}{4}$	22	8 $\frac{3}{4}$					7	11 $\frac{1}{2}$	25	0	8	3 $\frac{3}{4}$	26	1
7	3	22	9 $\frac{1}{4}$					7	11 $\frac{3}{4}$	25	0 $\frac{1}{2}$	8	4	26	2
				7	7 $\frac{1}{2}$	23	10 $\frac{1}{2}$	7	11 $\frac{1}{2}$	25	0 $\frac{1}{2}$				
7	3 $\frac{1}{4}$	22	9 $\frac{3}{4}$	7	7 $\frac{3}{4}$	23	11 $\frac{1}{2}$	7	11 $\frac{3}{4}$	25	1 $\frac{1}{2}$	8	4 $\frac{1}{4}$	26	2
7	3 $\frac{1}{2}$	22	10	7	7 $\frac{1}{2}$	23	11 $\frac{3}{4}$	8	0	25	1 $\frac{1}{2}$	8	4 $\frac{1}{2}$	26	2
7	3 $\frac{3}{4}$	22	10 $\frac{1}{4}$	7	7 $\frac{3}{4}$	24	0 $\frac{1}{2}$					8	4 $\frac{3}{4}$	26	3
7	3 $\frac{1}{2}$	22	10 $\frac{1}{2}$	7	7 $\frac{1}{2}$	24	0 $\frac{3}{4}$	8	0 $\frac{1}{2}$	25	2 $\frac{1}{2}$	8	4 $\frac{1}{2}$	26	3
7	3 $\frac{3}{4}$	22	11 $\frac{1}{4}$	7	7 $\frac{3}{4}$	24	0 $\frac{1}{2}$	8	0 $\frac{3}{4}$	25	2 $\frac{3}{4}$	8	4 $\frac{3}{4}$	26	4
7	3 $\frac{1}{2}$	22	11 $\frac{1}{2}$	7	8	24	1	8	0 $\frac{1}{2}$	25	3 $\frac{1}{4}$	8	4 $\frac{1}{2}$	26	4
7	3 $\frac{3}{4}$	22	11 $\frac{3}{4}$					8	0 $\frac{3}{4}$	25	3 $\frac{1}{2}$	8	4 $\frac{3}{4}$	26	4
7	3 $\frac{1}{2}$	23	0					8	0 $\frac{1}{2}$	25	3 $\frac{3}{4}$	8	4 $\frac{1}{2}$	26	4
7	4	23	0 $\frac{1}{2}$	7	8 $\frac{1}{4}$	24	1 $\frac{1}{4}$	8	0 $\frac{3}{4}$	25	4 $\frac{1}{4}$	8	5	26	5
				7	8 $\frac{1}{2}$	24	1 $\frac{1}{2}$	8	0 $\frac{1}{2}$	25	4 $\frac{1}{2}$				
7	4 $\frac{1}{4}$	23	0 $\frac{3}{4}$	7	8 $\frac{3}{4}$	24	2 $\frac{1}{4}$	8	0 $\frac{3}{4}$	25	4 $\frac{3}{4}$	8	5 $\frac{1}{4}$	26	5
7	4 $\frac{1}{2}$	23	1 $\frac{1}{4}$	7	8 $\frac{1}{2}$	24	2 $\frac{1}{2}$	8	0 $\frac{1}{2}$	25	5 $\frac{1}{4}$	8	5 $\frac{1}{2}$	26	6
7	4 $\frac{3}{4}$	23	1 $\frac{1}{2}$	7	8 $\frac{3}{4}$	24	2 $\frac{3}{4}$	8	1	25	5 $\frac{1}{2}$	8	5 $\frac{3}{4}$	26	6
7	4 $\frac{1}{2}$	23	2	7	8 $\frac{1}{2}$	24	3 $\frac{1}{4}$	8	1 $\frac{1}{4}$	25	5 $\frac{3}{4}$	8	5 $\frac{1}{2}$	26	6
7	4 $\frac{3}{4}$	23	2 $\frac{1}{4}$	7	8 $\frac{3}{4}$	24	3 $\frac{1}{2}$	8	1 $\frac{1}{2}$	25	6 $\frac{1}{4}$	8	5 $\frac{3}{4}$	26	7
7	4 $\frac{1}{2}$	23	2 $\frac{1}{2}$	7	8 $\frac{1}{2}$	24	3 $\frac{3}{4}$	8	1 $\frac{3}{4}$	25	6 $\frac{1}{2}$	8	5 $\frac{1}{2}$	26	7
7	4 $\frac{3}{4}$	23	2 $\frac{3}{4}$	7	9	24	4 $\frac{1}{4}$	8	1 $\frac{1}{2}$	25	6 $\frac{3}{4}$	8	5 $\frac{3}{4}$	26	8
7	4 $\frac{1}{2}$	23	3 $\frac{1}{4}$					8	1 $\frac{3}{4}$	25	7 $\frac{1}{4}$	8	6	26	8
7	4 $\frac{3}{4}$	23	3 $\frac{1}{2}$	7	9 $\frac{1}{4}$	24	4 $\frac{1}{2}$	8	1 $\frac{1}{2}$	25	7 $\frac{1}{2}$				
7	5	23	3 $\frac{3}{4}$	7	9 $\frac{1}{2}$	24	5 $\frac{1}{4}$	8	1 $\frac{3}{4}$	25	8 $\frac{1}{4}$	8	6 $\frac{1}{4}$	26	9
				7	9 $\frac{3}{4}$	24	5 $\frac{1}{2}$	8	2	25	8 $\frac{1}{2}$	8	6 $\frac{1}{2}$	26	9
7	5 $\frac{1}{4}$	23	3 $\frac{1}{2}$	7	9 $\frac{1}{2}$	24	6 $\frac{1}{4}$					8	6 $\frac{3}{4}$	26	10
7	5 $\frac{1}{2}$	23	4 $\frac{1}{4}$	7	9 $\frac{3}{4}$	24	6 $\frac{1}{2}$	8	2 $\frac{1}{2}$	25	8 $\frac{3}{4}$	8	6 $\frac{1}{2}$	26	10
7	5 $\frac{3}{4}$	23	4 $\frac{1}{2}$	7	9 $\frac{1}{2}$	24	6 $\frac{3}{4}$	8	2 $\frac{1}{2}$	25	9 $\frac{1}{4}$	8	6 $\frac{3}{4}$	26	11
7	5 $\frac{1}{2}$	23	5 $\frac{1}{4}$	7	9 $\frac{3}{4}$	24	6 $\frac{1}{2}$	8	2 $\frac{3}{4}$	25	10 $\frac{1}{4}$	8	6 $\frac{1}{2}$	26	11
7	5 $\frac{3}{4}$	23	5 $\frac{1}{2}$	7	9 $\frac{1}{2}$	24	6 $\frac{3}{4}$	8	2 $\frac{1}{2}$	25	10 $\frac{1}{2}$				
7	5 $\frac{1}{2}$	23	5 $\frac{3}{4}$	7	10	24	7 $\frac{1}{4}$	8	2 $\frac{3}{4}$	25	11 $\frac{1}{4}$	8	7 $\frac{1}{4}$	26	11
7	5 $\frac{3}{4}$	23	6 $\frac{1}{4}$					8	2 $\frac{1}{2}$	25	11 $\frac{1}{2}$	8	7 $\frac{1}{2}$	27	0
7	5 $\frac{1}{2}$	23	6 $\frac{1}{2}$	7	10 $\frac{1}{4}$	24	7 $\frac{1}{2}$	8	2 $\frac{3}{4}$	25	11 $\frac{3}{4}$	8	7 $\frac{3}{4}$	27	0
				7	10 $\frac{1}{2}$	24	8 $\frac{1}{4}$	8	2 $\frac{1}{2}$	25	12 $\frac{1}{4}$	8	7 $\frac{1}{2}$	27	0
7	6 $\frac{1}{4}$	23	7 $\frac{1}{4}$	7	10 $\frac{1}{2}$	24	8 $\frac{1}{2}$	8	2 $\frac{3}{4}$	25	12 $\frac{1}{2}$	8	7 $\frac{3}{4}$	27	0
7	6 $\frac{1}{2}$	23	7 $\frac{1}{2}$	7	10 $\frac{1}{4}$	24	8 $\frac{3}{4}$	8	2 $\frac{1}{2}$	25	12 $\frac{3}{4}$	8	7 $\frac{1}{2}$	27	0
7	6 $\frac{3}{4}$	23	7 $\frac{3}{4}$	7	10 $\frac{1}{2}$	24	9 $\frac{1}{4}$	8	3	25	13 $\frac{1}{4}$	8	7 $\frac{3}{4}$	27	0
7	6 $\frac{1}{2}$	23	8 $\frac{1}{4}$	7	10 $\frac{3}{4}$	24	9 $\frac{1}{2}$					8	7 $\frac{1}{2}$	27	0
7	6 $\frac{3}{4}$	23	8 $\frac{1}{2}$	7	10 $\frac{1}{2}$	24	9 $\frac{3}{4}$	8	3 $\frac{1}{4}$	25	13 $\frac{1}{2}$	8	7 $\frac{3}{4}$	27	1
7	6 $\frac{1}{2}$	23	8 $\frac{3}{4}$	7	10 $\frac{3}{4}$	24	10	8	3 $\frac{1}{2}$	25	14 $\frac{1}{4}$	8	7 $\frac{1}{2}$	27	1
7	6 $\frac{3}{4}$	23	9 $\frac{1}{4}$	7	11	24	10 $\frac{1}{2}$	8	3 $\frac{3}{4}$	26	0 $\frac{1}{2}$	8	7 $\frac{3}{4}$	27	1

27	3 $\frac{1}{2}$	9	0 $\frac{1}{2}$	28	5 $\frac{1}{2}$	9	5	29	1	9	
27	3 $\frac{3}{4}$	9	0 $\frac{3}{4}$	28	5 $\frac{3}{4}$	9	5 $\frac{1}{2}$	29	7 $\frac{1}{2}$	9	
27	4 $\frac{1}{2}$	9	0 $\frac{1}{2}$	28	6	9	5 $\frac{3}{4}$	29	7 $\frac{3}{4}$	9	
27	4 $\frac{3}{4}$	9	1	28	6 $\frac{1}{2}$	9	5 $\frac{1}{2}$	29	8 $\frac{1}{2}$	9	
27	5					9	5 $\frac{1}{2}$	29	8 $\frac{3}{4}$	9	
27	5 $\frac{1}{2}$	9	1 $\frac{1}{2}$	28	6 $\frac{3}{4}$	9	5 $\frac{3}{4}$	29	8 $\frac{1}{2}$	9	
27	5 $\frac{3}{4}$	9	1 $\frac{3}{4}$	28	7 $\frac{1}{2}$	9	5 $\frac{1}{2}$	29	8 $\frac{3}{4}$	9	1
27	5 $\frac{1}{2}$	9	1 $\frac{1}{2}$	28	7 $\frac{3}{4}$	9	5 $\frac{3}{4}$	29	9 $\frac{1}{2}$	9	
		9	1 $\frac{3}{4}$	28	8	9	5 $\frac{1}{2}$	29	9 $\frac{3}{4}$	9	
27	6 $\frac{1}{2}$	9	1 $\frac{1}{2}$	28	8 $\frac{1}{2}$	9	6	29	10 $\frac{1}{2}$	9	1
27	6 $\frac{3}{4}$	9	1 $\frac{3}{4}$	28	8 $\frac{3}{4}$					9	1
27	7	9	1 $\frac{1}{2}$	28	8 $\frac{1}{2}$					9	1
27	7 $\frac{1}{2}$	9	1 $\frac{3}{4}$	28	9 $\frac{1}{2}$	9	6 $\frac{1}{2}$	29	10 $\frac{1}{2}$	9	1
27	7 $\frac{3}{4}$	9	2	28	9 $\frac{3}{4}$	9	6 $\frac{3}{4}$	29	10 $\frac{3}{4}$	9	1
27	8 $\frac{1}{2}$					9	6 $\frac{1}{2}$	29	11 $\frac{1}{2}$	9	1
27	8 $\frac{3}{4}$	9	2 $\frac{1}{2}$	28	9 $\frac{1}{2}$	9	6 $\frac{3}{4}$	29	11 $\frac{3}{4}$	9	1
27	8 $\frac{1}{2}$	9	2 $\frac{3}{4}$	28	10 $\frac{1}{2}$	9	6 $\frac{1}{2}$	30	0	9	1
27	9	9	2 $\frac{1}{2}$	28	10 $\frac{3}{4}$	9	6 $\frac{3}{4}$	30	0 $\frac{1}{2}$	9	1
		9	2 $\frac{3}{4}$	28	11 $\frac{1}{2}$	9	6 $\frac{1}{2}$	30	0 $\frac{3}{4}$	9	
27	9 $\frac{1}{2}$	9	2 $\frac{1}{2}$	28	11 $\frac{3}{4}$	9	7	30	1 $\frac{1}{2}$	9	
27	9 $\frac{3}{4}$	9	2 $\frac{3}{4}$	28	11 $\frac{1}{2}$					9	
27	10 $\frac{1}{2}$	9	2 $\frac{1}{2}$	29	0 $\frac{1}{2}$	9	7 $\frac{1}{2}$	30	1 $\frac{1}{2}$	9	
27	10 $\frac{3}{4}$	9	3	29	0 $\frac{3}{4}$	9	7 $\frac{3}{4}$	30	2	9	
27	10 $\frac{1}{2}$					9	7 $\frac{1}{2}$	30	2 $\frac{1}{2}$	9	
27	11 $\frac{1}{2}$	9	3 $\frac{1}{2}$	29	1	9	7 $\frac{3}{4}$	30	2 $\frac{3}{4}$	9	
27	11 $\frac{3}{4}$	9	3 $\frac{3}{4}$	29	1 $\frac{1}{2}$	9	7 $\frac{1}{2}$	30	3 $\frac{1}{2}$	9	
28	0 $\frac{1}{2}$	9	3 $\frac{1}{2}$	29	1 $\frac{3}{4}$	9	7 $\frac{3}{4}$	30	3 $\frac{3}{4}$	10	
		9	3 $\frac{3}{4}$	29	2 $\frac{1}{2}$	9	7 $\frac{1}{2}$	30	4		

n.	Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
1 $\frac{1}{8}$	31	8 $\frac{1}{2}$	10	5 $\frac{1}{2}$	32	10 $\frac{1}{4}$	10	9 $\frac{7}{8}$	34	0	11	2 $\frac{1}{2}$	35	1 $\frac{1}{2}$				
1 $\frac{1}{4}$	31	8 $\frac{1}{2}$	10	5 $\frac{1}{2}$	32	10 $\frac{1}{2}$	10	10	34	0 $\frac{1}{8}$	11	2 $\frac{1}{2}$	35	1 $\frac{1}{2}$				
1 $\frac{3}{8}$	31	9 $\frac{1}{4}$	10	5 $\frac{3}{4}$	32	11					11	2 $\frac{3}{4}$	35	2 $\frac{1}{2}$				
1 $\frac{1}{2}$	31	9 $\frac{1}{2}$	10	5 $\frac{3}{4}$	32	11 $\frac{1}{2}$			10	10 $\frac{1}{8}$	34	0 $\frac{1}{4}$	11	2 $\frac{3}{4}$	35	2 $\frac{1}{2}$		
1 $\frac{5}{8}$	31	10	10	6	32	11 $\frac{3}{4}$			10	10 $\frac{1}{4}$	34	1 $\frac{1}{4}$	11	2 $\frac{3}{4}$	35	2 $\frac{1}{2}$		
1 $\frac{3}{4}$	31	10 $\frac{1}{2}$							10	10 $\frac{3}{8}$	34	1 $\frac{1}{2}$	11	2 $\frac{3}{4}$	35	3 $\frac{1}{4}$		
1 $\frac{7}{8}$	31	10 $\frac{3}{4}$							10	10 $\frac{1}{2}$	34	1 $\frac{3}{4}$	11	2 $\frac{3}{4}$	35	3 $\frac{1}{2}$		
2	31	11 $\frac{1}{4}$							10	10 $\frac{3}{4}$	34	2 $\frac{1}{4}$	11	3	35	4		
			10	6 $\frac{1}{8}$	33	0 $\frac{1}{8}$			10	10 $\frac{5}{8}$	34	2 $\frac{3}{8}$						
			10	6 $\frac{1}{4}$	33	0 $\frac{1}{4}$			10	10 $\frac{3}{4}$	34	2 $\frac{1}{2}$						
			10	6 $\frac{3}{8}$	33	1			10	10 $\frac{7}{8}$	34	2 $\frac{7}{8}$						
			10	6 $\frac{1}{2}$	33	1 $\frac{1}{8}$			10	10 $\frac{1}{2}$	34	3 $\frac{1}{8}$	11	3 $\frac{1}{8}$	35	4 $\frac{1}{2}$		
2 $\frac{1}{8}$	31	11 $\frac{3}{8}$	10	6 $\frac{1}{2}$	33	1 $\frac{1}{4}$			10	11	34	3 $\frac{1}{4}$	11	3 $\frac{1}{4}$	35	4 $\frac{1}{4}$		
2 $\frac{1}{4}$	32	0	10	6 $\frac{3}{8}$	33	2 $\frac{1}{8}$							11	3 $\frac{1}{4}$	35	5 $\frac{1}{4}$		
2 $\frac{1}{2}$	32	0 $\frac{1}{8}$	10	6 $\frac{3}{4}$	33	2 $\frac{1}{4}$							11	3 $\frac{1}{2}$	35	5 $\frac{1}{2}$		
2 $\frac{3}{8}$	32	0 $\frac{1}{4}$	10	6 $\frac{3}{4}$	33	2 $\frac{1}{2}$			10	11 $\frac{1}{8}$	34	3 $\frac{7}{8}$	11	3 $\frac{1}{2}$	35	5 $\frac{1}{2}$		
2 $\frac{1}{2}$	32	1 $\frac{1}{8}$	10	7	33	2 $\frac{3}{8}$			10	11 $\frac{1}{4}$	34	4 $\frac{1}{4}$	11	3 $\frac{1}{2}$	35	6		
2 $\frac{5}{8}$	32	1 $\frac{1}{4}$							10	11 $\frac{3}{8}$	34	4 $\frac{1}{2}$	11	3 $\frac{3}{4}$	35	6 $\frac{1}{4}$		
2 $\frac{3}{4}$	32	1 $\frac{1}{2}$							10	11 $\frac{1}{2}$	34	5	11	3 $\frac{3}{4}$	35	6 $\frac{1}{2}$		
2 $\frac{7}{8}$	32	2							10	11 $\frac{3}{4}$	34	5 $\frac{1}{4}$	11	3 $\frac{3}{4}$	35	6 $\frac{3}{4}$		
3	32	2 $\frac{1}{8}$	10	7 $\frac{1}{8}$	33	3 $\frac{1}{8}$			10	11 $\frac{1}{2}$	34	5 $\frac{1}{2}$	11	4	35	7 $\frac{1}{4}$		
			10	7 $\frac{1}{4}$	33	3 $\frac{1}{4}$			10	11 $\frac{3}{4}$	34	5 $\frac{3}{4}$						
			10	7 $\frac{3}{8}$	33	4 $\frac{1}{8}$			10	11 $\frac{1}{2}$	34	5 $\frac{1}{2}$						
			10	7 $\frac{1}{2}$	33	4 $\frac{1}{4}$			10	11 $\frac{3}{4}$	34	5 $\frac{3}{4}$	11	4 $\frac{1}{4}$	35	7 $\frac{1}{8}$		
3 $\frac{1}{8}$	32	2 $\frac{3}{8}$	10	7 $\frac{1}{2}$	33	4 $\frac{1}{2}$			10	11 $\frac{1}{2}$	34	6 $\frac{1}{4}$	11	4 $\frac{1}{4}$	35	8		
3 $\frac{1}{4}$	32	3 $\frac{1}{4}$	10	7 $\frac{3}{8}$	33	4 $\frac{3}{4}$			11	0	34	6 $\frac{1}{2}$	11	4 $\frac{1}{4}$	35	8 $\frac{1}{4}$		
3 $\frac{1}{2}$	32	3 $\frac{1}{2}$	10	7 $\frac{3}{4}$	33	5 $\frac{1}{4}$							11	4 $\frac{1}{2}$	35	8 $\frac{1}{2}$		
3 $\frac{3}{8}$	32	3 $\frac{3}{8}$	10	7 $\frac{3}{4}$	33	5 $\frac{3}{8}$			11	0 $\frac{1}{8}$	34	7 $\frac{1}{8}$	11	4 $\frac{1}{2}$	35	9 $\frac{1}{8}$		
3 $\frac{1}{2}$	32	4 $\frac{1}{8}$	10	8	33	6 $\frac{1}{8}$			11	0 $\frac{1}{4}$	34	7 $\frac{1}{4}$	11	4 $\frac{1}{2}$	35	9 $\frac{1}{4}$		
3 $\frac{5}{8}$	32	4 $\frac{1}{4}$							11	0 $\frac{3}{8}$	34	7 $\frac{3}{8}$	11	4 $\frac{3}{4}$	35	9 $\frac{3}{4}$		
3 $\frac{3}{4}$	32	4 $\frac{3}{4}$							11	0 $\frac{1}{2}$	34	8 $\frac{1}{4}$	11	4 $\frac{3}{4}$	35	10		
3 $\frac{7}{8}$	32	5 $\frac{1}{8}$	10	8 $\frac{1}{8}$	33	6 $\frac{1}{4}$			11	0 $\frac{3}{4}$	34	8 $\frac{3}{4}$	11	5	35	10 $\frac{1}{4}$		
4	32	5 $\frac{1}{4}$	10	8 $\frac{1}{4}$	33	6 $\frac{3}{4}$			11	0 $\frac{1}{2}$	34	8 $\frac{1}{2}$	11	5	35	10 $\frac{1}{2}$		
			10	8 $\frac{3}{8}$	33	7 $\frac{1}{8}$			11	0 $\frac{3}{4}$	34	9						
			10	8 $\frac{1}{2}$	33	7 $\frac{1}{4}$			11	0 $\frac{1}{2}$	34	9						
			10	8 $\frac{3}{4}$	33	8			11	0 $\frac{3}{4}$	34	9 $\frac{1}{4}$	11	5 $\frac{1}{4}$	35	10 $\frac{3}{4}$		
4 $\frac{1}{8}$	32	5 $\frac{7}{8}$	10	8 $\frac{3}{4}$	33	8 $\frac{1}{8}$			11	0 $\frac{1}{2}$	34	9 $\frac{1}{2}$	11	5 $\frac{1}{4}$	35	11 $\frac{1}{4}$		
4 $\frac{1}{4}$	32	6 $\frac{1}{4}$	10	8 $\frac{3}{4}$	33	8 $\frac{1}{4}$			11	0 $\frac{3}{4}$	34	9 $\frac{3}{4}$	11	5 $\frac{1}{2}$	35	11 $\frac{1}{2}$		
4 $\frac{1}{2}$	32	6 $\frac{1}{2}$	10	8 $\frac{3}{4}$	33	8 $\frac{3}{8}$			11	1	34	9 $\frac{3}{4}$	11	5 $\frac{1}{2}$	35	11 $\frac{1}{2}$		
4 $\frac{3}{8}$	32	7	10	8 $\frac{7}{8}$	33	8 $\frac{7}{8}$							11	5 $\frac{3}{4}$	35	11 $\frac{3}{4}$		
4 $\frac{1}{2}$	32	7 $\frac{1}{4}$	10	9	33	9 $\frac{1}{4}$			11	1 $\frac{1}{8}$	34	10 $\frac{1}{8}$	11	5 $\frac{3}{4}$	35	11 $\frac{3}{4}$		
4 $\frac{5}{8}$	32	7 $\frac{3}{8}$							11	1 $\frac{1}{4}$	34	10 $\frac{1}{4}$	11	5 $\frac{3}{4}$	35	11 $\frac{3}{4}$		
4 $\frac{3}{4}$	32	7 $\frac{1}{2}$							11	1 $\frac{3}{8}$	34	11	11	5 $\frac{3}{4}$	35	11 $\frac{3}{4}$		
4 $\frac{7}{8}$	32	8 $\frac{1}{8}$	10	9 $\frac{1}{8}$	33	9 $\frac{5}{8}$			11	1 $\frac{1}{2}$	34	11 $\frac{1}{2}$	11	5 $\frac{3}{4}$	35	11 $\frac{3}{4}$		
5	32	8 $\frac{1}{4}$	10	9 $\frac{1}{4}$	33	10			11	1 $\frac{1}{2}$	34	11 $\frac{1}{2}$	11	6	35	12		
			10	9 $\frac{3}{8}$	33	10 $\frac{3}{8}$			11	1 $\frac{3}{4}$	34	11 $\frac{3}{4}$						
			10	9 $\frac{1}{2}$	33	10 $\frac{1}{2}$			11	1 $\frac{3}{4}$	34	11 $\frac{3}{4}$						
5 $\frac{1}{8}$	32	9	10	9 $\frac{1}{2}$	33	10 $\frac{3}{4}$			11	1 $\frac{3}{4}$	34	11 $\frac{3}{4}$						
5 $\frac{1}{4}$	32	9 $\frac{1}{4}$	10	9 $\frac{1}{2}$	33	11 $\frac{1}{4}$			11	1 $\frac{3}{4}$	34	11 $\frac{3}{4}$						
5 $\frac{1}{2}$	32	9 $\frac{1}{2}$	10	9 $\frac{3}{4}$	33	11 $\frac{1}{2}$			11	2	34	12						

36	4	11	11	37	6	12	3	38	7	12
36	5	11	11	37	6	12	3	38	8	12
36	5	11	11	37	6	12	3	38	8	12
36	5	11	11	37	7	12	4	38	8	12
36	6	11	11	37	7	12	4	38	9	12
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36	7	12	0	37	8	12	4	38	10	12
36	7	12	0	37	8	12	4	38	10	12
36	7	12	0	37	9	12	4	38	10	12
36	7	12	0	37	9	12	4	38	11	12
36	8	12	0	37	9	12	4	38	11	12
36	8	12	0	37	10	12	5	39	0	12
36	9	12	0	37	10	12	5	39	0	12
36	9	12	0	37	11	12	5	39	1	12
36	9	12	0	37	11	12	5	39	1	12
36	10	12	1	37	11	12	5	39	2	12
36	10	12	1	37	11	12	5	39	2	12
36	10	12	1	38	0	12	5	39	2	12
36	11	12	1	38	0	12	5	39	2	12
36	11	12	1	38	1	12	6	39	3	12
37	0	12	1	38	1	12	6	39	3	12
37	0	12	1	38	1	12	6	39	4	12
37	0	12	1	38	2	12	6	39	4	12
37	0	12	1	38	2	12	6	39	4	12
37	1	12	2	38	2	12	6	39	4	12
37	1	12	2	38	2	12	6	39	4	12

CIRCLES ADVANCING BY AN EIGHTH.

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
12	11 $\frac{1}{2}$	40	9 $\frac{1}{2}$	13	4 $\frac{1}{2}$	41	11	13	8 $\frac{1}{2}$	43	0 $\frac{1}{2}$	14	0 $\frac{1}{2}$	44	
13	0	40	10	13	4 $\frac{1}{2}$	41	11 $\frac{1}{2}$	13	8 $\frac{1}{2}$	43	1 $\frac{1}{2}$	14	1	44	
				13	4 $\frac{1}{2}$	41	11 $\frac{1}{2}$	13	8 $\frac{1}{2}$	43	1 $\frac{1}{2}$				
13	0 $\frac{1}{2}$	40	10 $\frac{1}{2}$	13	4 $\frac{1}{2}$	42	0 $\frac{1}{2}$	13	8 $\frac{1}{2}$	43	1 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	40	10 $\frac{1}{2}$	13	4 $\frac{1}{2}$	42	0 $\frac{1}{2}$	13	9	43	2 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	40	11 $\frac{1}{2}$	13	4 $\frac{1}{2}$	42	1	13	9 $\frac{1}{2}$	43	2 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	40	11 $\frac{1}{2}$	13	4 $\frac{1}{2}$	42	1 $\frac{1}{2}$	13	9 $\frac{1}{2}$	43	3 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	41	0	13	4 $\frac{1}{2}$	42	1 $\frac{1}{2}$	13	9 $\frac{1}{2}$	43	3 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	41	0 $\frac{1}{2}$					13	9 $\frac{1}{2}$	43	3 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	0 $\frac{1}{2}$	41	0 $\frac{1}{2}$					13	9 $\frac{1}{2}$	43	3 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
13	1	41	1 $\frac{1}{2}$					13	9 $\frac{1}{2}$	43	4 $\frac{1}{2}$	14	1 $\frac{1}{2}$	44	
				13	5 $\frac{1}{2}$	42	2 $\frac{1}{2}$	13	9 $\frac{1}{2}$	43	4 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	1 $\frac{1}{2}$	13	5 $\frac{1}{2}$	42	2 $\frac{1}{2}$	13	9 $\frac{1}{2}$	43	5	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	2	13	5 $\frac{1}{2}$	42	3 $\frac{1}{2}$	13	10	43	5 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	2 $\frac{1}{2}$	13	5 $\frac{1}{2}$	42	4 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	6 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	2 $\frac{1}{2}$	13	5 $\frac{1}{2}$	42	4 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	6 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6	42	4 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	6 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$					13	10 $\frac{1}{2}$	43	7 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	5 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	7 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	5 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	7 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	6	13	10 $\frac{1}{2}$	43	7 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	6 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	6 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	2 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
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13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
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13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	14	3 $\frac{1}{2}$	44	
13	1 $\frac{1}{2}$	41	3 $\frac{1}{2}$	13	6 $\frac{1}{2}$	42	7 $\frac{1}{2}$	13	10 $\frac{1}{2}$	43	8 $\frac{1}{2}$	1			

6 $\frac{3}{4}$	36	3 $\frac{3}{4}$			12	3 $\frac{1}{4}$	38	7 $\frac{3}{4}$	12
6 $\frac{1}{2}$	36	4 $\frac{1}{4}$	11	11 $\frac{1}{4}$	37	3 $\frac{1}{2}$	38	7 $\frac{1}{2}$	12
7	36	4 $\frac{3}{4}$	11	11 $\frac{1}{2}$	37	3 $\frac{3}{4}$	38	8 $\frac{1}{4}$	12
			11	11 $\frac{3}{4}$	37	4	38	8 $\frac{3}{4}$	12
7 $\frac{1}{4}$	36	5	11	11 $\frac{1}{4}$	37	4 $\frac{1}{4}$	38	9 $\frac{1}{4}$	12
7 $\frac{1}{2}$	36	5 $\frac{1}{4}$	11	11 $\frac{1}{2}$	37	4 $\frac{1}{2}$	38	9 $\frac{1}{2}$	12
7 $\frac{3}{4}$	36	5 $\frac{3}{4}$	11	11 $\frac{3}{4}$	37	4 $\frac{3}{4}$	38	10 $\frac{1}{4}$	12
7 $\frac{1}{2}$	36	6 $\frac{1}{4}$	11	11 $\frac{1}{2}$	37	5	39	0	12
7 $\frac{3}{4}$	36	6 $\frac{3}{4}$	12	0	37	5 $\frac{1}{4}$	39	0 $\frac{1}{4}$	12
7 $\frac{1}{2}$	36	7	12	0 $\frac{1}{4}$	37	5 $\frac{1}{2}$	39	0 $\frac{1}{2}$	12
7 $\frac{3}{4}$	36	7 $\frac{1}{4}$	12	0 $\frac{1}{2}$	37	5 $\frac{3}{4}$	39	1 $\frac{1}{4}$	12
8	36	7 $\frac{3}{4}$	12	0 $\frac{3}{4}$	37	6	39	1 $\frac{1}{2}$	12
		7 $\frac{1}{2}$	12	0 $\frac{1}{4}$	37	6 $\frac{1}{4}$	39	3 $\frac{1}{4}$	12
		7 $\frac{3}{4}$	12	0 $\frac{1}{2}$	37	6 $\frac{1}{2}$	39	4	12
		7 $\frac{1}{2}$	12	0 $\frac{3}{4}$	37	6 $\frac{3}{4}$	39	4 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	8 $\frac{1}{4}$	12	0 $\frac{1}{4}$	37	6 $\frac{1}{4}$	39	4 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	8 $\frac{1}{2}$	12	0 $\frac{1}{2}$	37	6 $\frac{1}{2}$	39	4 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	9	12	0 $\frac{3}{4}$	37	6 $\frac{3}{4}$	39	4 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	9 $\frac{1}{4}$	12	0 $\frac{1}{4}$	37	7	39	5	12
8 $\frac{1}{2}$	36	9 $\frac{1}{2}$	12	0 $\frac{1}{2}$	37	7 $\frac{1}{4}$	39	5 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	9 $\frac{3}{4}$	12	0 $\frac{3}{4}$	37	7 $\frac{1}{2}$	39	5 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	9 $\frac{1}{4}$	12	1	37	7 $\frac{3}{4}$	39	5 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	10 $\frac{1}{4}$	12	1 $\frac{1}{4}$	37	8	39	6	12
8 $\frac{3}{4}$	36	10 $\frac{1}{2}$	12	1 $\frac{1}{2}$	37	8 $\frac{1}{4}$	39	6 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	10 $\frac{3}{4}$	12	1 $\frac{3}{4}$	37	8 $\frac{1}{2}$	39	6 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	11 $\frac{1}{4}$	12	1 $\frac{1}{4}$	37	8 $\frac{3}{4}$	39	6 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	11 $\frac{1}{2}$	12	1 $\frac{1}{2}$	37	9	39	7	12
8 $\frac{1}{4}$	36	11 $\frac{3}{4}$	12	1 $\frac{3}{4}$	37	9 $\frac{1}{4}$	39	7 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	12	12	2	37	9 $\frac{1}{2}$	39	7 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	12 $\frac{1}{4}$	12	2 $\frac{1}{4}$	37	9 $\frac{3}{4}$	39	7 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	12 $\frac{1}{2}$	12	2 $\frac{1}{2}$	37	10	39	8	12
8 $\frac{1}{2}$	36	12 $\frac{3}{4}$	12	3	37	10 $\frac{1}{4}$	39	8 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	13	12	3 $\frac{1}{4}$	37	10 $\frac{1}{2}$	39	8 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	13 $\frac{1}{4}$	12	3 $\frac{1}{2}$	37	10 $\frac{3}{4}$	39	8 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	13 $\frac{1}{2}$	12	3 $\frac{3}{4}$	37	11	39	9	12
8 $\frac{3}{4}$	36	13 $\frac{3}{4}$	12	4	37	11 $\frac{1}{4}$	39	9 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	14	12	4 $\frac{1}{4}$	37	11 $\frac{1}{2}$	39	9 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	14 $\frac{1}{4}$	12	4 $\frac{1}{2}$	37	11 $\frac{3}{4}$	39	9 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	14 $\frac{1}{2}$	12	4 $\frac{3}{4}$	37	12	39	10	12
8 $\frac{1}{4}$	36	14 $\frac{3}{4}$	12	5	37	12 $\frac{1}{4}$	39	10 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	15	12	5 $\frac{1}{4}$	37	12 $\frac{1}{2}$	39	10 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	15 $\frac{1}{4}$	12	5 $\frac{1}{2}$	37	12 $\frac{3}{4}$	39	10 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	15 $\frac{1}{2}$	12	5 $\frac{3}{4}$	37	13	39	11	12
8 $\frac{1}{2}$	36	16	12	6	37	13 $\frac{1}{4}$	39	11 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	16 $\frac{1}{4}$	12	6 $\frac{1}{4}$	37	13 $\frac{1}{2}$	39	11 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	16 $\frac{1}{2}$	12	6 $\frac{1}{2}$	37	13 $\frac{3}{4}$	39	11 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	16 $\frac{3}{4}$	12	6 $\frac{3}{4}$	37	14	39	12	12
8 $\frac{3}{4}$	36	17	12	7	37	14 $\frac{1}{4}$	39	12 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	17 $\frac{1}{4}$	12	7 $\frac{1}{4}$	37	14 $\frac{1}{2}$	39	12 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	17 $\frac{1}{2}$	12	7 $\frac{1}{2}$	37	14 $\frac{3}{4}$	39	12 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	17 $\frac{3}{4}$	12	7 $\frac{3}{4}$	37	15	39	13	12
8 $\frac{1}{4}$	36	18	12	8	37	15 $\frac{1}{4}$	39	13 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	18 $\frac{1}{4}$	12	8 $\frac{1}{4}$	37	15 $\frac{1}{2}$	39	13 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	18 $\frac{1}{2}$	12	8 $\frac{1}{2}$	37	15 $\frac{3}{4}$	39	13 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	18 $\frac{3}{4}$	12	8 $\frac{3}{4}$	37	16	39	14	12
8 $\frac{1}{2}$	36	19	12	9	37	16 $\frac{1}{4}$	39	14 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	19 $\frac{1}{4}$	12	9 $\frac{1}{4}$	37	16 $\frac{1}{2}$	39	14 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	19 $\frac{1}{2}$	12	9 $\frac{1}{2}$	37	16 $\frac{3}{4}$	39	14 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	19 $\frac{3}{4}$	12	9 $\frac{3}{4}$	37	17	39	15	12
8 $\frac{3}{4}$	36	20	12	10	37	17 $\frac{1}{4}$	39	15 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	20 $\frac{1}{4}$	12	10 $\frac{1}{4}$	37	17 $\frac{1}{2}$	39	15 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	20 $\frac{1}{2}$	12	10 $\frac{1}{2}$	37	17 $\frac{3}{4}$	39	15 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	20 $\frac{3}{4}$	12	10 $\frac{3}{4}$	37	18	39	16	12
8 $\frac{1}{4}$	36	21	12	11	37	18 $\frac{1}{4}$	39	16 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	21 $\frac{1}{4}$	12	11 $\frac{1}{4}$	37	18 $\frac{1}{2}$	39	16 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	21 $\frac{1}{2}$	12	11 $\frac{1}{2}$	37	18 $\frac{3}{4}$	39	16 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	21 $\frac{3}{4}$	12	11 $\frac{3}{4}$	37	19	39	17	12
8 $\frac{1}{2}$	36	22	12	12	37	19 $\frac{1}{4}$	39	17 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	22 $\frac{1}{4}$	12	12 $\frac{1}{4}$	37	19 $\frac{1}{2}$	39	17 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	22 $\frac{1}{2}$	12	12 $\frac{1}{2}$	37	19 $\frac{3}{4}$	39	17 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	22 $\frac{3}{4}$	12	12 $\frac{3}{4}$	37	20	39	18	12
8 $\frac{3}{4}$	36	23	12	13	37	20 $\frac{1}{4}$	39	18 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	23 $\frac{1}{4}$	12	13 $\frac{1}{4}$	37	20 $\frac{1}{2}$	39	18 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	23 $\frac{1}{2}$	12	13 $\frac{1}{2}$	37	20 $\frac{3}{4}$	39	18 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	23 $\frac{3}{4}$	12	13 $\frac{3}{4}$	37	21	39	19	12
8 $\frac{1}{4}$	36	24	12	14	37	21 $\frac{1}{4}$	39	19 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	24 $\frac{1}{4}$	12	14 $\frac{1}{4}$	37	21 $\frac{1}{2}$	39	19 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	24 $\frac{1}{2}$	12	14 $\frac{1}{2}$	37	21 $\frac{3}{4}$	39	19 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	24 $\frac{3}{4}$	12	14 $\frac{3}{4}$	37	22	39	20	12
8 $\frac{1}{2}$	36	25	12	15	37	22 $\frac{1}{4}$	39	20 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	25 $\frac{1}{4}$	12	15 $\frac{1}{4}$	37	22 $\frac{1}{2}$	39	20 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	25 $\frac{1}{2}$	12	15 $\frac{1}{2}$	37	22 $\frac{3}{4}$	39	20 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	25 $\frac{3}{4}$	12	15 $\frac{3}{4}$	37	23	39	21	12
8 $\frac{3}{4}$	36	26	12	16	37	23 $\frac{1}{4}$	39	21 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	26 $\frac{1}{4}$	12	16 $\frac{1}{4}$	37	23 $\frac{1}{2}$	39	21 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	26 $\frac{1}{2}$	12	16 $\frac{1}{2}$	37	23 $\frac{3}{4}$	39	21 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	26 $\frac{3}{4}$	12	16 $\frac{3}{4}$	37	24	39	22	12
8 $\frac{1}{4}$	36	27	12	17	37	24 $\frac{1}{4}$	39	22 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	27 $\frac{1}{4}$	12	17 $\frac{1}{4}$	37	24 $\frac{1}{2}$	39	22 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	27 $\frac{1}{2}$	12	17 $\frac{1}{2}$	37	24 $\frac{3}{4}$	39	22 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	27 $\frac{3}{4}$	12	17 $\frac{3}{4}$	37	25	39	23	12
8 $\frac{1}{2}$	36	28	12	18	37	25 $\frac{1}{4}$	39	23 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	28 $\frac{1}{4}$	12	18 $\frac{1}{4}$	37	25 $\frac{1}{2}$	39	23 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	28 $\frac{1}{2}$	12	18 $\frac{1}{2}$	37	25 $\frac{3}{4}$	39	23 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	28 $\frac{3}{4}$	12	18 $\frac{3}{4}$	37	26	39	24	12
8 $\frac{3}{4}$	36	29	12	19	37	26 $\frac{1}{4}$	39	24 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	29 $\frac{1}{4}$	12	19 $\frac{1}{4}$	37	26 $\frac{1}{2}$	39	24 $\frac{1}{2}$	12
8 $\frac{1}{2}$	36	29 $\frac{1}{2}$	12	19 $\frac{1}{2}$	37	26 $\frac{3}{4}$	39	24 $\frac{3}{4}$	12
8 $\frac{3}{4}$	36	29 $\frac{3}{4}$	12	19 $\frac{3}{4}$	37	27	39	25	12
8 $\frac{1}{4}$	36	30	12	20	37	27 $\frac{1}{4}$	39	25 $\frac{1}{4}$	12
8 $\frac{1}{2}$	36	30 $\frac{1}{4}$	12	20 $\frac{1}{4}$	37	27 $\frac{1}{2}$	39	25 $\frac{1}{2}$	12
8 $\frac{3}{4}$	36	30 $\frac{1}{2}$	12	20 $\frac{1}{2}$	37	27 $\frac{3}{4}$	39	25 $\frac{3}{4}$	12
8 $\frac{1}{4}$	36	30 $\frac{3}{4}$	12	20 $\frac{3}{4}$	37	28	39	26	12
8 $\frac{1}{2}$	36	31	12	21	37	28 $\frac{1}{4}$	39	26 $\frac{1}{4}$	12
8 $\frac{3}{4}$	36	31 $\frac{1}{4}$	12	21 $\frac{1}{4}$	37	28 $\frac{1}{2}$	39	26 $\frac{1}{2}$	12
8 $\frac{1}{4}$	36	31 $\frac{1}{2}$	12	21 $\frac{1}{2}$	37	28 $\frac{3}{4}$	39	26 $\frac{3}{4}$	12
8 $\frac{1}{2}$	36	31 $\frac{3}{4}$	12	21 $\frac{3}{4}$	37	29	39	27	12
8 $\frac{3}{4}$	36	32	12	22	37	29 $\frac{1}{4}$	39	27 $\frac{1}{4}$	12
8 $\frac{1}{4}$	36	32 $\frac{1}{4}$	12	22 $\frac{1}{4}$	37	29 $\frac{$			

CIRCLES ADVANCING BY AN EIGHTH.

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
12	11 $\frac{7}{8}$	40	9 $\frac{5}{8}$	13	4 $\frac{1}{2}$	41	11	13	8 $\frac{1}{2}$	43	0 $\frac{3}{4}$	14	0 $\frac{1}{4}$	44	1
13	0	40	10	13	4 $\frac{1}{4}$	41	11 $\frac{3}{8}$	13	8 $\frac{3}{8}$	43	1 $\frac{1}{8}$	14	1	44	2
				13	4 $\frac{3}{8}$	41	11 $\frac{1}{2}$	13	8 $\frac{1}{2}$	43	1 $\frac{1}{2}$				
13	0 $\frac{1}{8}$	40	10 $\frac{3}{8}$	13	4 $\frac{1}{2}$	42	0 $\frac{1}{8}$	13	8 $\frac{7}{8}$	43	1 $\frac{1}{4}$	14	1 $\frac{1}{8}$	44	3
13	0 $\frac{1}{4}$	40	10 $\frac{7}{8}$	13	4 $\frac{5}{8}$	42	0 $\frac{1}{4}$	13	9	43	2 $\frac{1}{4}$	14	1 $\frac{1}{4}$	44	4
13	0 $\frac{3}{8}$	40	11 $\frac{1}{4}$	13	4 $\frac{3}{4}$	42	1					14	1 $\frac{3}{8}$	44	5
13	0 $\frac{1}{2}$	40	11 $\frac{1}{2}$	13	4 $\frac{7}{8}$	42	1 $\frac{1}{8}$	13	9 $\frac{1}{8}$	43	2 $\frac{3}{8}$	14	1 $\frac{1}{2}$	44	6
13	0 $\frac{5}{8}$	41	0	13	5	42	1 $\frac{1}{4}$	13	9 $\frac{1}{4}$	43	3 $\frac{1}{8}$	14	1 $\frac{1}{2}$	44	7
13	0 $\frac{3}{4}$	41	0 $\frac{1}{8}$					13	9 $\frac{3}{8}$	43	3 $\frac{3}{8}$	14	1 $\frac{3}{4}$	44	8
13	0 $\frac{7}{8}$	41	0 $\frac{1}{4}$	13	5 $\frac{1}{8}$	42	2 $\frac{1}{8}$	13	9 $\frac{1}{2}$	43	3 $\frac{7}{8}$	14	1 $\frac{7}{8}$	44	9
13	1	41	1 $\frac{1}{8}$	13	5 $\frac{1}{4}$	42	2 $\frac{1}{4}$	13	9 $\frac{5}{8}$	43	4 $\frac{1}{8}$	14	2	44	10
				13	5 $\frac{3}{8}$	42	2 $\frac{3}{8}$	13	9 $\frac{3}{4}$	43	4 $\frac{3}{8}$				
				13	5 $\frac{1}{2}$	42	2 $\frac{1}{2}$	13	9 $\frac{7}{8}$	43	5	14	2 $\frac{1}{8}$	44	11
13	1 $\frac{1}{8}$	41	1 $\frac{1}{4}$	13	5 $\frac{5}{8}$	42	3 $\frac{1}{8}$	13	10	43	5 $\frac{1}{2}$	14	2 $\frac{1}{4}$	44	12
13	1 $\frac{1}{4}$	41	2	13	5 $\frac{3}{4}$	42	3 $\frac{1}{4}$	13	10 $\frac{1}{8}$	43	5 $\frac{5}{8}$	14	2 $\frac{1}{2}$	44	13
13	1 $\frac{3}{8}$	41	2 $\frac{1}{8}$	13	5 $\frac{7}{8}$	42	4 $\frac{1}{8}$	13	10 $\frac{1}{4}$	43	6 $\frac{1}{8}$	14	2 $\frac{3}{8}$	44	14
13	1 $\frac{1}{2}$	41	2 $\frac{1}{4}$	13	6	42	4 $\frac{1}{4}$	13	10 $\frac{3}{8}$	43	6 $\frac{3}{8}$	14	2 $\frac{1}{2}$	44	15
13	1 $\frac{5}{8}$	41	3 $\frac{1}{8}$					13	10 $\frac{1}{2}$	43	7	14	2 $\frac{5}{8}$	44	16
13	1 $\frac{3}{4}$	41	3 $\frac{1}{4}$	13	6 $\frac{1}{8}$	42	5 $\frac{1}{8}$	13	10 $\frac{5}{8}$	43	7 $\frac{1}{8}$	14	2 $\frac{7}{8}$	44	17
13	1 $\frac{7}{8}$	41	3 $\frac{3}{8}$	13	6 $\frac{1}{4}$	42	5 $\frac{1}{4}$	13	10 $\frac{3}{4}$	43	7 $\frac{3}{8}$	14	3	44	18
13	2	41	4 $\frac{1}{8}$	13	6 $\frac{3}{8}$	42	6	13	11	43	8 $\frac{1}{8}$	14	3 $\frac{1}{8}$	44	19
				13	6 $\frac{1}{2}$	42	6 $\frac{1}{2}$	13	11 $\frac{1}{8}$	43	9	14	3 $\frac{1}{4}$	44	20
13	2 $\frac{1}{8}$	41	4 $\frac{1}{4}$	13	6 $\frac{5}{8}$	42	6 $\frac{5}{8}$	13	11 $\frac{1}{4}$	43	9 $\frac{1}{4}$	14	3 $\frac{1}{2}$	44	21
13	2 $\frac{1}{4}$	41	5 $\frac{1}{8}$	13	6 $\frac{3}{4}$	42	7 $\frac{1}{8}$	13	11 $\frac{3}{8}$	43	9 $\frac{3}{8}$	14	3 $\frac{3}{8}$	44	22
13	2 $\frac{3}{8}$	41	5 $\frac{1}{4}$	13	6 $\frac{7}{8}$	42	7 $\frac{1}{4}$	13	11 $\frac{1}{2}$	43	10 $\frac{1}{8}$	14	3 $\frac{1}{2}$	44	23
13	2 $\frac{1}{2}$	41	6 $\frac{1}{8}$	13	7	42	8	13	11 $\frac{5}{8}$	43	10 $\frac{3}{8}$	14	3 $\frac{5}{8}$	44	24
13	2 $\frac{5}{8}$	41	6 $\frac{1}{4}$					13	11 $\frac{3}{4}$	43	11 $\frac{1}{8}$	14	4	45	0
13	2 $\frac{3}{4}$	41	6 $\frac{3}{8}$	13	7 $\frac{1}{8}$	42	8 $\frac{1}{8}$	13	11 $\frac{7}{8}$	43	11 $\frac{3}{8}$	14	4 $\frac{1}{8}$	45	1
13	2 $\frac{7}{8}$	41	7	13	7 $\frac{1}{4}$	42	8 $\frac{1}{4}$	14	0	43	11 $\frac{1}{4}$	14	4 $\frac{1}{4}$	45	2
13	3	41	7 $\frac{1}{8}$	13	7 $\frac{3}{8}$	42	9 $\frac{1}{8}$	14	0 $\frac{1}{8}$	44	0 $\frac{1}{8}$	14	4 $\frac{3}{8}$	45	3
				13	7 $\frac{1}{2}$	42	10	14	0 $\frac{1}{4}$	44	0 $\frac{1}{4}$	14	4 $\frac{1}{2}$	45	4
13	3 $\frac{1}{8}$	41	7 $\frac{3}{8}$	13	7 $\frac{5}{8}$	42	10 $\frac{1}{8}$	14	0 $\frac{1}{2}$	44	0 $\frac{1}{2}$	14	4 $\frac{3}{4}$	45	5
13	3 $\frac{1}{4}$	41	8 $\frac{1}{8}$	13	7 $\frac{3}{4}$	42	10 $\frac{3}{8}$	14	0 $\frac{3}{8}$	44	0 $\frac{3}{8}$	14	4 $\frac{7}{8}$	45	6
13	3 $\frac{3}{8}$	41	8 $\frac{1}{4}$	13	8	42	11 $\frac{1}{8}$	14	0 $\frac{1}{2}$	44	1 $\frac{1}{8}$	14	4 $\frac{1}{2}$	45	7
13	3 $\frac{1}{2}$	41	9 $\frac{1}{8}$					14	0 $\frac{5}{8}$	44	1 $\frac{1}{4}$	14	4 $\frac{3}{4}$	45	8
13	3 $\frac{5}{8}$	41	9 $\frac{1}{4}$	13	8 $\frac{1}{8}$	42	11 $\frac{1}{4}$	14	0 $\frac{3}{4}$	44	1 $\frac{1}{2}$	14	4 $\frac{1}{2}$	45	9
13	3 $\frac{3}{4}$	41	10 $\frac{1}{8}$	13	8 $\frac{1}{4}$	43	0	14	0 $\frac{7}{8}$	44	2 $\frac{1}{8}$	14	5	45	10
13	4	41	10 $\frac{3}{8}$	13	8 $\frac{3}{8}$	43	0 $\frac{1}{8}$	14	0 $\frac{1}{2}$	44	2 $\frac{1}{4}$				

45	5	14	9	46	6	15	2	47	8	15	1
45	5	14	10	46	7	15	2	47	8	15	1
45	5					15	2	47	8	15	1
45	6	14	10	46	7	15	2	47	8	15	1
45	6	14	10	46	7	15	2	47	9	15	1
		14	10	46	8	15	2	47	9	15	1
45	7	14	10	46	8	15	2	47	10	15	1
45	7	14	10	46	9	15	2	47	10	15	1
45	7	14	10	46	9	15	3	47	10	15	1
45	8	14	10	46	9						
45	8	14	11	46	10	15	3	47	11	15	1
45	9					15	3	47	11	15	1
45	9	14	11	46	11	15	3	48	0	15	1
45	9	14	11	46	11	15	3	48	0	15	1
		14	11	46	11	15	3	48	0	15	1
45	10	14	11	46	11	15	3	48	1	15	1
45	10	14	11	47	0	15	3	48	1	15	1
45	10	14	11	47	0	15	4	48	2	15	1
45	11	14	11	47	1					15	1
45	11	15	0	47	1	15	4	48	2	15	1
46	0					15	4	48	2	15	1
46	0	15	0	47	1	15	4	48	3	15	1
46	0	15	0	47	2	15	4	48	3	15	1
		15	0	47	2	15	4	48	4	15	1
46	1	15	0	47	3	15	4	48	4	15	1
46	1	15	0	47	3	15	4	48	4	15	1
46	2	15	0	47	3	15	5	48	5	15	1

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
5	10 $\frac{1}{8}$	49	10 $\frac{1}{8}$	16	2 $\frac{7}{8}$	51	0 $\frac{1}{8}$	16	7 $\frac{1}{8}$	52	1 $\frac{1}{8}$	16	11 $\frac{1}{8}$	53	3 $\frac{1}{8}$
5	10 $\frac{3}{8}$	49	10 $\frac{3}{8}$	16	3	51	0 $\frac{3}{8}$	16	7 $\frac{3}{8}$	52	1 $\frac{3}{8}$	16	11 $\frac{3}{8}$	53	3 $\frac{3}{8}$
5	10 $\frac{5}{8}$	49	11 $\frac{1}{8}$					16	7 $\frac{5}{8}$	52	2 $\frac{1}{8}$	16	11 $\frac{5}{8}$	53	4
5	10 $\frac{7}{8}$	49	11 $\frac{3}{8}$					16	7 $\frac{7}{8}$	52	2 $\frac{3}{8}$	16	11 $\frac{7}{8}$	53	4 $\frac{1}{8}$
5	11	50	0					16	8	52	3 $\frac{1}{8}$	17	0	53	4 $\frac{3}{8}$
				16	3 $\frac{1}{8}$	51	1	16	7 $\frac{1}{8}$	52	3 $\frac{3}{8}$				
				16	3 $\frac{3}{8}$	51	1 $\frac{1}{8}$	16	7 $\frac{3}{8}$	52	3 $\frac{5}{8}$				
5	11 $\frac{1}{8}$	50	0 $\frac{1}{8}$	16	3 $\frac{5}{8}$	51	1 $\frac{3}{8}$	16	7 $\frac{5}{8}$	52	3 $\frac{7}{8}$				
5	11 $\frac{3}{8}$	50	0 $\frac{3}{8}$	16	3 $\frac{7}{8}$	51	2 $\frac{1}{8}$	16	7 $\frac{7}{8}$	52	4 $\frac{1}{8}$				
5	11 $\frac{5}{8}$	50	1 $\frac{1}{8}$	16	3 $\frac{7}{8}$	51	2 $\frac{3}{8}$					17	0 $\frac{1}{8}$	53	5 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	1 $\frac{3}{8}$	16	3 $\frac{7}{8}$	51	2 $\frac{5}{8}$					17	0 $\frac{3}{8}$	53	5 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	1 $\frac{5}{8}$	16	3 $\frac{7}{8}$	51	3 $\frac{1}{8}$	16	8 $\frac{1}{8}$	52	4 $\frac{3}{8}$	17	0 $\frac{5}{8}$	53	6 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	2	16	4	51	3 $\frac{3}{8}$	16	8 $\frac{3}{8}$	52	5	17	0 $\frac{7}{8}$	53	6 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	2 $\frac{1}{8}$					16	8 $\frac{5}{8}$	52	5 $\frac{1}{8}$	17	0 $\frac{7}{8}$	53	7 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	2 $\frac{3}{8}$					16	8 $\frac{7}{8}$	52	5 $\frac{3}{8}$	17	1	53	8
6	0	50	3 $\frac{1}{8}$	16	4 $\frac{1}{8}$	51	4 $\frac{1}{8}$	16	8 $\frac{7}{8}$	52	6 $\frac{1}{8}$				
				16	4 $\frac{3}{8}$	51	4 $\frac{3}{8}$	16	8 $\frac{7}{8}$	52	6 $\frac{3}{8}$				
6	0 $\frac{1}{8}$	50	3 $\frac{3}{8}$	16	4 $\frac{5}{8}$	51	5 $\frac{1}{8}$	16	8 $\frac{7}{8}$	52	7	17	1 $\frac{1}{8}$	53	8 $\frac{1}{8}$
6	0 $\frac{1}{8}$	50	3 $\frac{5}{8}$	16	4 $\frac{5}{8}$	51	5 $\frac{3}{8}$	16	9	52	7 $\frac{1}{8}$	17	1 $\frac{3}{8}$	53	8 $\frac{3}{8}$
6	0 $\frac{3}{8}$	50	4 $\frac{1}{8}$	16	4 $\frac{5}{8}$	51	5 $\frac{5}{8}$					17	1 $\frac{5}{8}$	53	9 $\frac{1}{8}$
6	0 $\frac{3}{8}$	50	4 $\frac{3}{8}$	16	4 $\frac{5}{8}$	51	6	16	9 $\frac{1}{8}$	52	7 $\frac{3}{8}$	17	1 $\frac{5}{8}$	53	9 $\frac{3}{8}$
6	0 $\frac{5}{8}$	50	5 $\frac{1}{8}$	16	4 $\frac{5}{8}$	51	6 $\frac{1}{8}$	16	9 $\frac{1}{8}$	52	8 $\frac{1}{8}$	17	1 $\frac{5}{8}$	53	10
6	0 $\frac{5}{8}$	50	5 $\frac{3}{8}$	16	5	51	6 $\frac{3}{8}$	16	9 $\frac{3}{8}$	52	8 $\frac{3}{8}$	17	1 $\frac{5}{8}$	53	10 $\frac{1}{8}$
6	0 $\frac{5}{8}$	50	5 $\frac{5}{8}$					16	9 $\frac{3}{8}$	52	9	17	1 $\frac{5}{8}$	53	10 $\frac{3}{8}$
6	0 $\frac{7}{8}$	50	6 $\frac{1}{8}$	16	5 $\frac{1}{8}$	51	7 $\frac{1}{8}$	16	9 $\frac{3}{8}$	52	9 $\frac{1}{8}$	17	2	53	11 $\frac{1}{8}$
				16	5 $\frac{3}{8}$	51	7 $\frac{3}{8}$	16	9 $\frac{3}{8}$	52	9 $\frac{3}{8}$				
6	1 $\frac{1}{8}$	50	6 $\frac{3}{8}$	16	5 $\frac{3}{8}$	51	8	16	9 $\frac{5}{8}$	52	10 $\frac{1}{8}$	17	2 $\frac{1}{8}$	53	11 $\frac{3}{8}$
6	1 $\frac{1}{8}$	50	7	16	5 $\frac{5}{8}$	51	8 $\frac{1}{8}$	16	9 $\frac{5}{8}$	52	10 $\frac{3}{8}$	17	2 $\frac{3}{8}$	53	11 $\frac{5}{8}$
6	1 $\frac{3}{8}$	50	7 $\frac{1}{8}$	16	5 $\frac{5}{8}$	51	8 $\frac{3}{8}$					17	2 $\frac{5}{8}$	54	0 $\frac{1}{8}$
6	1 $\frac{3}{8}$	50	7 $\frac{3}{8}$	16	5 $\frac{5}{8}$	51	9 $\frac{1}{8}$	16	10 $\frac{1}{8}$	52	11	17	2 $\frac{5}{8}$	54	0 $\frac{3}{8}$
6	1 $\frac{5}{8}$	50	8 $\frac{1}{8}$	16	5 $\frac{7}{8}$	51	9 $\frac{3}{8}$	16	10 $\frac{1}{8}$	52	11 $\frac{1}{8}$	17	2 $\frac{5}{8}$	54	1 $\frac{1}{8}$
6	1 $\frac{5}{8}$	50	8 $\frac{3}{8}$	16	6	51	10	16	10 $\frac{3}{8}$	52	11 $\frac{3}{8}$	17	2 $\frac{5}{8}$	54	1 $\frac{3}{8}$
6	1 $\frac{5}{8}$	50	9					16	10 $\frac{5}{8}$	53	0 $\frac{1}{8}$	17	2 $\frac{5}{8}$	54	1 $\frac{5}{8}$
6	2	50	9 $\frac{1}{8}$	16	6 $\frac{1}{8}$	51	10 $\frac{1}{8}$	16	10 $\frac{5}{8}$	53	0 $\frac{3}{8}$	17	3	54	2 $\frac{1}{8}$
				16	6 $\frac{3}{8}$	51	10 $\frac{3}{8}$	16	10 $\frac{5}{8}$	53	0 $\frac{5}{8}$				
6	2 $\frac{1}{8}$	50	9 $\frac{3}{8}$	16	6 $\frac{3}{8}$	51	11 $\frac{1}{8}$	16	10 $\frac{7}{8}$	53	1 $\frac{1}{8}$	17	3 $\frac{1}{8}$	54	2 $\frac{3}{8}$
6	2 $\frac{1}{8}$	50	10 $\frac{1}{8}$	16	6 $\frac{5}{8}$	51	11 $\frac{3}{8}$	16	11	53	1 $\frac{3}{8}$	17	3 $\frac{3}{8}$	54	3
6	2 $\frac{3}{8}$	50	10 $\frac{3}{8}$	16	6 $\frac{5}{8}$	52	0					17	3 $\frac{5}{8}$	54	3 $\frac{1}{8}$
6	2 $\frac{3}{8}$	50	11	16	6 $\frac{7}{8}$	52	0 $\frac{1}{8}$	16	11 $\frac{1}{8}$	53	2	17	3 $\frac{5}{8}$	54	3 $\frac{3}{8}$
6	2 $\frac{5}{8}$	50	11 $\frac{1}{8}$	16	6 $\frac{7}{8}$	52	0 $\frac{3}{8}$	16	11 $\frac{3}{8}$	53	2 $\frac{1}{8}$	17	3 $\frac{5}{8}$	54	4 $\frac{1}{8}$
6	2 $\frac{5}{8}$	50	11 $\frac{3}{8}$	16	7	52	1 $\frac{1}{8}$	16	11 $\frac{5}{8}$	53	2 $\frac{3}{8}$	17	3 $\frac{5}{8}$	54	4 $\frac{3}{8}$

54	5 $\frac{3}{8}$	17	8 $\frac{3}{8}$	55	7 $\frac{1}{8}$	18	0 $\frac{7}{8}$	56	9 $\frac{1}{8}$	18
54	6 $\frac{1}{8}$	17	8 $\frac{3}{8}$	55	7 $\frac{3}{8}$	18	1	56	9 $\frac{3}{8}$	18
54	6 $\frac{3}{8}$	17	8 $\frac{3}{8}$	55	8 $\frac{3}{8}$	18	1 $\frac{1}{8}$	56	10	18
54	7	17	8 $\frac{3}{8}$	55	8 $\frac{5}{8}$	18	1 $\frac{1}{4}$	56	10 $\frac{1}{4}$	18
54	7 $\frac{1}{8}$	17	9	55	9 $\frac{1}{8}$	18	1 $\frac{1}{8}$	56	10 $\frac{1}{8}$	18
54	7 $\frac{3}{8}$	17	9 $\frac{1}{8}$	55	9 $\frac{3}{8}$	18	1 $\frac{1}{4}$	56	11 $\frac{1}{4}$	18
54	8 $\frac{1}{8}$	17	9 $\frac{1}{4}$	55	9 $\frac{5}{8}$	18	1 $\frac{1}{8}$	56	11 $\frac{1}{8}$	18
54	8 $\frac{3}{8}$	17	9 $\frac{3}{8}$	55	10 $\frac{1}{4}$	18	1 $\frac{1}{4}$	57	0	18
		17	9 $\frac{5}{8}$	55	10 $\frac{3}{8}$	18	1 $\frac{3}{8}$	57	0 $\frac{3}{8}$	18
54	8 $\frac{5}{8}$	17	9 $\frac{5}{8}$	55	11 $\frac{1}{8}$	18	2	57	0 $\frac{5}{8}$	18
54	9 $\frac{1}{8}$	17	9 $\frac{5}{8}$	55	11 $\frac{3}{8}$	18	2 $\frac{1}{8}$	57	1 $\frac{1}{8}$	18
54	9 $\frac{3}{8}$	17	9 $\frac{5}{8}$	55	11 $\frac{5}{8}$	18	2 $\frac{1}{4}$	57	1 $\frac{1}{4}$	18
54	10 $\frac{1}{8}$	17	10	56	0 $\frac{1}{4}$	18	2 $\frac{1}{8}$	57	2	18
54	10 $\frac{1}{4}$	17	10 $\frac{1}{8}$	56	0 $\frac{3}{8}$	18	2 $\frac{1}{4}$	57	2 $\frac{3}{8}$	18
54	10 $\frac{3}{8}$	17	10 $\frac{1}{4}$	56	1	18	2 $\frac{3}{8}$	57	2 $\frac{5}{8}$	18
54	11 $\frac{1}{8}$	17	10 $\frac{3}{8}$	56	1 $\frac{3}{8}$	18	2 $\frac{5}{8}$	57	3 $\frac{1}{8}$	18
54	11 $\frac{3}{8}$	17	10 $\frac{5}{8}$	56	1 $\frac{5}{8}$	18	2 $\frac{7}{8}$	57	3 $\frac{3}{8}$	18
		17	10 $\frac{7}{8}$	56	2 $\frac{1}{4}$	18	3	57	4	18
55	0 $\frac{1}{8}$	17	10 $\frac{7}{8}$	56	2 $\frac{3}{8}$	18	3 $\frac{1}{8}$	57	4 $\frac{3}{8}$	18
55	0 $\frac{3}{8}$	17	10 $\frac{7}{8}$	56	2 $\frac{5}{8}$	18	3 $\frac{1}{4}$	57	4 $\frac{5}{8}$	18
55	0 $\frac{5}{8}$	17	10 $\frac{7}{8}$	56	3	18	3 $\frac{3}{8}$	57	5 $\frac{1}{8}$	18
55	1 $\frac{1}{8}$	17	11	56	3 $\frac{1}{8}$	18	3 $\frac{1}{2}$	57	5 $\frac{3}{8}$	18
55	1 $\frac{3}{8}$	17	11 $\frac{1}{8}$	56	3 $\frac{3}{8}$	18	3 $\frac{3}{8}$	57	5 $\frac{5}{8}$	18
55	2	17	11 $\frac{1}{4}$	56	4 $\frac{1}{8}$	18	3 $\frac{5}{8}$	57	6 $\frac{1}{8}$	18
55	2 $\frac{1}{8}$	17	11 $\frac{3}{8}$	56	4 $\frac{3}{8}$	18	3 $\frac{7}{8}$	57	6 $\frac{3}{8}$	18
55	2 $\frac{3}{8}$	17	11 $\frac{5}{8}$	56	4 $\frac{5}{8}$	18	4	57	6 $\frac{5}{8}$	18
55	2 $\frac{5}{8}$	17	12	56	5	18	4 $\frac{1}{8}$	57	7	18

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
t.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
8	9 $\frac{1}{2}$	58	11 $\frac{1}{2}$	19	1 $\frac{1}{2}$	59	11 $\frac{1}{2}$	19	5 $\frac{1}{2}$	61	0 $\frac{1}{2}$	19	9 $\frac{1}{2}$	62	0 $\frac{1}{2}$
8	9 $\frac{1}{2}$	58	11 $\frac{1}{2}$	19	1 $\frac{1}{2}$	60	0 $\frac{1}{2}$	19	5 $\frac{1}{2}$	61	0 $\frac{3}{4}$	19	9 $\frac{1}{2}$	62	1 $\frac{1}{4}$
8	9 $\frac{3}{4}$	59	0	19	1 $\frac{3}{4}$	60	0 $\frac{1}{2}$	19	5 $\frac{3}{4}$	61	1 $\frac{1}{4}$	19	9 $\frac{3}{4}$	62	1 $\frac{3}{4}$
8	9 $\frac{3}{4}$	59	0 $\frac{1}{2}$	19	1 $\frac{3}{4}$	60	1	19	5 $\frac{3}{4}$	61	1 $\frac{1}{2}$	19	9 $\frac{3}{4}$	62	2 $\frac{1}{4}$
8	9 $\frac{3}{4}$	59	0 $\frac{3}{4}$	19	1 $\frac{3}{4}$	60	1 $\frac{1}{2}$	19	5 $\frac{3}{4}$	61	1 $\frac{3}{4}$	19	9 $\frac{3}{4}$	62	2 $\frac{3}{4}$
8	9 $\frac{3}{4}$	59	1 $\frac{1}{2}$	19	1 $\frac{3}{4}$	60	1 $\frac{3}{4}$	19	5 $\frac{3}{4}$	61	2 $\frac{1}{4}$	19	9 $\frac{3}{4}$	62	2 $\frac{3}{4}$
8	9 $\frac{3}{4}$	59	1 $\frac{1}{2}$	19	1 $\frac{3}{4}$	60	2 $\frac{1}{2}$	19	5 $\frac{3}{4}$	61	2 $\frac{3}{4}$	19	9 $\frac{3}{4}$	62	3 $\frac{1}{4}$
8	10	59	2	19	2	60	2 $\frac{1}{2}$	19	6	61	3 $\frac{1}{2}$	19	10	62	3 $\frac{1}{2}$
8	10 $\frac{1}{2}$	59	2 $\frac{1}{2}$	19	2 $\frac{1}{2}$	60	2 $\frac{3}{4}$	19	6 $\frac{1}{2}$	61	3 $\frac{3}{4}$	19	10 $\frac{1}{2}$	62	4
8	10 $\frac{1}{2}$	59	2 $\frac{3}{4}$	19	2 $\frac{1}{2}$	61	3 $\frac{1}{4}$	19	6 $\frac{1}{2}$	61	3 $\frac{3}{4}$	19	10 $\frac{1}{2}$	62	4 $\frac{1}{4}$
8	10 $\frac{3}{4}$	59	3 $\frac{1}{4}$	19	2 $\frac{3}{4}$	60	3 $\frac{1}{2}$	19	6 $\frac{3}{4}$	61	4 $\frac{1}{4}$	19	10 $\frac{3}{4}$	62	4 $\frac{3}{4}$
8	10 $\frac{3}{4}$	59	3 $\frac{1}{2}$	19	2 $\frac{3}{4}$	60	4 $\frac{1}{4}$	19	6 $\frac{3}{4}$	61	4 $\frac{3}{4}$	19	10 $\frac{3}{4}$	62	5 $\frac{1}{4}$
8	10 $\frac{3}{4}$	59	3 $\frac{3}{4}$	19	2 $\frac{3}{4}$	60	4 $\frac{3}{4}$	19	6 $\frac{3}{4}$	61	5	19	10 $\frac{3}{4}$	62	5 $\frac{3}{4}$
8	10 $\frac{3}{4}$	59	4 $\frac{1}{4}$	19	2 $\frac{3}{4}$	60	4 $\frac{3}{4}$	19	6 $\frac{3}{4}$	61	5 $\frac{1}{4}$	19	10 $\frac{3}{4}$	62	6
8	10 $\frac{3}{4}$	59	4 $\frac{1}{2}$	19	2 $\frac{3}{4}$	60	5 $\frac{1}{4}$	19	6 $\frac{3}{4}$	61	5 $\frac{3}{4}$	19	10 $\frac{3}{4}$	62	6 $\frac{1}{4}$
8	11	59	5 $\frac{1}{2}$	19	3	60	5 $\frac{3}{4}$	19	7	61	6 $\frac{1}{4}$	19	11	62	6 $\frac{3}{4}$
18	11 $\frac{1}{2}$	59	5 $\frac{1}{2}$	19	3 $\frac{1}{2}$	60	6	19	7 $\frac{1}{2}$	61	6 $\frac{3}{4}$	19	11 $\frac{1}{2}$	62	7 $\frac{1}{4}$
18	11 $\frac{1}{2}$	59	5 $\frac{3}{4}$	19	3 $\frac{1}{2}$	60	6 $\frac{1}{4}$	19	7 $\frac{1}{2}$	61	7	19	11 $\frac{1}{2}$	62	7 $\frac{3}{4}$
18	11 $\frac{3}{4}$	59	6 $\frac{1}{4}$	19	3 $\frac{3}{4}$	60	6 $\frac{3}{4}$	19	7 $\frac{3}{4}$	61	7 $\frac{1}{4}$	19	11 $\frac{3}{4}$	62	8
18	11 $\frac{3}{4}$	59	6 $\frac{1}{2}$	19	3 $\frac{3}{4}$	60	7 $\frac{1}{4}$	19	7 $\frac{3}{4}$	61	7 $\frac{3}{4}$	19	11 $\frac{3}{4}$	62	8 $\frac{1}{4}$
18	11 $\frac{3}{4}$	59	7	19	3 $\frac{3}{4}$	60	7 $\frac{3}{4}$	19	7 $\frac{3}{4}$	61	8 $\frac{1}{4}$	19	11 $\frac{3}{4}$	62	8 $\frac{3}{4}$
18	11 $\frac{3}{4}$	59	7 $\frac{1}{4}$	19	3 $\frac{3}{4}$	60	8	19	7 $\frac{3}{4}$	61	8 $\frac{3}{4}$	19	11 $\frac{3}{4}$	62	9 $\frac{1}{4}$
18	11 $\frac{3}{4}$	59	7 $\frac{3}{4}$	19	3 $\frac{3}{4}$	60	8 $\frac{1}{4}$	19	7 $\frac{3}{4}$	61	9	19	11 $\frac{3}{4}$	62	9 $\frac{3}{4}$
19	0	59	8 $\frac{1}{4}$	19	4	60	8 $\frac{3}{4}$	19	8	61	9 $\frac{1}{4}$	20	0	62	9 $\frac{3}{4}$
19	0 $\frac{1}{4}$	59	8 $\frac{3}{4}$	19	4 $\frac{1}{4}$	60	9 $\frac{1}{4}$	19	8 $\frac{1}{4}$	61	9 $\frac{3}{4}$	20	0 $\frac{1}{4}$	62	10 $\frac{1}{4}$
19	0 $\frac{1}{4}$	59	9	19	4 $\frac{1}{4}$	60	9 $\frac{3}{4}$	19	8 $\frac{1}{4}$	61	10 $\frac{1}{4}$	20	0 $\frac{1}{4}$	62	10 $\frac{3}{4}$
19	0 $\frac{1}{2}$	59	9 $\frac{1}{2}$	19	4 $\frac{1}{2}$	60	10	19	8 $\frac{1}{2}$	61	10 $\frac{3}{4}$	20	0 $\frac{1}{2}$	62	11 $\frac{1}{4}$
9	0 $\frac{1}{2}$	59	9 $\frac{3}{4}$	19	4 $\frac{1}{2}$	60	10 $\frac{1}{4}$	19	8 $\frac{1}{2}$	61	11	20	0 $\frac{1}{2}$	62	11 $\frac{3}{4}$
9	0 $\frac{1}{2}$	59	10 $\frac{1}{4}$	19	4 $\frac{1}{2}$	60	10 $\frac{3}{4}$	19	8 $\frac{1}{2}$	61	11 $\frac{1}{4}$	20	0 $\frac{1}{2}$	62	11 $\frac{3}{4}$
9	0 $\frac{1}{2}$	59	10 $\frac{3}{4}$	19	4 $\frac{1}{2}$	60	11 $\frac{1}{4}$	19	8 $\frac{1}{2}$	61	11 $\frac{3}{4}$	20	0 $\frac{1}{2}$	63	0 $\frac{1}{4}$
9	0 $\frac{3}{4}$	59	11	19	4 $\frac{3}{4}$	60	11 $\frac{3}{4}$	19	8 $\frac{3}{4}$	62	0 $\frac{1}{4}$	20	0 $\frac{3}{4}$	63	0 $\frac{3}{4}$
9	1	59	11 $\frac{1}{4}$	19	5	60	11 $\frac{3}{4}$	19	9	62	0 $\frac{3}{4}$	20	0 $\frac{3}{4}$	63	0 $\frac{3}{4}$

to prove the general utility of these Tables, their simplicity and clearness are sufficient to give their value to the artist and mechanic. It is clearly perceived, on inspection, that the Tables commence with as small a diameter as is generally used in hoops and rings, viz. one inch, and include the regular gradation of one-eighth of an inch upwards of twenty feet; and in the column of Circumference, against each Diameter stand the respective circumferences: hence all that is required on inspecting these Tables is to enter into them any proposed diameter or circumference, and the answer to the inquiry is immediately obtained.

Example.—Required the circumference of a hoop the diameter being 11 feet 7 $\frac{1}{2}$ inches.

In the column of circumferences, opposite the given diameter, stands 36 feet 7 $\frac{3}{8}$ inches, the circumference required.

But it will be necessary to observe, that in the formation of hoops and rings a contraction of metal takes place. Now, the just allowance for this contraction is the exact thickness of the metal.

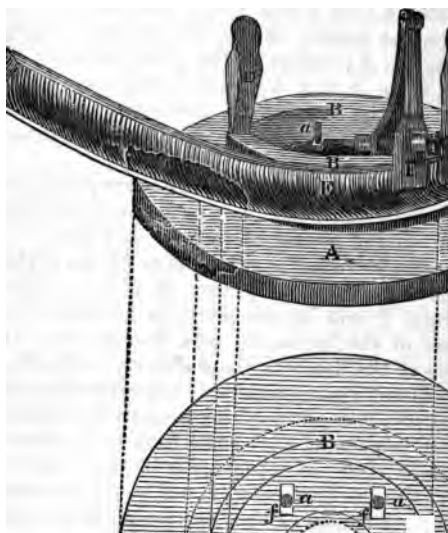
The foregoing example appertains to the formation of hoops or iron bent on the flat; but in the formation of rings or iron bent on the edge, the same rule must also be followed, only taking care to add the *breadth* instead of the thickness. As for example:

To make a ring whose inside diameter is 8 feet $2\frac{1}{4}$ inches, the *breadth* of the iron being $2\frac{1}{4}$ inches; by adding the $2\frac{1}{4}$ inches to the given diameter, will increase it to 8 feet $4\frac{1}{2}$ inches; opposite to this diameter in the column of circumferences stands 26 feet $4\frac{1}{2}$ inches, being the length of iron necessary for the ring.

The foregoing observations relate more particularly to plain hoops and rings; but as respects the hoops that are on the wheels of railway carriages, a difference must be observed, which is as follows: These hoops having a flange projecting on the one edge of the surface it will be necessary, in addition to the thickness of the metal, to add two-thirds of the thickness of the flange to the diameter, as the flange side would contract considerably more than the plain surface; this is supposing the tires are in a straight form, but, in general, they come from the iron-works in a curved state, as represented in the engraving, figure 3. In the latter case, it will be only necessary to add the thickness of the bare metal, as the afore-said portion of the thickness of the flange is allowed for in the curve. By having had some experience in hoops of this nature, I have found that the curve may be exactly obtained, by using four times the circumference of the hoop as a radius.

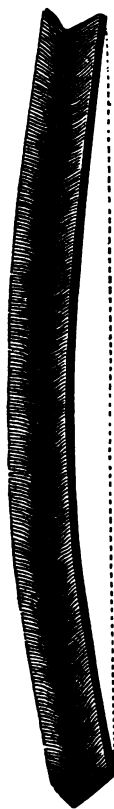
In the engraving, fig. 1, is given a representation of a tire in its curved state, fixed to the blocks, and in the act of being bent; but if the tire has not been previously curved, it may easily be done in the

Figures 1 and 2.



The following is a description of the figures 1 and 2: A is a strong cast-iron ground-plate,

Figure 3.



in which *ffff* are four slot-holes for the bolts *aaaa* to slide in, and are for the purpose of screwing down the two semicircular blocks, to prevent them from moving whilst the tire is in the act of being bent. *BB* is the block in two halves, opening at *cc*; the aperture is cut in a conical form, for the reception of the two conical wedges *DD*, on which the tire *E* is represented. *hh* are two holes in the ground-plate, into which the wedges are driven whilst blocking the hoop. *F* is a strong cramp for screwing the tire firm to the block whilst in the act of being bent round it: it is made with a joint at the top, and secures the tire to the block by means of a strong square-threaded screw, which screws into a boss on the innermost leg.

But the practical utility of this Table is not confined to smiths alone; to the millwright it will be found equally useful and expeditious, as on a bare inspection of the Table he may ascertain the diameter of any wheel that may be required to be made, the pitch and number of teeth being given.

Ex. Suppose a wheel were ordered to be made to contain sixty teeth, the pitch of the teeth to be $3\frac{1}{2}$ inches, the dimensions of the wheel may be ascertained simply as follows:

Multiply the pitch of the tooth by the

5	5 $\frac{1}{2}$	14	10	46	7 $\frac{1}{2}$	15	2 $\frac{1}{2}$	47	8 $\frac{1}{2}$	15	6
5	5 $\frac{3}{4}$					15	2 $\frac{3}{4}$	47	8 $\frac{3}{4}$	15	6
5	6 $\frac{1}{4}$	14	10 $\frac{1}{4}$	46	7 $\frac{3}{4}$	15	2 $\frac{1}{2}$	47	9 $\frac{1}{4}$	15	7
5	6 $\frac{3}{4}$	14	10 $\frac{3}{4}$	46	7 $\frac{3}{4}$	15	2 $\frac{3}{4}$	47	9 $\frac{3}{4}$	15	7
		14	10 $\frac{1}{2}$	46	8 $\frac{1}{2}$	15	2 $\frac{1}{2}$	47	10 $\frac{1}{2}$	15	7
5	7	14	10 $\frac{1}{2}$	46	8 $\frac{1}{2}$	15	2 $\frac{3}{4}$	47	10 $\frac{3}{4}$	15	7
5	7 $\frac{1}{2}$	14	10 $\frac{3}{4}$	46	9 $\frac{1}{4}$	15	3	47	10 $\frac{3}{4}$	15	7
5	7 $\frac{3}{4}$	14	10 $\frac{3}{4}$	46	9 $\frac{1}{4}$					15	7
5	8 $\frac{1}{4}$	14	10 $\frac{3}{4}$	46	9 $\frac{3}{4}$					15	7
5	8 $\frac{3}{4}$	14	11	46	10 $\frac{1}{4}$					15	7
5	9					15	3 $\frac{1}{4}$	47	11 $\frac{1}{4}$	15	7
5	9 $\frac{1}{4}$	14	11 $\frac{1}{4}$	46	10 $\frac{3}{4}$	15	3 $\frac{1}{2}$	47	11 $\frac{1}{2}$	15	7
5	9 $\frac{3}{4}$	14	11 $\frac{1}{2}$	46	11 $\frac{1}{4}$	15	3 $\frac{3}{4}$	48	0	15	7
		14	11 $\frac{3}{4}$	46	11 $\frac{1}{2}$	15	3 $\frac{1}{2}$	48	0 $\frac{1}{4}$	15	7
		14	11 $\frac{1}{2}$	46	11 $\frac{3}{4}$	15	3 $\frac{3}{4}$	48	0 $\frac{3}{4}$	15	7
15	10 $\frac{1}{4}$	14	11 $\frac{1}{2}$	46	11 $\frac{3}{4}$	15	3 $\frac{1}{2}$	48	1 $\frac{1}{4}$	15	7
15	10 $\frac{1}{2}$	14	11 $\frac{3}{4}$	47	0 $\frac{1}{4}$	15	3 $\frac{3}{4}$	48	1 $\frac{3}{4}$	15	7
15	10 $\frac{3}{4}$	14	11 $\frac{3}{4}$	47	0 $\frac{3}{4}$	15	4	48	2	15	7
15	11 $\frac{1}{4}$	14	11 $\frac{3}{4}$	47	1					15	7
15	11 $\frac{3}{4}$	15	0	47	1 $\frac{1}{4}$	15	4 $\frac{1}{4}$	48	2 $\frac{1}{4}$	15	7
46	0 $\frac{1}{4}$					15	4 $\frac{1}{2}$	48	2 $\frac{1}{2}$	15	7
46	0 $\frac{1}{2}$	15	0 $\frac{1}{4}$	47	1 $\frac{3}{4}$	15	4 $\frac{3}{4}$	48	3 $\frac{1}{4}$	15	7
46	0 $\frac{3}{4}$	15	0 $\frac{1}{2}$	47	2 $\frac{1}{4}$	15	4 $\frac{1}{2}$	48	3 $\frac{3}{4}$	15	7
		15	0 $\frac{3}{4}$	47	2 $\frac{3}{4}$	15	4 $\frac{3}{4}$	48	4	15	7
46	1 $\frac{1}{4}$	15	0 $\frac{3}{4}$	47	3	15	4 $\frac{1}{2}$	48	4 $\frac{1}{4}$	15	7
46	1 $\frac{1}{2}$	15	0 $\frac{3}{4}$	47	3 $\frac{1}{4}$	15	4 $\frac{3}{4}$	48	4 $\frac{3}{4}$	15	7
46	2	15	0 $\frac{3}{4}$	47	3 $\frac{3}{4}$	15	5	48	5 $\frac{1}{4}$	15	7
46	2 $\frac{1}{4}$	15	0 $\frac{3}{4}$	47	4 $\frac{1}{4}$					15	7

Diam.		Circum.		Diam.		Circum.		Diam.		Circum.		Diam.		Circum.	
Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.	Ft.	In.
5	10 $\frac{1}{8}$	49	10 $\frac{1}{8}$	16	2 $\frac{7}{8}$	51	0 $\frac{1}{8}$	16	7 $\frac{1}{8}$	52	1 $\frac{1}{8}$	16	11 $\frac{1}{8}$	53	3 $\frac{1}{8}$
5	10 $\frac{3}{8}$	49	10 $\frac{3}{8}$	16	3	51	0 $\frac{3}{8}$	16	7 $\frac{3}{8}$	52	1 $\frac{3}{8}$	16	11 $\frac{3}{8}$	53	3 $\frac{3}{8}$
5	10 $\frac{5}{8}$	49	11 $\frac{1}{8}$					16	7 $\frac{5}{8}$	52	2 $\frac{1}{8}$	16	11 $\frac{5}{8}$	53	4
5	10 $\frac{7}{8}$	49	11 $\frac{3}{8}$					16	7 $\frac{7}{8}$	52	2 $\frac{3}{8}$	16	11 $\frac{7}{8}$	53	4 $\frac{1}{8}$
5	11	50	0	16	3 $\frac{1}{8}$	51	1	16	7 $\frac{7}{8}$	52	2 $\frac{5}{8}$	17	0	53	4 $\frac{1}{8}$
				16	3 $\frac{1}{4}$	51	1 $\frac{1}{8}$	16	7 $\frac{7}{8}$	52	3 $\frac{1}{8}$				
5	11 $\frac{1}{8}$	50	0 $\frac{1}{8}$	16	3 $\frac{1}{4}$	51	1 $\frac{1}{4}$	16	7 $\frac{7}{8}$	52	3 $\frac{1}{4}$	17	0 $\frac{1}{8}$	53	5 $\frac{1}{8}$
5	11 $\frac{1}{4}$	50	0 $\frac{3}{8}$	16	3 $\frac{1}{2}$	51	2 $\frac{1}{8}$	16	7 $\frac{7}{8}$	52	3 $\frac{3}{8}$	17	0 $\frac{1}{4}$	53	5 $\frac{3}{8}$
5	11 $\frac{3}{8}$	50	1 $\frac{1}{8}$	16	3 $\frac{3}{8}$	51	2 $\frac{1}{4}$	16	8	52	4 $\frac{1}{8}$	17	0 $\frac{1}{2}$	53	6
5	11 $\frac{5}{8}$	50	1 $\frac{3}{8}$	16	3 $\frac{5}{8}$	51	2 $\frac{3}{8}$					17	0 $\frac{3}{8}$	53	6 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	2	16	3 $\frac{7}{8}$	51	3 $\frac{1}{8}$	16	8 $\frac{1}{8}$	52	4 $\frac{1}{4}$	17	0 $\frac{1}{2}$	53	6 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	2 $\frac{1}{8}$	16	4	51	3 $\frac{1}{4}$	16	8 $\frac{1}{4}$	52	5	17	0 $\frac{1}{2}$	53	6 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	2 $\frac{3}{8}$					16	8 $\frac{3}{8}$	52	5 $\frac{1}{8}$	17	0 $\frac{3}{4}$	53	7 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	2 $\frac{5}{8}$	16	4 $\frac{1}{8}$	51	4 $\frac{1}{8}$	16	8 $\frac{3}{8}$	52	5 $\frac{3}{8}$	17	0 $\frac{3}{4}$	53	7 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	2 $\frac{7}{8}$	16	4 $\frac{1}{4}$	51	4 $\frac{1}{4}$	16	8 $\frac{3}{8}$	52	6 $\frac{1}{8}$	17	1	53	8
5	11 $\frac{7}{8}$	50	3	16	4 $\frac{1}{2}$	51	5 $\frac{1}{8}$	16	8 $\frac{3}{8}$	52	6 $\frac{1}{4}$				
5	11 $\frac{7}{8}$	50	3 $\frac{1}{8}$	16	4 $\frac{3}{8}$	51	5 $\frac{1}{4}$	16	8 $\frac{3}{8}$	52	6 $\frac{3}{8}$	17	1 $\frac{1}{8}$	53	8 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	3 $\frac{1}{4}$	16	4 $\frac{3}{4}$	51	5 $\frac{3}{8}$	16	8 $\frac{3}{8}$	52	7	17	1 $\frac{1}{4}$	53	8 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	3 $\frac{1}{2}$	16	4 $\frac{7}{8}$	51	5 $\frac{5}{8}$	16	8 $\frac{3}{8}$	52	7 $\frac{1}{8}$	17	1 $\frac{1}{2}$	53	9 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	3 $\frac{3}{8}$	16	5	51	6 $\frac{1}{8}$	16	9 $\frac{1}{8}$	52	7 $\frac{3}{8}$	17	1 $\frac{1}{2}$	53	9 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	3 $\frac{5}{8}$	16	5 $\frac{1}{4}$	51	6 $\frac{1}{4}$	16	9 $\frac{1}{4}$	52	8 $\frac{1}{8}$	17	1 $\frac{1}{2}$	53	10
5	11 $\frac{7}{8}$	50	4	16	5 $\frac{1}{2}$	51	6 $\frac{3}{8}$	16	9 $\frac{1}{4}$	52	8 $\frac{3}{8}$	17	1 $\frac{3}{4}$	53	10 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	4 $\frac{1}{8}$	16	5 $\frac{3}{4}$	51	6 $\frac{5}{8}$	16	9 $\frac{1}{4}$	52	9	17	1 $\frac{3}{4}$	53	10 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	4 $\frac{1}{4}$	16	5 $\frac{7}{8}$	51	7 $\frac{1}{8}$	16	9 $\frac{1}{4}$	52	9 $\frac{1}{8}$	17	1 $\frac{3}{4}$	53	10 $\frac{5}{8}$
5	11 $\frac{7}{8}$	50	4 $\frac{1}{2}$	16	6	51	7 $\frac{3}{8}$	16	9 $\frac{1}{4}$	52	9 $\frac{3}{8}$	17	2	53	11 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	4 $\frac{3}{8}$	16	6 $\frac{1}{8}$	51	7 $\frac{5}{8}$	16	9 $\frac{1}{4}$	52	9 $\frac{5}{8}$				
5	11 $\frac{7}{8}$	50	4 $\frac{3}{4}$	16	6 $\frac{1}{4}$	51	8 $\frac{1}{8}$	16	9 $\frac{1}{4}$	52	10 $\frac{1}{8}$	17	2 $\frac{1}{8}$	53	11 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	4 $\frac{5}{8}$	16	6 $\frac{3}{8}$	51	8 $\frac{3}{8}$	16	9 $\frac{1}{4}$	52	10 $\frac{3}{8}$	17	2 $\frac{1}{4}$	53	11 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	4 $\frac{5}{4}$	16	6 $\frac{3}{4}$	51	8 $\frac{5}{8}$	16	10	52	10 $\frac{5}{8}$	17	2 $\frac{1}{2}$	54	0 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	5	16	6 $\frac{7}{8}$	51	9 $\frac{1}{8}$	16	10	52	11	17	2 $\frac{1}{2}$	54	0 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	5 $\frac{1}{8}$	16	7	51	9 $\frac{3}{8}$	16	10	52	11 $\frac{1}{8}$	17	2 $\frac{1}{2}$	54	1 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	5 $\frac{1}{4}$	16	7 $\frac{1}{8}$	51	9 $\frac{5}{8}$	16	10	52	11 $\frac{3}{8}$	17	2 $\frac{3}{4}$	54	1 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	5 $\frac{1}{2}$	16	7 $\frac{1}{4}$	51	10 $\frac{1}{8}$	16	10	52	11 $\frac{5}{8}$	17	2 $\frac{3}{4}$	54	1 $\frac{5}{8}$
5	11 $\frac{7}{8}$	50	5 $\frac{3}{8}$	16	7 $\frac{3}{8}$	51	10 $\frac{3}{8}$	16	10	52	11 $\frac{7}{8}$	17	2 $\frac{7}{8}$	54	2
5	11 $\frac{7}{8}$	50	5 $\frac{3}{4}$	16	7 $\frac{5}{8}$	51	10 $\frac{5}{8}$	16	10	52	12	17	3	54	2 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	5 $\frac{7}{8}$	16	8	51	11 $\frac{1}{8}$	16	10	52	12 $\frac{1}{8}$				
5	11 $\frac{7}{8}$	50	6	16	8 $\frac{1}{8}$	51	11 $\frac{3}{8}$	16	10	52	12 $\frac{3}{8}$	17	3 $\frac{1}{8}$	54	2 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	6 $\frac{1}{8}$	16	8 $\frac{1}{4}$	51	11 $\frac{5}{8}$	16	10	52	12 $\frac{5}{8}$	17	3 $\frac{1}{4}$	54	3
5	11 $\frac{7}{8}$	50	6 $\frac{1}{4}$	16	8 $\frac{1}{2}$	51	11 $\frac{7}{8}$	16	10	52	13	17	3 $\frac{1}{2}$	54	3 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	6 $\frac{3}{8}$	16	8 $\frac{3}{8}$	51	12 $\frac{1}{8}$	16	10	52	13 $\frac{1}{8}$	17	3 $\frac{1}{2}$	54	3 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	6 $\frac{3}{4}$	16	8 $\frac{3}{4}$	51	12 $\frac{3}{8}$	16	10	52	13 $\frac{3}{8}$	17	3 $\frac{3}{4}$	54	3 $\frac{5}{8}$
5	11 $\frac{7}{8}$	50	6 $\frac{7}{8}$	16	8 $\frac{7}{8}$	51	12 $\frac{5}{8}$	16	10	52	13 $\frac{5}{8}$	17	3 $\frac{7}{8}$	54	4
5	11 $\frac{7}{8}$	50	7	16	9	51	13 $\frac{1}{8}$	16	10	52	14	17	4	54	4 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	7 $\frac{1}{8}$	16	9 $\frac{1}{8}$	51	13 $\frac{3}{8}$	16	10	52	14 $\frac{1}{8}$				
5	11 $\frac{7}{8}$	50	7 $\frac{1}{4}$	16	9 $\frac{1}{4}$	51	13 $\frac{5}{8}$	16	10	52	14 $\frac{3}{8}$	17	4 $\frac{1}{8}$	54	4 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	7 $\frac{1}{2}$	16	9 $\frac{1}{2}$	51	14 $\frac{1}{8}$	16	10	52	14 $\frac{5}{8}$	17	4 $\frac{1}{4}$	54	4 $\frac{1}{2}$
5	11 $\frac{7}{8}$	50	7 $\frac{3}{8}$	16	9 $\frac{3}{8}$	51	14 $\frac{3}{8}$	16	10	52	15	17	4 $\frac{3}{8}$	54	4 $\frac{3}{8}$
5	11 $\frac{7}{8}$	50	7 $\frac{3}{4}$	16	9 $\frac{3}{4}$	51	14 $\frac{5}{8}$	16	10	52	15 $\frac{1}{8}$	17	4 $\frac{3}{4}$	54	4 $\frac{5}{8}$
5	11 $\frac{7}{8}$	50	7 $\frac{7}{8}$	16	9 $\frac{7}{8}$	51	15 $\frac{1}{8}$	16	10	52	15 $\frac{3}{8}$	17	4 $\frac{7}{8}$	54	5
5	11 $\frac{7}{8}$	50	8	16	10	51	15 $\frac{3}{8}$	16	10	52	15 $\frac{5}{8}$	17	5	54	5 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	8 $\frac{1}{8}$	16	10 $\frac{1}{8}$	51	15 $\frac{5}{8}$	16	10	52	16	17	5 $\frac{1}{4}$	54	5 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	8 $\frac{1}{4}$	16	10 $\frac{1}{4}$	51	15 $\frac{7}{8}$	16	10	52	16 $\frac{1}{8}$	17	5 $\frac{1}{2}$	54	5 $\frac{1}{2}$
5	11 $\frac{7}{8}$	50	8 $\frac{1}{2}$	16	10 $\frac{1}{2}$	51	16 $\frac{1}{8}$	16	10	52	16 $\frac{1}{4}$	17	5 $\frac{3}{4}$	54	5 $\frac{3}{4}$
5	11 $\frac{7}{8}$	50	8 $\frac{3}{8}$	16	10 $\frac{3}{8}$	51	16 $\frac{3}{8}$	16	10	52	16 $\frac{3}{8}$	17	5 $\frac{7}{8}$	54	6
5	11 $\frac{7}{8}$	50	8 $\frac{3}{4}$	16	10 $\frac{3}{4}$	51	16 $\frac{5}{8}$	16	10	52	16 $\frac{5}{8}$	17	6	54	6 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	8 $\frac{7}{8}$	16	10 $\frac{7}{8}$	51	16 $\frac{7}{8}$	16	10	52	17	17	6 $\frac{1}{4}$	54	6 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	9	16	11	51	17 $\frac{1}{8}$	16	10	52	17 $\frac{1}{8}$	17	6 $\frac{1}{2}$	54	6 $\frac{1}{2}$
5	11 $\frac{7}{8}$	50	9 $\frac{1}{8}$	16	11 $\frac{1}{8}$	51	17 $\frac{3}{8}$	16	10	52	17 $\frac{3}{8}$	17	6 $\frac{3}{4}$	54	6 $\frac{3}{4}$
5	11 $\frac{7}{8}$	50	9 $\frac{1}{4}$	16	11 $\frac{1}{4}$	51	17 $\frac{5}{8}$	16	10	52	17 $\frac{5}{8}$	17	7	54	7
5	11 $\frac{7}{8}$	50	9 $\frac{1}{2}$	16	11 $\frac{1}{2}$	51	18 $\frac{1}{8}$	16	10	52	18	17	7 $\frac{1}{8}$	54	7 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	9 $\frac{3}{8}$	16	11 $\frac{3}{8}$	51	18 $\frac{3}{8}$	16	10	52	18 $\frac{1}{8}$	17	7 $\frac{1}{4}$	54	7 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	9 $\frac{3}{4}$	16	11 $\frac{3}{4}$	51	18 $\frac{5}{8}$	16	10	52	18 $\frac{3}{8}$	17	7 $\frac{1}{2}$	54	7 $\frac{1}{2}$
5	11 $\frac{7}{8}$	50	9 $\frac{7}{8}$	16	11 $\frac{7}{8}$	51	19 $\frac{1}{8}$	16	10	52	18 $\frac{5}{8}$	17	7 $\frac{3}{4}$	54	7 $\frac{3}{4}$
5	11 $\frac{7}{8}$	50	10	16	12	51	19 $\frac{3}{8}$	16	10	52	19	17	7 $\frac{7}{8}$	54	8
5	11 $\frac{7}{8}$	50	10 $\frac{1}{8}$	16	12 $\frac{1}{8}$	51	19 $\frac{5}{8}$	16	10	52	19 $\frac{1}{8}$	17	8	54	8 $\frac{1}{8}$
5	11 $\frac{7}{8}$	50	10 $\frac{1}{4}$	16	12 $\frac{1}{4}$	51	20 $\frac{1}{8}$	16	10	52	19 $\frac{3}{8}$	17	8 $\frac{1}{4}$	54	8 $\frac{1}{4}$
5	11 $\frac{7}{8}$	50	10 $\frac{1}{2}$	16	12 $\frac{1}{2}$	51	20 $\frac{3}{8}$	16	10	52	19 $\frac{5}{8}$	17	8 $\frac{1}{2}$	54	8 $\frac{1}{2}$
5	11 $\frac{7}{8}$	50	10 $\frac{3}{8}$	16	12 $\frac{3}{8}$	51	20 $\frac{5}{8}$	16	10	52	20	17	8 $\frac{3}{4}$	54	8 $\frac{3}{4}$
5	11 $\frac{7}{8}$	50	10 $\frac{3}{4}$	16	12 $\frac{3}{4}$	51	21 $\frac{1}{8}$	16	10	52	20 $\frac{1}{8}$	17	8 $\frac{3}{4}$		

[illegible]

TABLE OF FLAT IRON.

Thick.	Broad.	lbs. oz.	Thick.	Broad.	lbs. oz.	Thick.	Broad.	lbs. oz.
in.	in.		in.	in.		in.	in.	
$\frac{1}{4}$	$11\frac{1}{8}$	4 9·8	$\frac{1}{4}$	4	3 5·1	$\frac{1}{4}$	$8\frac{1}{8}$	7 2·5
	$11\frac{1}{4}$	4 10·7		$4\frac{1}{8}$	3 6·7		$8\frac{3}{4}$	7 4·2
	$11\frac{3}{8}$	4 11·5		$4\frac{1}{4}$	3 8·4		$8\frac{5}{8}$	7 5·8
	$11\frac{1}{2}$	4 12·3		$4\frac{3}{8}$	3 10·1		9	7 7·5
	$11\frac{5}{8}$	4 13·2		$4\frac{1}{2}$	3 11·7		$9\frac{1}{8}$	7 9·1
	$11\frac{3}{4}$	4 14·0		$4\frac{5}{8}$	3 13·4		$9\frac{1}{4}$	7 10·8
	$11\frac{7}{8}$	4 14·8		$4\frac{3}{4}$	3 15·0		$9\frac{3}{8}$	7 12·5
	12	4 15·6		$4\frac{7}{8}$	4 0·7		$9\frac{1}{2}$	7 14·1
				5	4 2·4		$9\frac{5}{8}$	7 15·8
	$\frac{1}{2}$	0 6·6		$5\frac{1}{8}$	4 4·0		$9\frac{3}{4}$	8 1·4
	$\frac{3}{4}$	0 8·3		$5\frac{1}{4}$	4 5·7		$9\frac{7}{8}$	8 3·1
	$\frac{1}{2}$	0 10·0		$5\frac{3}{8}$	4 7·3		10	8 4·8
	$\frac{3}{4}$	0 11·6		$5\frac{1}{2}$	4 9·0		$10\frac{1}{8}$	8 6·4
	1	0 13·2		$5\frac{5}{8}$	4 10·7		$10\frac{1}{4}$	8 8·1
	$1\frac{1}{8}$	0 14·9		$5\frac{3}{4}$	4 12·3		$10\frac{3}{8}$	8 9·7
	$1\frac{1}{4}$	1 0·6		$5\frac{7}{8}$	4 14·0		$10\frac{1}{2}$	8 11·4
	$1\frac{3}{8}$	1 2·2		6	4 15·6		$10\frac{5}{8}$	8 13·1
	$1\frac{1}{2}$	1 3·9		$6\frac{1}{8}$	5 1·3		$10\frac{3}{4}$	8 14·7
	$1\frac{5}{8}$	1 5·5		$6\frac{1}{4}$	5 3·0		$10\frac{7}{8}$	9 0·4
	$1\frac{3}{4}$	1 7·2		$6\frac{3}{8}$	5 4·6		11	9 2·0
	$1\frac{7}{8}$	1 9·0		$6\frac{1}{2}$	5 6·3		$11\frac{1}{8}$	9 3·7
	2	1 10·5		$6\frac{5}{8}$	5 7·9		$11\frac{1}{4}$	9 5·4
	$2\frac{1}{8}$	1 12·2		$6\frac{3}{4}$	5 9·6		$11\frac{3}{8}$	9 7·0
	$2\frac{1}{4}$	1 13·8		$6\frac{7}{8}$	5 11·3		$11\frac{1}{2}$	9 8·7
	$2\frac{3}{8}$	1 15·5		7	5 13·0		$11\frac{5}{8}$	9 10·3
	$2\frac{1}{2}$	2 1·2		$7\frac{1}{8}$	5 14·6		$11\frac{3}{4}$	9 12·0
	$2\frac{5}{8}$	2 2·8		$7\frac{1}{4}$	6 0·2		$11\frac{7}{8}$	9 13·7
	$2\frac{3}{4}$	2 4·5		$7\frac{3}{8}$	6 2·0		12	9 15·3
	$2\frac{7}{8}$	2 6·1		$7\frac{1}{2}$	6 3·6			
	3	2 7·8		$7\frac{5}{8}$	6 5·2		$\frac{3}{8}$	0 14·9
	$3\frac{1}{8}$	2 9·5		$7\frac{3}{4}$	6 7·0		$\frac{7}{8}$	1 1·3
	$3\frac{1}{4}$	2 11·1		$7\frac{7}{8}$	6 8·5		1	1 3·8
	$3\frac{3}{8}$	2 12·8		8	6 10·2		$1\frac{1}{8}$	1 6·3
	$3\frac{1}{2}$	2 14·4		$8\frac{1}{8}$	6 12·0		$1\frac{1}{4}$	1 8·8
	$3\frac{5}{8}$	3 0·1		$8\frac{1}{4}$	6 13·5		$1\frac{3}{8}$	1 11·3
	$3\frac{3}{4}$	3 1·8		$8\frac{3}{8}$	6 15·2		$1\frac{1}{2}$	1 13·8
	$3\frac{7}{8}$	3 3·4		$8\frac{1}{2}$	7 0·8		$1\frac{5}{8}$	2 0·3

2	2	7.7	6	8	3.6	11	1
2 $\frac{1}{2}$	2	10.2	6 $\frac{1}{2}$	8	6.1	11 $\frac{1}{2}$	1
2 $\frac{1}{4}$	2	12.7	6 $\frac{3}{4}$	8	8.6	11 $\frac{3}{4}$	1
2 $\frac{3}{8}$	2	15.1	7	8	11.1	11 $\frac{5}{8}$	1
2 $\frac{1}{2}$	3	1.6	7 $\frac{1}{8}$	8	13.5	11 $\frac{3}{4}$	1
2 $\frac{3}{8}$	3	4.1	7 $\frac{1}{4}$	9	0.0	11 $\frac{1}{2}$	1
2 $\frac{1}{2}$	3	6.6	7 $\frac{3}{8}$	9	2.5	12	1
2 $\frac{3}{8}$	3	9.1	7 $\frac{1}{2}$	9	5.0		
3	3	11.6	7 $\frac{5}{8}$	9	7.5	1	
3 $\frac{1}{8}$	3	14.1	7 $\frac{3}{4}$	9	10.0	1 $\frac{1}{8}$	
3 $\frac{1}{4}$	4	0.5	7 $\frac{7}{8}$	9	12.4	1 $\frac{1}{4}$	
3 $\frac{3}{8}$	4	3.0	8	9	14.9	1 $\frac{3}{8}$	
3 $\frac{1}{2}$	4	5.5	8 $\frac{1}{8}$	10	1.4	1 $\frac{1}{2}$	
3 $\frac{3}{8}$	4	8.0	8 $\frac{1}{4}$	10	3.9	1 $\frac{5}{8}$	
3 $\frac{1}{2}$	4	10.5	8 $\frac{3}{8}$	10	6.4	1 $\frac{3}{4}$	
3 $\frac{5}{8}$	4	13.0	8 $\frac{1}{2}$	10	8.9	1 $\frac{7}{8}$	
4	4	15.4	8 $\frac{5}{8}$	10	11.3	2	
4 $\frac{1}{8}$	5	1.9	8 $\frac{3}{4}$	10	13.8	2 $\frac{1}{8}$	
4 $\frac{1}{4}$	5	4.4	8 $\frac{7}{8}$	11	0.3	2 $\frac{1}{4}$	
4 $\frac{3}{8}$	5	6.9	9	11	2.8	2 $\frac{3}{8}$	
4 $\frac{1}{2}$	5	9.4	9 $\frac{1}{8}$	11	5.3	2 $\frac{1}{2}$	
4 $\frac{3}{8}$	5	11.9	9 $\frac{1}{4}$	11	7.8	2 $\frac{5}{8}$	
4 $\frac{1}{2}$	5	14.3	9 $\frac{3}{8}$	11	10.3	2 $\frac{3}{4}$	
4 $\frac{5}{8}$	6	0.8	9 $\frac{1}{2}$	11	12.7	2 $\frac{7}{8}$	
5	6	3.3	9 $\frac{5}{8}$	11	15.2	3	
5 $\frac{1}{8}$	6	5.8	9 $\frac{3}{4}$	12	1.7	3 $\frac{1}{8}$	
5 $\frac{1}{4}$	6	8.2	9 $\frac{7}{8}$	12	4.2	3 $\frac{1}{4}$	

Thick.	Broad.	lbs. oz.	Thick.	Broad.	lbs. oz.	Thick.	Broad.	lbs. oz.
in.	in.		in.	in.		in.	in.	
$4\frac{3}{8}$	7	3·9	$9\frac{1}{8}$	14	14·4	$2\frac{3}{8}$	5	6·9
$4\frac{1}{2}$	7	7·2	$9\frac{1}{4}$	15	1·7	$2\frac{1}{2}$	5	11·0
$4\frac{5}{8}$	7	10·5	$9\frac{3}{8}$	15	5·0	$2\frac{7}{8}$	5	15·2
$4\frac{7}{8}$	7	13·8	$9\frac{5}{8}$	15	8·4	3	6	3·3
$4\frac{7}{8}$	8	1·1	$9\frac{1}{2}$	15	11·7	$3\frac{1}{8}$	6	7·5
5	8	4·4	$9\frac{3}{4}$	15	15·0	$3\frac{1}{4}$	6	11·6
$5\frac{1}{8}$	8	7·7	$9\frac{7}{8}$	16	2·3	$3\frac{3}{8}$	6	15·7
$5\frac{1}{4}$	8	11·1	$9\frac{7}{8}$	16	5·6	$3\frac{1}{2}$	7	3·9
$5\frac{3}{8}$	8	14·4	10	16	8·9	$3\frac{5}{8}$	7	8·0
$5\frac{1}{2}$	9	1·7	$10\frac{1}{8}$	16	12·2	$3\frac{7}{8}$	7	12·2
$5\frac{5}{8}$	9	5·0	$10\frac{1}{4}$	16	15·5	$3\frac{7}{8}$	8	0·3
$5\frac{3}{4}$	9	8·3	$10\frac{3}{8}$	17	2·8	4	8	4·4
$5\frac{7}{8}$	9	11·6	$10\frac{1}{2}$	17	6·2	$4\frac{1}{8}$	8	8·6
6	9	14·9	$10\frac{3}{4}$	17	9·5	$4\frac{1}{4}$	8	12·7
$6\frac{1}{8}$	10	2·2	$10\frac{5}{8}$	17	12·8	$4\frac{3}{8}$	9	0·9
$6\frac{1}{4}$	10	5·6	$10\frac{7}{8}$	18	0·1	$4\frac{1}{2}$	9	5·0
$6\frac{3}{8}$	10	8·9	11	18	3·4	$4\frac{3}{4}$	9	9·1
$6\frac{1}{2}$	10	12·2	$11\frac{1}{8}$	18	6·7	$4\frac{7}{8}$	9	13·3
$6\frac{5}{8}$	10	15·5	$11\frac{1}{4}$	18	10·0	$4\frac{7}{8}$	10	1·4
$6\frac{3}{4}$	11	2·8	$11\frac{3}{8}$	18	13·3	5	10	5·6
$6\frac{7}{8}$	11	6·1	$11\frac{1}{2}$	19	0·7	$5\frac{1}{8}$	10	9·7
7	11	9·4	$11\frac{3}{4}$	19	4·0	$5\frac{1}{4}$	10	13·8
$7\frac{1}{8}$	11	12·7	$11\frac{5}{8}$	19	7·3	$5\frac{3}{8}$	11	2·0
$7\frac{1}{4}$	12	0·0	$11\frac{7}{8}$	19	10·6	$5\frac{1}{2}$	11	6·1
$7\frac{3}{8}$	12	3·4	12	19	13·9	$5\frac{5}{8}$	11	10·3
$7\frac{1}{2}$	12	6·7				$5\frac{3}{4}$	11	14·4
$7\frac{5}{8}$	12	10·0	$1\frac{1}{8}$	2	9·4	$5\frac{7}{8}$	12	2·5
$7\frac{3}{4}$	12	13·3	$1\frac{3}{8}$	2	13·5	6	12	6·7
$7\frac{7}{8}$	13	0·6	$1\frac{1}{2}$	3	1·6	$6\frac{1}{8}$	12	10·8
8	13	3·9	$1\frac{3}{4}$	3	5·8	$6\frac{1}{4}$	12	15·0
$8\frac{1}{8}$	13	7·2	$1\frac{5}{8}$	3	9·9	$6\frac{3}{8}$	13	3·1
$8\frac{1}{4}$	13	10·5	$1\frac{7}{8}$	3	14·1	$6\frac{1}{2}$	13	7·2
$8\frac{3}{8}$	13	13·9	2	4	2·2	$6\frac{5}{8}$	13	11·4
$8\frac{1}{2}$	14	1·2	$2\frac{1}{8}$	4	6·3	$6\frac{3}{4}$	13	15·5
$8\frac{5}{8}$	14	4·5	$2\frac{1}{4}$	4	10·5	$6\frac{7}{8}$	14	3·7
$8\frac{3}{4}$	14	7·8	$2\frac{3}{8}$	4	14·6	7	14	7·8
$8\frac{7}{8}$	14	11·1	$2\frac{1}{2}$	5	2·8	$7\frac{1}{8}$	14	11·9

15	8.4
7 $\frac{1}{2}$	15 12.5
7 $\frac{3}{4}$	16 0.6
7 $\frac{1}{2}$	16 4.8
8	16 8.9
8 $\frac{1}{2}$	16 13.1
8 $\frac{1}{2}$	17 1.2
8 $\frac{1}{2}$	17 5.3
8 $\frac{1}{2}$	17 9.5
8 $\frac{1}{2}$	17 13.6
8 $\frac{3}{4}$	18 1.8
8 $\frac{3}{4}$	18 5.9
9	18 10.0
9 $\frac{1}{2}$	18 14.2
9 $\frac{1}{2}$	19 2.3
9 $\frac{1}{2}$	19 6.5
9 $\frac{1}{2}$	19 10.6
9 $\frac{1}{2}$	19 14.7
9 $\frac{3}{4}$	20 2.9
9 $\frac{3}{4}$	20 7.0
0	20 11.2
0 $\frac{1}{2}$	20 15.3
0 $\frac{1}{2}$	21 3.4
0 $\frac{1}{2}$	21 7.6
0 $\frac{1}{2}$	21 11.7
0 $\frac{1}{2}$	21 15.9
0 $\frac{1}{2}$	22 4.0

4

1 $\frac{1}{2}$	3 11.6
1 $\frac{1}{2}$	4 0.5
1 $\frac{1}{2}$	4 5.5
1 $\frac{1}{2}$	4 10.5
2	4 15.4
2 $\frac{1}{2}$	5 4.4
2 $\frac{1}{2}$	5 9.4
2 $\frac{1}{2}$	5 14.3
2 $\frac{1}{2}$	6 3.3
2 $\frac{1}{2}$	6 8.3
2 $\frac{1}{2}$	6 13.2
2 $\frac{1}{2}$	7 2.2
3	7 7.2
3 $\frac{1}{2}$	7 12.2
3 $\frac{1}{2}$	8 1.1
3 $\frac{1}{2}$	8 6.1
3 $\frac{1}{2}$	8 11.1
3 $\frac{1}{2}$	9 0.0
3 $\frac{1}{2}$	9 5.0
3 $\frac{1}{2}$	9 10.0
4	9 14.9
4 $\frac{1}{2}$	10 3.9
4 $\frac{1}{2}$	10 8.9
4 $\frac{1}{2}$	10 13.8
4 $\frac{1}{2}$	11 2.8
4 $\frac{1}{2}$	11 7.8

0	14
6 $\frac{1}{2}$	15
6 $\frac{1}{2}$	15
6 $\frac{1}{2}$	15
6 $\frac{1}{2}$	16
6 $\frac{1}{2}$	16
6 $\frac{1}{2}$	16
6 $\frac{1}{2}$	17
7	17
7 $\frac{1}{2}$	17
7 $\frac{1}{2}$	18
7 $\frac{1}{2}$	18
7 $\frac{1}{2}$	18
7 $\frac{1}{2}$	18
7 $\frac{1}{2}$	19
8	19
8 $\frac{1}{2}$	20
8 $\frac{1}{2}$	20
8 $\frac{1}{2}$	20
8 $\frac{1}{2}$	21
8 $\frac{1}{2}$	21
8 $\frac{1}{2}$	21
9	22
9 $\frac{1}{2}$	22
9 $\frac{1}{2}$	22

Thick.	Broad.	qrs. lbs. oz.	Thick.	Broad.	lbs. oz.	Thick.	Broad.	qrs. lbs. oz.
in.	in.		in.	in.		in.	in.	
$\frac{1}{4}$	$10\frac{3}{8}$	0 25 12·3	$\frac{1}{4}$	$4\frac{1}{2}$	13 0·6	$\frac{1}{4}$	$9\frac{1}{8}$	0 26 7·1
	$10\frac{1}{2}$	0 26 1·3		$4\frac{3}{8}$	13 6·4		$9\frac{1}{4}$	0 26 12·9
	$10\frac{3}{4}$	0 26 6·2		$4\frac{1}{2}$	13 12·2		$9\frac{3}{8}$	0 27 2·7
	$10\frac{5}{8}$	0 26 11·2		$4\frac{7}{8}$	14 2·0		$9\frac{1}{2}$	0 27 8·5
	$10\frac{3}{4}$	0 27 0·2		5	14 7·8		$9\frac{5}{8}$	0 27 14·3
	11	0 27 5·1		$5\frac{1}{8}$	14 13·6		$9\frac{3}{4}$	1 0 4·0
	$11\frac{1}{8}$	0 27 10·1		$5\frac{1}{4}$	15 3·4		$9\frac{7}{8}$	1 0 9·8
	$11\frac{1}{4}$	0 27 15·1		$5\frac{3}{8}$	15 9·2	10	10	1 0 15·6
	$11\frac{3}{8}$	1 0 4·0		$5\frac{1}{2}$	15 15·0	$10\frac{1}{8}$	$10\frac{1}{8}$	1 1 5·4
	$11\frac{1}{2}$	1 0 9·0		$5\frac{5}{8}$	16 4·8	$10\frac{1}{4}$	$10\frac{1}{4}$	1 1 11·2
	$11\frac{3}{4}$	1 0 14·0		$5\frac{3}{4}$	16 10·6	$10\frac{3}{8}$	$10\frac{3}{8}$	1 2 1·0
	$11\frac{5}{8}$	1 1 3·0		$5\frac{7}{8}$	17 0·4	$10\frac{1}{2}$	$10\frac{1}{2}$	1 2 6·8
	$11\frac{3}{4}$	1 1 7·9		6	17 6·2	$10\frac{3}{4}$	$10\frac{3}{4}$	1 2 12·6
	12	1 1 12·9		$6\frac{1}{8}$	17 12·0	$10\frac{5}{8}$	$10\frac{5}{8}$	1 3 2·4
				$6\frac{1}{4}$	18 1·8	$10\frac{3}{4}$	$10\frac{3}{4}$	1 3 8·2
$\frac{1}{2}$	$1\frac{3}{8}$	0 5 1·1		$6\frac{3}{8}$	18 7·6	11	11	1 3 14·0
	$1\frac{1}{2}$	0 5 6·9		$6\frac{1}{2}$	18 13·4	$11\frac{1}{8}$	$11\frac{1}{8}$	1 4 3·8
	2	0 5 12·7		$6\frac{5}{8}$	19 3·1	$11\frac{1}{4}$	$11\frac{1}{4}$	1 4 9·6
	$2\frac{1}{8}$	0 6 2·5		$6\frac{3}{4}$	19 8·9	$11\frac{3}{8}$	$11\frac{3}{8}$	1 4 15·4
	$2\frac{1}{4}$	0 6 8·3		$6\frac{7}{8}$	19 14·7	$11\frac{1}{2}$	$11\frac{1}{2}$	1 5 5·2
	$2\frac{3}{8}$	0 6 14·1		7	20 4·5	$11\frac{5}{8}$	$11\frac{5}{8}$	1 5 11·0
	$2\frac{1}{2}$	0 7 3·9		$7\frac{1}{8}$	20 10·3	$11\frac{3}{4}$	$11\frac{3}{4}$	1 6 0·8
	$2\frac{5}{8}$	0 7 9·7		$7\frac{1}{4}$	21 0·1	$11\frac{7}{8}$	$11\frac{7}{8}$	1 6 6·6
	$2\frac{3}{4}$	0 7 15·5		$7\frac{3}{8}$	21 5·9	12	12	1 6 12·4
	$2\frac{7}{8}$	0 8 5·3		$7\frac{1}{2}$	21 11·7			
	3	0 8 11·1		$7\frac{5}{8}$	22 1·5	1	2	0 6 10·0
	$3\frac{1}{8}$	0 9 0·9		$7\frac{3}{4}$	22 7·3	$2\frac{1}{8}$	$2\frac{1}{8}$	0 7 0·6
	$3\frac{1}{4}$	0 9 6·7		$7\frac{7}{8}$	22 13·1	$2\frac{1}{4}$	$2\frac{1}{4}$	0 7 7·2
	$3\frac{3}{8}$	0 9 12·4		8	23 2·9	$2\frac{3}{8}$	$2\frac{3}{8}$	0 7 13·8
	$3\frac{1}{2}$	0 10 2·2		$8\frac{1}{8}$	23 8·7	$2\frac{1}{2}$	$2\frac{1}{2}$	0 8 4·4
	$3\frac{5}{8}$	0 10 8·0		$8\frac{1}{4}$	23 14·5	$2\frac{5}{8}$	$2\frac{5}{8}$	0 8 11·1
	$3\frac{3}{4}$	0 10 13·8		$8\frac{3}{8}$	24 4·3	$2\frac{3}{4}$	$2\frac{3}{4}$	0 9 1·7
	$3\frac{7}{8}$	0 11 3·6		$8\frac{1}{2}$	24 10·1	$2\frac{7}{8}$	$2\frac{7}{8}$	0 9 8·3
	4	0 11 9·4		$8\frac{5}{8}$	24 15·9	3	3	0 9 14·7
	$4\frac{1}{8}$	0 11 15·2		$8\frac{3}{4}$	25 5·7	$3\frac{1}{8}$	$3\frac{1}{8}$	0 10 5·6
	$4\frac{1}{4}$	0 12 5·0		$8\frac{7}{8}$	25 11·5	$3\frac{1}{4}$	$3\frac{1}{4}$	0 10 12·2
	$4\frac{3}{8}$	0 12 10·8		9	26 1·3	$3\frac{3}{8}$	$3\frac{3}{8}$	0 11 2·8

$3\frac{3}{8}$	12	6·7	$6\frac{3}{8}$	0	21	15·0	$9\frac{1}{2}$	1
$3\frac{1}{2}$	12	13·3	$6\frac{1}{2}$	0	22	5·7	$9\frac{3}{8}$	1
4	13	3·9	$6\frac{7}{8}$	0	22	12·3	$9\frac{1}{4}$	1
$4\frac{1}{8}$	13	10·6	7	0	23	2·9	$9\frac{7}{8}$	1
$4\frac{1}{4}$	14	1·2	$7\frac{1}{8}$	0	23	9·5	10	1
$4\frac{3}{8}$	14	7·8	$7\frac{1}{4}$	0	24	0·2	$10\frac{1}{8}$	1
$4\frac{1}{2}$	14	14·4	$7\frac{3}{8}$	0	24	6·6	$10\frac{1}{4}$	1
$4\frac{5}{8}$	15	5·0	$7\frac{1}{2}$	0	24	13·4	$10\frac{3}{8}$	1
$4\frac{3}{4}$	15	11·7	$7\frac{5}{8}$	0	25	4·0	$10\frac{1}{2}$	1
$4\frac{7}{8}$	16	2·3	$7\frac{3}{4}$	0	25	10·6	$10\frac{3}{4}$	1
5	16	8·9	$7\frac{7}{8}$	0	26	1·3	$10\frac{7}{8}$	1
$5\frac{1}{8}$	16	15·5	8	0	26	7·9	$10\frac{7}{4}$	1
$5\frac{1}{4}$	17	6·2	$8\frac{1}{8}$	0	26	14·5	11	1
$5\frac{3}{8}$	17	12·8	$8\frac{1}{4}$	0	27	5·1	$11\frac{1}{8}$	1
$5\frac{1}{2}$	18	3·4	$8\frac{3}{8}$	0	27	11·8	$11\frac{1}{4}$	1
$5\frac{5}{8}$	18	10·0	$8\frac{1}{2}$	1	0	2·4	$11\frac{3}{8}$	1
$5\frac{3}{4}$	19	0·7	$8\frac{5}{8}$	1	0	9·0	$11\frac{1}{2}$	1
6	19	7·3	$8\frac{3}{4}$	1	0	15·6	$11\frac{5}{8}$	1
$6\frac{1}{8}$	19	13·9	$8\frac{7}{8}$	1	1	6·3	$11\frac{3}{4}$	1
$6\frac{1}{4}$	20	4·5	9	1	1	12·9	$11\frac{7}{8}$	1
$6\frac{3}{8}$	20	11·2	$9\frac{1}{8}$	1	2	3·5	12	1

Thick.	Broad.	qrs. lbs. oz.			Thick.	Broad.	qrs. lbs. oz.			Thick.	Broad.	qrs. lbs. oz.		
n. $\frac{1}{4}$	in.				n. $\frac{1}{4}$	in.				n. $\frac{1}{4}$	in.			
	2 $\frac{1}{4}$	0	8	6.1		11 $\frac{1}{4}$	1	14	13.5		10 $\frac{1}{4}$	1	16	8.0
	2 $\frac{1}{2}$	0	9	5.0		11 $\frac{1}{2}$	1	15	12.4		11	1	17	8.6
	2 $\frac{3}{4}$	0	10	3.9		12	1	16	11.4		11 $\frac{1}{4}$	1	18	9.2
	3	0	11	2.8							11 $\frac{1}{2}$	1	19	9.7
	3 $\frac{1}{4}$	0	12	1.7	1 $\frac{1}{4}$	2 $\frac{1}{4}$	0	10	5.6		11 $\frac{3}{4}$	1	20	10.3
	3 $\frac{1}{2}$	0	13	0.6		2 $\frac{1}{2}$	0	11	6.1		12	1	21	10.8
	3 $\frac{3}{4}$	0	13	15.5		3	0	12	6.7					
	4	0	14	14.4		3 $\frac{1}{4}$	0	13	7.2	1 $\frac{3}{4}$	2 $\frac{1}{4}$	0	12	8.3
	4 $\frac{1}{4}$	0	15	13.3		3 $\frac{1}{2}$	0	14	7.8		3	0	13	10.6
	4 $\frac{1}{2}$	0	16	12.2		3 $\frac{3}{4}$	0	15	8.4		3 $\frac{1}{4}$	0	14	12.8
	4 $\frac{3}{4}$	0	17	11.1		4	0	16	8.9		3 $\frac{1}{2}$	0	15	15.0
	5	0	18	10.0		4 $\frac{1}{4}$	0	17	9.5		3 $\frac{3}{4}$	0	17	1.2
	5 $\frac{1}{4}$	0	19	8.9		4 $\frac{1}{2}$	0	18	10.0		4	0	18	3.4
	5 $\frac{1}{2}$	0	20	7.8		4 $\frac{3}{4}$	0	19	10.6		4 $\frac{1}{4}$	0	19	5.6
	5 $\frac{3}{4}$	0	21	6.8		5	0	20	11.2		4 $\frac{1}{2}$	0	20	7.8
	6	0	22	5.7		5 $\frac{1}{4}$	0	21	11.7		4 $\frac{3}{4}$	0	21	10.1
	6 $\frac{1}{4}$	0	23	4.6		5 $\frac{1}{2}$	0	22	12.3		5	0	22	12.3
	6 $\frac{1}{2}$	0	24	3.5		5 $\frac{3}{4}$	0	23	12.8		5 $\frac{1}{4}$	0	23	14.5
	6 $\frac{3}{4}$	0	25	2.4		6	0	24	13.4		5 $\frac{1}{2}$	0	25	0.7
	7	0	26	1.3		6 $\frac{1}{4}$	0	25	14.0		5 $\frac{3}{4}$	0	26	2.9
	7 $\frac{1}{4}$	0	27	0.2		6 $\frac{1}{2}$	0	26	14.5		6	0	27	5.1
	7 $\frac{1}{2}$	0	27	15.1		6 $\frac{3}{4}$	0	27	15.1		6 $\frac{1}{4}$	1	0	7.4
	7 $\frac{3}{4}$	1	0	14.0		7	1	0	15.6		6 $\frac{1}{2}$	1	1	9.6
	8	1	1	12.9		7 $\frac{1}{4}$	1	2	0.2		6 $\frac{3}{4}$	1	2	11.8
	8 $\frac{1}{4}$	1	2	11.8		7 $\frac{1}{2}$	1	3	0.8		7	1	3	14.0
	8 $\frac{1}{2}$	1	3	10.7		7 $\frac{3}{4}$	1	4	1.3		7 $\frac{1}{4}$	1	5	0.2
	8 $\frac{3}{4}$	1	4	9.6		8	1	5	1.9		7 $\frac{1}{2}$	1	6	2.4
	9	1	5	8.5		8 $\frac{1}{4}$	1	6	2.4		7 $\frac{3}{4}$	1	7	4.7
	9 $\frac{1}{4}$	1	6	7.4		8 $\frac{1}{2}$	1	7	3.0		8	1	8	6.9
	9 $\frac{1}{2}$	1	7	6.3		8 $\frac{3}{4}$	1	8	3.6		8 $\frac{1}{4}$	1	9	9.1
	9 $\frac{3}{4}$	1	8	5.2		9	1	9	4.1		8 $\frac{1}{2}$	1	10	11.3
	10	1	9	4.1		9 $\frac{1}{4}$	1	10	4.7		8 $\frac{3}{4}$	1	11	13.5
	10 $\frac{1}{4}$	1	10	3.0		9 $\frac{1}{2}$	1	11	5.2		9	1	12	15.7
	10 $\frac{1}{2}$	1	11	1.9		9 $\frac{3}{4}$	1	12	5.8		9 $\frac{1}{4}$	1	14	2.0
	10 $\frac{3}{4}$	1	12	0.8	10	1	13	6.4		9 $\frac{1}{2}$	1	15	4.2	
	11	1	12	15.7	10 $\frac{1}{4}$	1	14	6.9		9 $\frac{3}{4}$	1	16	6.4	
	11 $\frac{1}{4}$	1	13	14.6	10 $\frac{1}{2}$	1	15	7.5		10	1	17	8.6	

5	1	14	13.5	7	2	1	0.4	9	9
6	1	16	11.4	7	2	2	15.9	9	9
6	1	18	9.2	7	2	4	15.3	9	9
6	1	20	7.0	8	2	6	14.8	10	10
6	1	22	4.8	8	2	8	14.3	10	10
7	1	24	2.6	8	2	10	13.7	10	10
7	1	26	0.4	8	2	12	13.2	10	10
7	1	27	14.2	9	2	14	12.7	11	11
7	2	1	12.0	9	2	16	12.1	11	11
8	2	3	9.8	9	2	18	11.6	11	11
8	2	5	7.6	9	2	20	11.1	11	11
8	2	7	5.4	10	2	22	10.5	11	11
8	2	9	3.2	10	2	24	10.0	12	12
9	2	11	1.0	10	2	26	9.4	2	5
9	2	12	14.9	10	3	0	8.9	5	5
9	2	14	12.7	11	3	2	8.4	5	5
9	2	16	10.5	11	3	4	7.8	6	6
10	2	18	8.3	11	3	6	7.3	6	6
10	2	20	6.1	11	3	8	6.8	6	6
10	2	22	3.9	12	3	10	6.2	6	6
10	2	24	1.7	2	5	1	13	6.4	7
11	2	25	15.5	5	1	15	7.5	7	7
11	2	27	13.3	5	1	17	8.6	7	7
11	3	1	11.1	5	1	19	9.7	7	7
11	3	3	8.9	6	1	21	10.8	8	8
12	3	5	6.7	6	1	23	12.0	8	8
4	1	9	5.8	6	1	25	13.1	8	8
5	1	11	5.2	6	1	27	14.2	9	9
5	1	12	4.7	7	2	1	15.3	9	9

respective thickness of each bar. Hence to
of any length of a bar of rectangular iron
ascertained simply, as follows :

Rule.—Multiply the tabular weight, acc
the thickness and breadth, by the number
the bar, the product will be the weight requ

Example.—In a bar of iron whose thick
inches, the breadth $6\frac{1}{4}$ inches, and the leng
what is the weight thereof?

In the Table for $2\frac{1}{2}$ inches thick, and of
inches, stand 2qrs. 2lbs. 10·9oz., being t
of one lineal foot. Multiply this number b
and we have as follows :

cwt.	qrs.	lbs.	oz.	
0	2	2	10·9	
				$6 \times 3 = 18$
<hr/>				
3	0	16	1·4	
			3	
<hr/>				
9	1	20	4·2	Answer.

The foregoing Table of weights is obtai
following approximate rule :

Multiply the area of the end of the
length of one foot, and multiply that produ
product will be the weight in pounds :

Incl	qrs.	lbs.	ozs.	In	qrs.	lbs.	ozs.	In	qrs.	lbs.	ozs.
1	0	0	0.4	4	1	16	4.1	8	6	3	
1	0	0	2.6	4	1	18	15.8	8	6	8	
1	0	0	5.8	4	1	21	12.6	8	6	14	
1	0	0	10.4	4	1	24	10.8	8	6	19	
1	0	1	0.1	4	1	27	10.2	8	6	25	
1	0	1	7.3	4	2	2	11.0	8	7	3	
1	0	1	15.8	4	2	5	13.1	8	7	8	
1	0	2	9.4	5	2	3	0.6	9	7	14	
1	0	3	4.8	5	2	12	5.2	9	7	20	
1	0	4	1.1	5	2	15	11.0	9	7	26	
1	0	4	14.7	5	2	19	2.4	9	8	4	
1	0	5	13.7	5	2	22	11.0	9	8	10	
1	0	6	13.9	5	2	26	4.8	9	8	16	
1	0	7	15.5	5	3	2	0.1	9	8	22	
1	0	9	2.4	5	3	5	12.6	9	9		
2	0	10	6.5	6	3	9	10.4	10	9		
2	0	11	12.0	6	3	13	8.6	10	9	1	
2	0	13	1.7	6	3	17	9.0	10	9	2	
2	0	14	10.7	6	3	21	10.6	10	9	2	
2	0	16	4.1	6	3	25	13.6	10	10		
2	0	17	14.8	6	4	2	1.8	10	10		
2	0	19	9.6	6	4	6	7.4	10	10		
2	0	21	8.0	6	4	11	1.4	10	10		
3	0	23	6.5	7	4	15	6.4	11	11		
3	0	25	6.4	7	4	19	15.5	11	11		
3	0	27	7.6	7	4	24	10.6	11	11		
3	1	1	10.0	7	5	1	6.7	11	12		
3	1	3	13.9	7	5	6	4.0	11	12		

The Tables of the weight of round and square malleable iron have been obtained by the following approximate rules :

Rule 1.—For round bars. Multiply the square of the diameter in inches by the length in feet, the product by 2·6. The product will be the weight in pounds avoirdupois, nearly.

Rule 2.—For square bars. Multiply the side of the bar in inches by the length in feet, and that by 3·32. The product will be the weight in pounds avoirdupois, nearly.

Example 1.—What is the weight of a round malleable iron $4\frac{1}{2}$ feet long, and $2\frac{1}{4}$ inches diameter?

$$2\cdot25^2 \times 4\cdot5 = 22\cdot78125 \times 2\cdot6 = 59\cdot23125 \text{ lbs.} = 59 \text{ lbs.}$$

Example 2.—Required the weight of a square malleable iron whose length is $7\frac{1}{4}$ feet, and 1 inch square.

$$1\cdot5^2 \times 7\cdot25 = 16\cdot8125 \times 3\cdot32 = 54\cdot1575 \text{ lbs.} = 54 \text{ lbs.}$$

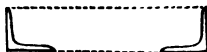
	5 5 5 5	5 6 6 7		6 6 6	8 9 9		8 8 0	0
1 11 1 1 1 1 1 1 1	5 5 5 5 5 5 5	7 7 8 8 8 9 9	2 4 1 1 1 1 1 1 1	6 6 6 6 6 6 7 7	10 10 10 11 11 11 0 0	2 9 1 1 1 1 1 1 1	8 8 8 8 8 8 8 8	0 1 1 1 2 2 2 2
2 0 1 1 1 1 1 1 1	5 5 5 5 5 6 6 6	10 10 11 11 11 0 0 0	2 5 1 1 1 1 1 1 1	7 7 7 7 7 7 7 7	1 1 1 2 2 2 3 3	2 10 1 1 1 1 1 1 1	8 8 8 8 8 8 8 8	0 1 1 1 1 1 1 1
2 1 1 1 1 1 1 1	6 6 6 6 6 6 6	1 1 2 2 2 3 3	2 6 1 1 1 1 1 1 1	7 7 7 7 7 7 7 7	3 4 4 5 5 6 6 6	2 11 1 1 1 1 1 1 1	8 8 8 8 8 8 8 8	0 1 1 1 1 1 1 1

号 子 音	15 15	3 4	号 子 音	10 16	0 1	号 子 音	16 16	9 9
5 3	15	4 $\frac{1}{2}$	5 6	16	1 $\frac{1}{2}$	5 9	16	10 $\frac{1}{2}$
音	15	5	音	16	1 $\frac{1}{2}$	音	16	10 $\frac{1}{2}$
音	15	5 $\frac{1}{2}$	音	16	2 $\frac{1}{2}$	音	16	10 $\frac{1}{2}$
音	15	5 $\frac{3}{4}$	音	16	2 $\frac{1}{2}$	音	16	11 $\frac{1}{2}$
音	15	6 $\frac{1}{2}$	音	16	2 $\frac{1}{2}$	音	16	11 $\frac{1}{2}$
音	15	6 $\frac{1}{2}$	音	16	3 $\frac{1}{2}$	音	17	0
音	15	6 $\frac{1}{2}$	音	16	3 $\frac{1}{2}$	音	17	0 $\frac{1}{2}$
音	15	7 $\frac{1}{2}$	音	16	4	音	17	0 $\frac{1}{2}$
5 4	15	7 $\frac{1}{2}$	5 7	16	4 $\frac{1}{2}$			
音	15	7 $\frac{1}{2}$	音	16	4 $\frac{1}{2}$			
音	15	8 $\frac{1}{2}$	音	16	5 $\frac{1}{2}$			
音	15	8 $\frac{1}{2}$	音	16	5 $\frac{1}{2}$			
音	15	9	音	16	5 $\frac{1}{2}$			
音	15	9 $\frac{1}{2}$	音	16	6 $\frac{1}{2}$			
音	15	9 $\frac{1}{2}$	音	16	6 $\frac{1}{2}$			
音	15	10 $\frac{1}{2}$	音	16	6 $\frac{1}{2}$			

	12 12 12	12 2 $\frac{1}{2}$ 2 $\frac{1}{2}$		13 13	7 $\frac{1}{2}$ 7 $\frac{1}{2}$		15 15	0 $\frac{1}{2}$ 1
7	12 12 12 12 12 12 12	3 $\frac{1}{2}$ 3 $\frac{1}{2}$ 4 $\frac{1}{2}$ 4 $\frac{1}{2}$ 4 $\frac{1}{2}$ 5 $\frac{1}{2}$ 5 $\frac{1}{2}$ 6 $\frac{1}{2}$	4 0	13 13 13 13 13 13 13 13	8 $\frac{1}{2}$ 8 $\frac{1}{2}$ 9 $\frac{1}{2}$ 9 $\frac{1}{2}$ 10 10 $\frac{1}{2}$ 10 $\frac{1}{2}$ 11 $\frac{1}{2}$	4 5	15 15 15 15 15 15 15 15	1 $\frac{1}{2}$ 1 $\frac{1}{2}$ 2 $\frac{1}{2}$ 2 $\frac{1}{2}$ 3 $\frac{1}{2}$ 3 $\frac{1}{2}$ 4 4 $\frac{1}{2}$
3 8	12 12 12 12 12 12 12	6 $\frac{1}{2}$ 7 7 $\frac{1}{2}$ 7 $\frac{1}{2}$ 8 $\frac{1}{2}$ 8 $\frac{1}{2}$ 9 $\frac{1}{2}$ 9 $\frac{1}{2}$	4 1	13 14 14 14 14 14 14 14	11 $\frac{1}{2}$ 0 $\frac{1}{2}$ 0 $\frac{1}{2}$ 1 1 $\frac{1}{2}$ 1 $\frac{1}{2}$ 2 $\frac{1}{2}$ 2 $\frac{1}{2}$	4 6	15 15 15 15 15 15 15 15	4 $\frac{1}{2}$ 5 $\frac{1}{2}$ 5 $\frac{1}{2}$ 6 $\frac{1}{2}$ 6 $\frac{1}{2}$ 7 7 7
3 9	12 12 12 12 12 13 13 13	10 10 $\frac{1}{2}$ 10 $\frac{1}{2}$ 11 $\frac{1}{2}$ 11 $\frac{1}{2}$ 0 $\frac{1}{2}$ 0 $\frac{1}{2}$ 1	4 2	14 14 14 14 14 14 14 14	3 $\frac{1}{2}$ 3 $\frac{1}{2}$ 4 4 $\frac{1}{2}$ 4 $\frac{1}{2}$ 5 $\frac{1}{2}$ 5 $\frac{1}{2}$ 6 $\frac{1}{2}$	4 7	15 15 15 15 15 15 15 15	8 8 9 9 10 1 1 1

breadth of the angle must be taken from the diameter,—for this reason, that the diameter is from outside to outside of the ring, as in the following sectional figure :

12 inches outside.



2½ in.

Suppose a ring is to be made of iron whose diameter outside is to be 12 inches, breadth of the angle 2½ inches; then, by subtracting the breadth of the angle from 12 inches, we have left 9 inches. Looking into the Table in the column of diameters, we find in the circumference column, opposite 9 inches, 2 feet 8½ inches, which is the length of iron necessary for the ring.

It has been already observed, that between wrought and plain iron a considerable difference exists in regard to the proportion of the circumference to the diameter: this is owing to the angle or flange of the bar, and when the iron is formed into a hoop it contracts more or less, as the diameter is taken inside or outside of the hoop.

Ex. Required the circumference of a hoop, whose axes are $18\frac{1}{2}$ and 13 inches, the thickness of the iron being $2\frac{1}{4}$ inches. (*Table*

$$\begin{array}{r}
 18\frac{1}{2} \\
 13 \\
 \hline
 2)31\frac{1}{2} \\
 \hline
 15\frac{3}{4} \\
 + 2\frac{1}{4} \text{ thickness.} \\
 \hline
 18\frac{1}{4} \text{ inches, the diameter.}
 \end{array}$$

Entering into the Table of Diameters, 18 inches, the circumference will be found $9\frac{1}{4}$ inches.

In constructing elliptical hoops of iron with the angle outside, reference must be made to the Tables for hoops of angled iron: the result will be similar to the above example. where the angle is inside, the thickness must be taken from half the sum of the

Note.—It must be observed, that in the Examples given in the Observations on Table I., the hoops formed of angled iron, that the thicknesses are nothing more than the end

unit being that of a common sheet, so designed, 4 feet by 2 feet, in lbs.; thus,

A 70lb plate is $\frac{1}{16}$ th of an inch in thickness.

46½	"	$\frac{1}{8}$	"
23	"	$\frac{1}{16}$	"
11½	"	$\frac{1}{32}$	"
6	"	$\frac{1}{64}$	&c., &c.

The thickness of lead is also in common determined by the weight, the unit being the square or superficial foot; thus,

4-lb lead is $\frac{1}{16}$ th of an inch in thickness.

6	"	$\frac{1}{10}$	"
7½	"	$\frac{1}{8}$	"
11	"	$\frac{3}{16}$	"
15	"	$\frac{1}{2}$	"

COMPARATIVE WEIGHTS OF DIFFERENT MATERIALS

Bar iron being 1.	Cast iron being 1.	Dry deal being 1.
Cast iron = .95	Bar iron = 1.07	Cast iron =
Steel = 1.02	Steel = 1.08	Cast tin =
Copper = 1.16	Brass = 1.16	Brass =
Brass = 1.09	Copper = 1.21	Copper =
Lead = 1.48	Lead = 1.56	Lead =

1. Suppose I have an article of plate iron, the

METALS, AND ANY DIAMETER REQUIRE

Thickness in parts of an inch.	Wrought iron.	Copper.	Lead.
$\frac{1}{8}$	·326	11 $\frac{1}{2}$ lbs. plate ·38	2 lbs. lead
$\frac{1}{16}$	·653	23 $\frac{1}{2}$ " ·76	4 "
$\frac{3}{32}$	·976	35 " 1·14	5 $\frac{1}{2}$ "
$\frac{1}{8}$	1·3	46 $\frac{1}{2}$ " 1·52	8 "
$\frac{5}{32}$	1·627	58 " 1·9	9 $\frac{1}{4}$ "
$\frac{3}{16}$	1·95	70 " 2·28	11 "
$\frac{7}{32}$	2·277	80 $\frac{1}{2}$ " 2·66	13 "
$\frac{1}{2}$	2·6	93 " 3·04	15 "

Rule.—To the interior diameter of the pipe in inches, add the thickness of the metal; multiply the sum by the decimal numbers opposite the name of the metal's name; also multiply the length of the pipe in feet, and the product will be the weight of the pipe in lbs.

1. Required the weight of a copper pipe whose interior diameter is 7 $\frac{1}{2}$ inches, its length 6 $\frac{1}{4}$ feet, and the metal $\frac{1}{8}$ of an inch in thickness.

$$7\cdot5 + \cdot125 = 7\cdot625 \times 1\cdot52 \times 6\cdot25 = 72\cdot4 \text{ lbs.}$$

2. What is the weight of a leaden pipe 18 $\frac{1}{2}$ feet long, whose interior diameter is 4 inches, and the metal $\frac{1}{4}$ of an inch in thickness.

MEASURE OF TIMBER.

1. Flat or Board Measure.

Breadth in inches.	Area of a lineal foot.	Breadth in inches.	Area of a lineal foot.	Breadth in inches.	Area lineal
$\frac{1}{2}$	·0208	4	·3334	8	·6667
$\frac{3}{4}$	·0417	$4\frac{1}{2}$	·3542	$8\frac{1}{2}$	·6875
$\frac{5}{8}$	·0625	$4\frac{3}{4}$	·375	$8\frac{3}{4}$	·7083
1	·0834	$4\frac{7}{8}$	·3958	$8\frac{7}{8}$	·7292
$1\frac{1}{4}$	·1042	5	·4167	9	·75
$1\frac{1}{2}$	·125	$5\frac{1}{4}$	·4375	$9\frac{1}{4}$	·7708
$1\frac{3}{4}$	·1459	$5\frac{1}{2}$	·4583	$9\frac{1}{2}$	·7917
2	·1667	$5\frac{3}{4}$	·4792	$9\frac{3}{4}$	·8125
$2\frac{1}{4}$	·1875	6	·5	10	·8333
$2\frac{1}{2}$	·2084	$6\frac{1}{4}$	·5208	$10\frac{1}{4}$	·8542
$2\frac{3}{4}$	·2292	$6\frac{1}{2}$	·5416	$10\frac{1}{2}$	·875
3	·25	$6\frac{3}{4}$	·5625	$10\frac{3}{4}$	·8958
$3\frac{1}{4}$	·2708	7	·5833	11	·9167
$3\frac{1}{2}$	·2916	$7\frac{1}{4}$	·6042	$11\frac{1}{4}$	·9375
$3\frac{3}{4}$	·3125	$7\frac{1}{2}$	·625	$11\frac{1}{2}$	·9583
		$7\frac{3}{4}$	·6458	$11\frac{3}{4}$	·9792

Application and Use of the Table.

1. Required the number of square feet in a
or plank $16\frac{1}{2}$ feet in length and $9\frac{3}{4}$ inches in br

Opposite $9\frac{3}{4}$ is $\cdot 8125 \times 16\cdot 5 = 13\cdot 4$ square feet.

or $16\cdot 5$ feet in length and $9\frac{3}{4}$ inches in breadth and

in dimensions —

Suppose the mean $\frac{1}{4}$ girth of a tree 21 $\frac{1}{4}$ in
its length 16 feet, what are its contents in
cubic feet?

$$3.136 \times 16 = 50.176 \text{ cubic feet.}$$

Battens, Deals, and Planks, as imported into
this country, are each similar in their various lengths
differing in their widths and thicknesses, and their
principal distinction: thus, a batten is 7
by 2 $\frac{1}{2}$,—a deal 9 by 3,—and a plank 11 by 3,—
being what are termed the standard dimensions
which they are bought and sold, the length
being taken at 12 feet; therefore, in estimating
the proper value of any quantity, nothing more
is required than their lineal dimensions, by which to
ascertain the number of times 12 feet there are in the
whole.

Suppose I wish to purchase the following:

7 of	6 feet	6 × 7 = 42 feet
5 "	14 "	14 × 5 = 70 "
11 "	19 "	19 × 11 = 209 "
and 6 "	21 "	21 × 6 = 126 "

12)447(37.25 standard

2. Suppose I pay 31s. 6d. for three cwt or 1 what rate is that per ton? 1 ton = 20 cwt.

Set 3 upon B to 31.5 upon A; and against 20 upon 1 upon A.

RULE OF THREE INVERSE.

Rule.—Invert the slide, and the operation same as direct proportion.

1. I know that six men are capable of performing a certain given portion of work in eight days; what rate the same performed in three; how many must there be employed?

Set 6 upon C to 8 upon A; and against 3 upon C is 16

2. The lever of a safety-valve is 20 inches in and 5 inches between the fixed end and centre valve; what weight must there be placed on of the lever to equipoise a force or pressure of tending to raise the valve?

Set 5 upon C to 40 upon A; and against 20 on C is 1

3. If $8\frac{3}{4}$ yards of cloth, $1\frac{1}{2}$ yard in width sufficient quantity, how much will be required which is only $\frac{7}{8}$ ths in width, to effect the same

lbs. on c.

1. Required the cubic contents of a cylinder, length, and 10 inches quarter girt.

Set 30 upon B to 144 (the gauge-point) upon A
10 upon D is 20·75 feet upon C.

2. In a cylinder 9 inches in length, and diameter, how many cubic inches?

Set 9 upon B to 1273 (the gauge-point) upon A
7 on D is 346 inches on C.

3. What is the weight of a bar of cast iron square, and 6 feet long?

Set 6 upon B to 32 (the gauge-point) upon A;
upon D is 168 lbs. upon C.

By the common rule.

4. Required the weight of a cylinder iron 10 inches long, and 5½ diameter.

Set 10 upon B to 283 (G. P.) upon A; and
D is 66·65 lbs. on C.

5. What is the weight of a dry rope 2 and 4 inches circumference?

Set 25 upon B to 47 (G. P.) upon A; and
53·16 lbs. on C.

What is the weight of a short-link

23 feet in length and 37 in width.

Set 1 upon B to 23 upon A; and against 126.5 square feet upon A.

If 5 square feet of boiler surface be each horse-power, how many horses' power is the boiler equal to?

Set 5 upon B to 126.5 upon A; and again 25.5 upon A.

EQUIVALENT PRICES TO CEMENT

in lbs.	cwt. or 112 lbs.		qr. or 28 lbs.		stone or 14 lbs.		lb. or 1.	doz. or 12.		score or 20.		per 100.		per 12
	L.	S.	D.	L.	S.	D.	D.	S.	D.	S.	D.	L.	S.	D.
8	0	2	4	0	0	7	1	0	3	0	5	0	2	1
10	0	3	6	0	0	10½	0	4½	0	7½	0	3	1½	0
12	0	4	8	0	1	2	0	6	0	10	0	4	2	0
14	0	5	10	0	1	5½	0	7½	1	0½	0	5	2½	0
16	0	6	12	0	1	9	0	10½	1	3	0	6	3	0
18	0	7	14	0	2	0½	1	0½	1	5½	0	7	3½	0
20	0	8	16	0	2	4	1	1	1	8	0	8	4	0
22	0	9	18	0	2	7½	1	1½	1	10½	0	9	4½	0
24	0	10	20	0	3	1	1	2	1	12	0	10	5	0
26	0	11	22	0	3	2½	1	2½	2	14	0	11	5½	0
28	0	12	24	0	3	6	1	3	2	16	0	12	6	0
30	0	13	26	0	3	9½	1	3½	2	18	0	13	6½	0
32	0	14	28	0	4	1	1	4	2	20	0	14	7	0
34	0	15	30	0	4	4½	2	4½	2	22	0	15	7½	0
36	0	16	32	0	4	8	2	5	3	24	0	16	8	0
38	0	17	34	0	4	11½	2	5½	3	26	0	17	8½	0
40	0	18	36	0	5	3	2	6	3	28	0	18	9	0
42	0	19	38	0	5	6½	2	6½	3	30	0	19	9½	0
44	0	20	40	0	5	10	2	7	4	32	0	20	10	0
46	0	21	42	0	5	13½	2	7½	4	34	0	21	10½	0
48	0	22	44	0	6	1	3	8	4	36	0	22	11	0
50	0	23	46	0	6	4½	3	8½	4	38	0	23	11½	0
52	0	24	48	0	6	8	3	9	4	40	0	24	12	0
54	0	25	50	0	6	11½	3	9½	5	42	0	25	12½	0
56	0	26	52	0	7	3	4	10	5	44	0	26	13	0
58	0	27	54	0	7	6½	4	10½	5	46	0	27	13½	0
60	0	28	56	0	7	10	4	11	5	48	0	28	14	0
62	0	29	58	0	8	1	5	11½	6	50	0	29	14½	0
64	0	30	60	0	8	4½	5	12	6	52	0	30	15	0
66	0	31	62	0	8	8	5	12½	6	54	0	31	15½	0
68	0	32	64	0	9	1	6	13	6	56	0	32	16	0
70	0	33	66	0	9	4½	6	13½	6	58	0	33	16½	0
72	0	34	68	0	9	8	6	14	6	60	0	34	17	0
74	0	35	70	0	10	1	7	14½	7	62	0	35	17½	0
76	0	36	72	0	10	4½	7	15	7	64	0	36	18	0
78	0	37	74	0	10	8	7	15½	7	66	0	37	18½	0
80	0	38	76	0	11	1	8	16	8	68	0	38	19	0
82	0	39	78	0	11	4½	8	16½	8	70	0	39	19½	0
84	0	40	80	0	12	3	9	17	8	72	0	40	20	0
86	0	41	82	0	12	6½	9	17½	9	74	0	41	20½	0
88	0	42	84	0	13	1	10	18	9	76	0	42	21	0
90	0	43	86	0	13	4½	10	18½	10	78	0	43	21½	0
92	0	44	88	0	13	8	10	19	10	80	0	44	22	0
94	0	45	90	0	14	1	11	19½	11	82	0	45	22½	0
96	0	46	92	0	14	4½	11	20	11	84	0	46	23	0
98	0	47	94	0	14	8	11	20½	11	86	0	47	23½	0
100	0	48	96	0	15	1	12	21	12	88	0	48	24	0
102	0	49	98	0	15	4½	12	21½	12	90	0	49	24½	0
104	0	50	100	0	15	8	12	22	12	92	0	50	25	0
106	0	51	102	0	16	1	13	22½	13	94	0	51	25½	0
108	0	52	104	0	16	4½	13	23	13	96	0	52	26	0
110	0	53	106	0	16	8	13	23½	13	98	0	53	26½	0
112	0	54	108	0	17	1	14	24	14	100	0	54	27	0
114	0	55	110	0	17	4½	14	24½	14	102	0	55	27½	0
116	0	56	112	0	17	8	14	25	14	104	0	56	28	0
118	0	57	114	0	18	1	15	25½	15	106	0	57	28½	0
120	0	58	116	0	18	4½	15	26	15	108	0	58	29	0
122	0	59	118	0	18	8	15	26½	15	110	0	59	29½	0
124	0	60	120	0	19	1	16	27	16	112	0	60	30	0
126	0	61	122	0	19	4½	16	27½	16	114	0	61	30½	0
128	0	62	124	0	19	8	16	28	16	116	0	62	31	0
130	0	63	126	0	20	1	17	28½	17	118	0	63	31½	0
132	0	64	128	0	20	4½	17	29	17	120	0	64	32	0
134	0	65	130	0	20	8	17	29½	17	122	0	65	32½	0
136	0	66	132	0	21	1	18	30	18	124	0	66	33	0
138	0	67	134	0	21	4½	18	30½	18	126	0	67	33½	0
140	0	68	136	0	21	8	18	31	18	128	0	68	34	0
142	0	69	138	0	22	1	19	31½	19	130	0	69	34½	0
144	0	70	140	0	22	4½	19	32	19	132	0	70	35	0
146	0	71	142	0	22	8	19	32½	19	134	0	71	35½	0
148	0	72	144	0	23	1	20	33	20	136	0	72	36	0
150	0	73	146	0	23	4½	20	33½	20	138	0	73	36½	0
152	0	74	148	0	23	8	20	34	20	140	0	74	37	0
154	0	75	150	0	24	1	21	34½	21	142	0	75	37½	0
156	0	76	152	0	24	4½	21	35	21	144	0	76	38	0
158	0	77	154	0	24	8	21	35½	21	146	0	77	38½	0
160	0	78	156	0	25	1	22	36	22	148	0	78	39	0
162	0	79	158	0	25	4½	22	36½	22	150	0	79	39½	0
164	0	80	160	0	25	8	22	37	22	152	0	80	40	0
166	0	81	162	0	26	1	23	37½	23	154	0	81	40½	0
168	0	82	164	0	26	4½	23	38	23	156	0	82	41	0
170	0	83	166	0	26	8	23	38½	23	158	0	83	41½	0
172	0	84	168	0	27	1	24	39	24	160	0	84	42	0
174	0	85	170	0	27	4½	24	39½	24	162	0	85	42½	0
176	0	86	172	0	27	8	24	40	24	164	0	86	43	0
178	0	87	174	0	28	1	25	40½	25	166	0	87	43½	0
180	0	88	176	0	28	4½	25	41	25	168	0	88	44	0
182	0	89	178	0	28	8	25	41½	25	170	0	89	44½	0
184	0	90	180	0	29	1	26	42	26	172	0	90	45	0
186	0	91	182	0	29	4½	26	42½	26	174	0	91	45½	0
188	0	92	184	0	29	8	26	43	26	176	0	92	46	0
190	0	93	186	0	30	1	27	43½	27	178	0	93	46½	0
192	0	94	188	0	30	4½	27	44	27	180	0	94	47	0
194	0	95	190	0	30	8	27	44½	27	182	0	95	47½	0
196	0	96	192	0	31	1	28	45	28	184	0	96	48	0
198	0	97	194	0	31	4½	28	45½	28	186	0	97	48½	0
200	0	98	196	0	31	8	28	46	28	188	0	98	49	0
202	0	99	198	0	32	1	29	46½	29	190	0	99	49½	0
204	0	100	200	0	32	4½	29	47	29	192	0	100	50	0
206	0	101	202	0	32	8	29	47½	29	194	0	101	50½	0
208	0	102	204	0	33	1	30	48	30	196	0	102	51	0
210	0	103	206	0	33	4½	30	48½	30	198	0	103	51½	0
212	0	104	208	0	33	8	30	49	30	200	0	104	52	0
214	0	105	210	0	34	1	31	49½	31	202	0	105	52½	0
216	0	106	212	0	34	4½	31	50	31	204	0	106	53	0
218	0	107	214	0	34	8	31	50½	31	206	0	107	53½	0
220	0	108	216	0	35	1	32	51	32	208	0	108	54	0
222	0	109	218	0	35	4½	32	51½	32	210	0	109	54½	0
224	0	110	220	0	35	8	32	52	32	212	0	110	55	0
226	0	111	222	0	36	1	33	52½	33	214	0	111	55½	0
228	0	112	224	0	36	4½	33	53	33	216	0	112	56	0
230	0</													

500	"	= 16 2
50	"	= 1 12
2	"	= 0 1
<u>2552</u>		<u>£82 8</u>

2. In the Table of Equivalent Prices, the first column from the left hand is the price per single; or 1; hence the other columns on the right and that give the price at an equal rate, according to various denominations by which the columns are headed.

Thus, suppose the price per lb. = $3\frac{1}{4}d.$, the price per ton = £30. 6s. 8d. Again, suppose the price per cwt. = £1. 10s., the price per dozen = 2s. 6d., &c.

STRENGTH OF MATERIALS.

Materials of construction are liable to four different kinds of strain; viz., stretching, or transverse action, and torsion or twisting: the first of which depends upon the body's tenacity; the second, on its resistance to compression; the third, on its tenacity and compression combined; and the fourth, on that property by which it opposes an acting force tending to change from a straight to that of a spiral direction, the fibres of wood

Circum in inch	Weight thom i	Diam chain :	Weight fathom	tons & cwt.	Circum in inch	Weight thom	Diam chain	Weight thom
3½	23¼	1⅞	5½	1 5½	10	23	1⅞	43
4½	42¼	2⅞	8	1 16¾	10¾	28	1⅞	49
5	52¼	3⅞	10½	2 10	11½	30½	1 in.	56
5¾	7	4	14	3 5½	12¼	36	1⅞	63
6½	9¾	4⅞	18	4 3½	13	39	1⅞	71
7	11½	5	22	5 2	13¾	45	1⅞	79
8	15	5⅞	27	6 4½	14½	48½	1⅞	87
8¾	19	6¼	32	7 7	15¼	56	1⅞	96
9½	21	6⅞	37	8 13½	16	60	1⅞	106

Note.—It must be understood and also borne in mind in estimating the amount of tensile strain to which subjected, the weight of the body itself must also into account; for according to its position so may it mate to its whole weight, in tending to produce within itself; as in the almost constant application and chains to great depths, considerable heights, &

*Alloys that are of greater Tenacity than the
their Constituents, as determined by the
ments of Muschenbroek.*

Swedish copper 6 parts, Malacca tin 1; tenacity per sq. inc
Chili copper 6 parts, Malacca tin 1; " "
Japan copper 5 parts, Banca tin 1; " "
Andalusian copper 6 parts, Cornish tin 1; " "

Ex. A beam of Riga fir, 12 inches by 12 inches, projecting 6½ feet from the wall; what is the weight it will support at the extremity of the beam?

Tabular value of $s=1100$

$12 \times 4.5=54$ sectional area.

$$\text{Then, } \frac{1100 \times 12 \times 54}{78} = 9138.4 \text{ lbs.}$$

When fracture of a beam is produced by pressure, the fibres of the lower section are separated by extension, whilst at the top those of the upper portion are destroyed by compression; hence exists a point in section where neither the one nor the other takes place, and distinguished as the point of neutral axis. by the law of fracture thus established, and data of tenacity and compression given in Table (p. 137), we are enabled to form the strongest section with the least possible material. In cast iron the resistance to compression is 6½ to 1 of tenacity; consequently a beam of the strongest section must be of the following form:



and a parabola in the direction of length, the quantity of material in the bottom flange being about 6 times that in the stem, but such is

3	1278	·24	1089	·33	954	·426	855	·1
3½	1739	·205	1482	·28	1298	·365	1164	·
4	2272	·18	1936	·245	1700	·32	1520	·
4½	2875	·16	2450	·217	2146	·284	1924	·
5	3560	·144	3050	·196	2650	·256	2375	·
6	5112	·12	4356	·163	3816	·213	3420	·
7	6958	·103	5929	·14	5194	·183	4655	·
8	9088	·09	7744	·123	6784	·16	6080	·
9	—	—	9801	·109	8586	·142	7695	·
10	—	—	12100	·098	10600	·128	9500	·
11	—	—	—	—	12826	·117	11495	·
12	—	—	—	—	15264	·107	13680	·
13	—	—	—	—	—	—	16100	·
14	—	—	—	—	—	—	18600	·
	12 feet.		14 feet.		16 feet.		18 feet	
6	2548	·48	2184	·65	1912	·85	1699	1
7	3471	·41	2975	·58	2603	·73	2314	
8	4532	·36	3884	·49	3396	·64	3020	
9	5733	·32	4914	·44	4302	·57	3825	
10	7083	·28	6071	·39	5312	·51	4722	
11	8570	·26	7346	·36	6428	·47	5714	
12	10192	·24	8736	·33	7648	·43	6796	
13	11971	·22	10260	·31	8978	·39	7980	
14	13883	·21	11900	·28	10412	·36	9255	
15	15937	·19	13660	·26	11952	·34	10624	
16	18128	·18	15536	·24	13584	·32	12080	
17	20500	·17	17500	·23	15353	·3	13647	
18	22932	·16	19656	·21	17208	·28	15700	

lbs. by the square of the column's length, divide the product by twenty times the π of π ; and the quotient will be equal to multiplied by the cube of the least thickness being expressed in inches.

Note 1.—When the pillar or support is a square, will be the fourth root of the quotient.

2. If the pillar or column be a cylinder, tabular value of π by 12, and the fourth root of equal the diameter.

Ex. 1. What should be the least diameter of oak support, to bear a weight of 2240 lbs. with sensible flexure, its breadth being 3 inches and length 5 feet?

Tabular value of $\pi=105$,

$$\text{and } \frac{2240 \times 5^2}{20 \times 105 \times 3} = \sqrt[3]{8.888} = 2.05$$

Ex. 2. Required the side of a square support, 9 feet in length, to bear a permanent weight of 6000 lbs.

Tabular value of $\pi=96$,

$$\text{and } \frac{6000 \times 9^2}{20 \times 96} = \sqrt[4]{253} = 4 \text{ inches}$$

"		"
"	oak (Dantzic)	"
"	red deal	"

Elasticity of torsion, or resistance of bodies

The angle of flexure by torsion is as the extensibility of the body directly, and as the diameter; hence, the length of a being given, the power, and the leverage acts with, being known, and also the number of degrees of torsion that will not affect the machine, to determine the diameter in a given angle of flexure.

Rule.—Multiply the power in lbs. by the shaft in feet, and by the leverage in the product by fifty-five times the number in the angle of torsion: and the fourth quotient equal the shaft's diameter in inches.

Ex. Required the diameters for a shaft 35 feet in length, and to transmit a power of 1245 lbs., acting at the circumference of 6 feet radius, so that the twist of the shaft by the application of the power may not exceed 1 degree.

$$\frac{1245 \times 35 \times 2.5}{55 \times 1} = \sqrt[4]{1981} = 6.67 \text{ inches in diameter}$$

Relative strength of metals to resist torsion

surfaces.

Heat also expands water in the li
Thus, when water is at 42° Fahr., it is at
density, or 1·00000 in bulk.

At 62° Fahr. its bulk is increased to 1·			
„ 92	„	„	1·
„ 122	„	„	1·
„ 152	„	„	1·
„ 182	„	„	1·
„ 212	„	„	1·

Water also expands in nearly an
from 42° Fahr., by reduction of temperat
abstraction of heat, down to the freezi

Atmospheric air is increased in bu
tion of temperature, as in the followin

At 32° Fahr. vol. equal 1·000				At 100° Fahr. 1	
„ 35	„	„	1·007	„ 110	„
„ 40	„	„	1·021	„ 120	„
„ 45	„	„	1·032	„ 130	„
„ 50	„	„	1·043	„ 140	„
„ 55	„	„	1·055	„ 150	„
„ 60	„	„	1·066	„ 160	„
„ 65	„	„	1·077	„ 170	„
„ 70	„	„	1·089	„ 180	„
„ 75	„	„	1·099	„ 190	„
„ 80	„	„	1·110	„ 200	„

conductors or retainers of heat, are
 viz.:—Stones, bricks, earthenware,
 sheep's wool, raw silk, and fur, each
 sively lower in their conducting power

Specific heat (formerly, capacity
 a term applied to the quantity of cal-
 stance can absorb or give out by a
 change of temperature, the amount
 mined by relation to the quantity which
 of another kind, as water, absorbs or
 a like change. Thus the quantity of
 to raise oil two degrees will only raise
 Hence a pound of water at 212° is said
 twice as much heat, or to have twice
 for heat, as that of oil.

The specific heat of water being	
" "	oil equal
" "	iron "
" "	copper "
" "	zinc "
" "	mercury

Gravity.—Gravity or gravitation
 pressure or weight. All bodies possess
 property, more or less, proportionate to
 degrees of density.

2	48·3	64·4
3	80·5	144·9
4	112·7	257·6
5	144·9	402·5
6	177·1	579·6
7	209·3	788·9
8	241·5	1030·4
9	273·7	1304·1
10	305·9	1610·0

The velocity acquired by a body falling from a given height is the same whether it falls vertically or descends upon a plane any way inclined.

Force of gravity is the cause of retarded and accelerated motion on inclined planes, the retarding force being as the height of the plane to the length of the plane. On a level line of railway $9\frac{1}{2}$ lbs. traction will overcome 2240 lbs., or one ton of insistent weight. On an incline or rise of 1 in 350, the traction to overcome the same weight is $\frac{2240}{350} = 6·4$, $+ 9·5 = 15·9$ lbs. Again, if the plane be descending, then the force of traction is diminished in an equal ratio, and the weight is increased by gravity; thus $9·5 - 6·4 = 3·1$ lbs. is the traction on the descending plane.

Force of gravity is also the restricting

of each are alike, then stop both and let freely. Opposite the centre of the centre of oscillation.

Of Motion.—Motion, in mechanics is a result or effect of a cause, acting in a manner as to impart either linear or circular motion by motive power. Thus, the piston of an engine by the action of the steam imparts motion. In the fly-wheel, through the crank, is produced uniform circular motion, and by means of eccentric cambs, etc., any degree of distortion may easily be produced.

Centrifugal force signifies the tendency of bodies to fly off in a tangential line from the centre of rotation, the amount of tendency being a function of the velocity of the body in motion, being proportional to the square of the velocity. —Multiply the square of the number of revolutions per minute by the radius of the circle, and by $\cdot 00032$ the weight of the body, and the product is the centrifugal force in terms of weight. Thus, suppose a body weighing 3 lbs. is describing a circle of 10 feet radius 3 times in a minute $3^2 \times 10 \times 1000 \cdot 00032 =$

inches, and if the square of the distance between any two points on its surface be divided by the diameter, the quotient will equal the altitude between the summit of the first point and that of the other point; hence, the distance the excess by level with an aneroid becomes 7.962 inches; at two miles it becomes 31.848, etc., being as the square of the distance; hence, the excess subtracted from the aneroid level, equals the true level as required in precise leveling operations.

Capillary attraction signifies a property of fluids, observable in small tubes, flat, thin spaces, or porous substances, as sponge, cotton-wick threads, etc., of raising water or other fluids above the natural level; hence the application of this principle for obtaining a continued supply of lubricating fluid between surfaces in a syphon form of worsted threads, which is immersed in oil, the other end being inserted and supported by the tube through which the fluid is conducted.

Atmospheric air is a transparent, subtle, elastic fluid, that naturally surrounds the globe, and in which we breathe for the support of life.

Liquids, or fluids, are incompressible and non-elastic, but adapted to useful purposes through friction by agitation and inequality of surface. Hydraulic machines are brought in to produce useful effects; and although the laws of statics and hydraulics are universally applicable to fluids in general, yet water being the most abundant in nature it is invariably had recourse to for purposes of motive power.

Fluids when confined exert a force in every direction, but when unconfined they follow the same laws as falling bodies in free fall. They are governed by mechanical considerations and produce similar results, so that through water wheels and turbines by the force of gravity, the greatest effect is produced, whether for turbines or water wheels.

Liquids, because of their gravity, press equally in every direction; any surface within a liquid sustains a pressure on every side equal to the weight of the column of liquid above it. The pressure is equal to as many times the weight of the greatest column or height of the liquid as the sectional area of the column is to the sectional area of the surface. The amount of pressure sustained is proportional to the height of the liquid above the surface.

substance required.

Example.—A piece of ye
40 ounces in the air, and being
attached to a piece of iron we
the two together are found to w
water, and the iron alone 25·8 o
required the specific gravity of

$40 + 25·8 = 65·8$, also $65·8$
 $40 \div 62·5 = 64$ the specific gravi

The specific gravity of a fl
mined by taking a solid body
sink in the fluid, and of known
weighing it both in the air and
difference between the two we
tiplied by the specific gravity
and the product divided by the
in the air; the quotient will be
of the fluid, that of water bein

Example.—Required the
given mixture of muriatic acid
of glass, the specific gravity of
 $3\frac{1}{2}$ ounces when immersed, and

$6 - 3·75 = 2·25$, $\times 3 = 6·75$, \div
gravity.

of temperature from 32° to 212°

Factors for increase of length.		Factors for increase of length.	
Glass tube . . .	·000861	Gold, to . . .	·000861
Platina . . .	·000884	Copper . . .	·000992
" . . .	·000992	Silver . . .	·001220
Iron . . .	·001220	Lead . . .	·001466
Gold, from . . .	·001466	Zinc . . .	·001466

Hence, the length of a bar of any named substances will be increased to its original length at 32°, multiplied by the factors in the table, when raised to a temperature. Thus, a bar of iron 50 inches in length become expanded at 212°, to $50 \times 1.001220 = 50.061$ inches.

Liquefaction, Melting, and Fusion are synonymous terms, but in some instances different: they each signify a change from a solid to a liquid state by heat. In the case of liquefaction, a solvent, as hot water, is required; thus, neither salt nor sugar can be liquefied alone. To ice, mercury, tallow, &c., "melting" is the common appellation; but to the fusion of metals alone in their liquid state, "fusion" is never applied; hence, fusion is never applied; hence, fusion is never applied; hence, fusion is never applied.

Velocity by a given Power

Horse Power.	Number of revolutions per minute of cast									
	20	25	30	35	40	45	50	55	60	65
Diameters of the shafts in inches.										
10	5½	6½	5½	4½	4½	4½	4½	4½	4½	4
20	7½	6½	6½	6½	5½	5½	5½	5½	5½	5
30	8½	7½	7½	7	6½	6½	6½	6	5½	5
40	9½	8½	8½	7½	7½	7	6½	6½	6½	6
50	10	9½	8½	8½	8	7½	7	7½	7	6
60	10½	9½	9½	8½	8½	8½	7½	7½	7½	7
70	11½	10½	9½	9½	8½	8½	8	8	7½	7
80	11½	10½	10½	9½	9½	8½	8½	8½	8½	7
90	12½	11½	10½	10½	9½	9	9	8½	8½	8
100	12½	11½	11	10½	10	9½	9½	9	8½	8
125	13½	12½	11½	11½	10½	10½	10	9½	9½	9
150	14½	13½	12½	12	11½	11	10½	10½	10	9
175	16½	14½	13½	12½	12	11½	11	10½	10½	10
200	15½	14½	13½	13½	12½	12½	11½	11½	11	10
Number of revolutions per minute of wrought										
	20	25	30	35	40	45	50	55	60	65
10	5	4½	4½	4½	4	3½	3½	3½	3½	3
20	6½	5½	5½	5½	5	4½	4½	4½	4½	4
30	7½	6½	6½	6	5½	5½	5½	5½	5	4
40	8	7½	7	6½	6½	6½	6	6	5½	5
50	8½	8	7½	7	7½	6½	6½	6½	6	5
60	9	8½	8	7½	7½	6½	6½	6½	6½	6
70	9½	9	8½	8	7½	7	7	7	6½	6
80	10½	9½	8½	8½	8	7½	7½	7½	7½	7
90	10½	9½	9½	8½	8½	8	7½	7½	7½	7
100	10½	10½	9½	9	8½	8½	8	7½	7½	7
125	11½	10½	10½	9½	9½	9	8½	8½	8½	8
150	12½	11½	11	10½	10	9½	9½	9	8½	8
175	13½	12½	11½	10½	10½	10	9½	9½	9	8
200	13½	12½	12	11½	10½	10½	10½	9½	9½	9

eter of ces in ches.	Decima Numbers.
. . .	.8508
. . .	.9163
. . .	.9817
. . .	1.0471
. . .	1.1778
. . .	1.3088
. . .	1.5708

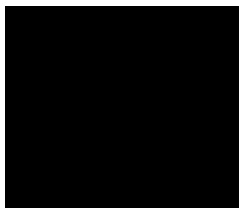
hole tube surface
 ace of a boiler con-
 meter, and 6 feet in

13.12 square feet, total

942 square feet, effective

to non-condensing

engine, the diameter
 orce of steam being



Diameter Cylinder in inch	30	35	40	45	50
	Horse power.				
3½	1	1¼	1½	1¾	1
3¾	1¼	1½	1¾	1¾	2
4	1½	1¾	1¾	2¼	2
4¼	1¾	1¾	2¼	2¼	2
4½	1¾	2¼	2¼	2¼	3
4¾	2	2¼	2¼	3	3
5	2¼	2¼	3	3¾	3
5¼	2¼	3	3¼	3¾	4
5½	2¾	3¼	3½	4	4
5¾	3	3½	4	4½	5
6	3¼	3¾	4¼	5	5
6½	3¾	4½	5	5¾	6
7	4½	5½	5¾	6¼	7
7½	5	6	6¾	7½	8
8	5¾	6¾	7½	8½	9
8½	6¼	7½	8	9¼	10
9	7¼	8½	9¾	11	12
9½	8½	9½	10¾	12½	13
10	9	10½	12	13½	15
11	10¾	12¾	14½	16¼	18
11½	12	13¾	15¾	17¾	19
12	13	15	17¼	19¼	21

is not working to any greater extent
 than the common slide will effect.
 Non-condensing engines require more
 than a proper supply to the boiler
 an addition for leakage, waste, etc.
 consumption of fuel is as the quantity
 evaporated, requiring on an average
 11 lbs. of coal per nominal horse power
 of the double-cylinder engine on the
 principles, and only requiring a small
 water for condensation as in the combined
 and extra fuel as those on the
 principle, but to produce the same
 power, neither the one nor the other
 equal proportions; hence its economy.
 Thus, an engine with a cylinder of
 diameter, and steam at 7 lbs. per
 equals 16 horses' power nominally, and
 a cylinder of 12 inches diameter
 40 lbs. per square inch, equals 16
 nominally on the non-condensing
 an engine on the combined principle
 at 40 lbs. per square inch, and the
 piston has passed through about $4\frac{1}{2}$ ft.
 in a non-condensing cylinder of $8\frac{1}{2}$

one.

2. When the required pulley is greater given one.

Rule.—Add double the number B to 2 from the square root of the sum subtracted and call the remainder E. Multiply the by the distance between the centres, of and the product, added to the radius of or less pulley, will give the radius of the or greater pulley.

Ex. 1. Let the distance between the shafts equal 36 inches, the radius of 30 inches, and half the length of belt 98 to find the radius of the other pulley.

3.1416 multiplied by 30=94.248

Add distance between shafts 36

130.248 trial

Subtract half length of belt 98.55

Divide by distance between shafts 36)31.698(.880

From2.4674

Subtract twice A, or .8805 \times 2 = 1.761

= .7064 square r

= .8404, which subtract from 1.5708 = .7304, or

Rule.—In each case multiply the circumference in inches by the length in feet, and use the divisors as follow

For customary measure 2304 For the true

When $\frac{1}{4}$ the girth is
allowed for bark 3009 „

When $\frac{1}{8}$ th the girth is
allowed for bark 2845 „

Note.—The mean girth is taken for the c

Ex. 1. Required the contents of a t
measure, when $\frac{1}{4}$ th of the girth is all
circumference of mean girth being 4
length of tree 18 feet.

$$48^2 \times 18 = 41472 \div 3009 = 13$$

Ex. 2. Required the true conten
dimensions when no allowance for ba

$$41472 \div 1800 = 23 \text{ feet.}$$

On Windmills as as a Motive-powe

Wind, or air in motion become
source of motive power through imp
the sails of a windmill, and although
trustworthy for stability of motion, is
for corn and flour mills, pumping of v

The shaft or axle that lies transverse

9	81	729	3·0000000
10	100	1000	3·1622777
11	121	1331	3·3166248
12	144	1728	3·4641016
13	169	2197	3·6055513
14	196	2744	3·7416574
15	225	3375	3·8729833
16	256	4096	4·0000000
17	289	4913	4·1231056
18	324	5832	4·2426407
19	361	6859	4·3588989
20	400	8000	4·4721360
21	441	9261	4·5825757
22	484	10648	4·6904158
23	529	12167	4·7958315
24	576	13824	4·8989795
25	625	15625	5·0000000
26	676	17576	5·0990195
27	729	19683	5·1961524
28	784	21952	5·2915026
29	841	24389	5·3851648
30	900	27000	5·4772256
31	961	29791	5·5677644
32	1024	32768	5·6568542
33	1089	35937	5·7445626
34	1156	39304	5·8309519
35	1225	42875	5·9160798
36	1296	46656	6·0000000
37	1369	50653	6·0827625

89	7921	701969	9·4339811	.
90	8100	729000	9·4868330	.
91	8281	753571	9·5393920	.
92	8464	778688	9·5916630	.
93	8619	804357	9·6436508	.
94	8836	830584	9·6953597	.
95	9025	857375	9·7467943	.
96	9216	884736	9·7979590	.
97	9409	912673	9·8488578	.
98	9601	941192	9·8994949	.
99	9801	970299	9·9498744	.
100	10000	1000000	10·0000000	.
101	10201	1030301	10·0498756	.
102	10404	1061208	10·0995049	.
103	10609	1092727	10·1488916	.
104	10816	1124864	10·1980390	.
105	11025	1157625	10·2469508	.
106	11236	1191016	10·2956301	.
107	11449	1225043	10·3440804	.
108	11664	1259712	10·3923048	.
109	11881	1295029	10·4403065	.
110	12100	1331000	10·4880885	.
111	12321	1367631	10·5356538	.
112	12544	1404928	10·5830052	.
113	12769	1442897	10·6301458	.
114	12996	1481544	10·6770783	.
115	13225	1520875	10·7238053	.
116	13456	1560896	10·7703296	.
117	13689	1601613	10·8166538	.
118	13921	1643039	10·8627805	.

169	28561	4826809	13-0000000
170	28900	4913000	13-0384048
171	29241	5000211	13-0766968
172	29584	5088448	13-1148770
173	29929	5177717	13-1529464
174	30276	5268024	13-1909080
175	30625	5359375	13-2287566
176	30976	5451776	13-2664992
177	31329	5545233	13-3041347
178	31684	5639752	13-3416641
179	32041	5735339	13-3790882
180	32400	5832000	13-4164079
181	32761	5929741	13-4536240
182	33124	6028568	13-4907376
183	33489	6128487	13-5277493
184	33856	6229504	13-5646600
185	34225	6331625	13-6014705
186	34596	6434856	13-6381817
187	34969	6539203	13-6747943
188	35344	6644672	13-7113092
189	35721	6751269	13-7477271
190	36100	6859000	13-7840488
191	36481	6967871	13-8202750
192	36864	7077888	13-8561065
193	37249	7189057	13-8924440
194	37636	7301384	13-9283883
195	38025	7414875	13-9642400
196	38416	7529536	14-0000000
197	38809	7645373	14-0356688

249	62001	15438249	15-7797338
250	62500	15625000	15-8113883
251	63001	15813251	15-8429795
252	63504	16003008	15-8745079
253	64009	16194277	15-9059737
254	64516	16387064	15-9373775
255	65025	16581375	15-9687194
256	65536	16777216	16-0000000
257	66049	16974593	16-0312195
258	66564	17173512	16-0623784
259	67081	17373979	16-0934769
260	67600	17576000	16-1245155
261	68121	17779581	16-1554944
262	68644	17984728	16-1864141
263	69169	18191447	16-2172747
264	69696	18399744	16-2480768
265	70225	18609625	16-2788206
266	70756	18821096	16-3095064
267	71289	19034163	16-3401346
268	71824	19248832	16-3707055
269	72361	19465109	16-4012195
270	72900	19683000	16-4316767
271	73441	19902511	16-4620776
272	73984	20123648	16-4924225
273	74529	20346417	16-5227116
274	75076	20570824	16-5521454
275	75625	20796875	16-5831240
276	76176	21024576	16-6132477
277	76729	21253933	16-6433170

	Cube Root.
6	847021
6	854124
6	861212
6	868285
6	875344
6	882389
6	889419
6	896435
6	903436
6	910423
6	917396
6	924356
6	931301
6	938232
6	945150
6	952053
6	958943
6	965820
6	972683
6	979532
6	986368
6	993191
7	000000
7	006796
7	013579
7	020349
7	027106
7	033850

409	167281	68417929	20·2237484
410	168100	68921000	20·2484567
411	168921	69426531	20·2731349
412	169744	69934528	20·2977831
413	170569	70444997	20·3224014
414	171396	70957944	20·3469899
415	172225	71478375	20·3715488
416	173056	71991296	20·3960781
417	173889	72511713	20·4205779
418	174724	73034632	20·4450483
419	175561	73560059	20·4694895
420	176400	74088000	20·4939015
421	177241	74618461	20·5182845
422	178084	75151448	20·5426386
423	178929	75686967	20·5669638
424	179776	76225024	20·5912603
425	180625	76765625	20·6155281
426	181476	77308776	20·6397674
427	182329	77854483	20·6639783
428	183184	78402752	20·6881609
429	184041	78953589	20·7123152
430	184900	79507000	20·7364414
431	185761	80062991	20·7605395
432	186624	80621568	20·7846097
433	187489	81182737	20·8086520
434	188356	81746504	20·8326667
435	189225	82312875	20·8566536
436	190096	82881856	20·8806130
437	190969	83453453	20·9045450

489	239121	116930169	22-1133444
490	240100	117649000	22-1359436
491	241081	118370771	22-1585198
492	242064	119095488	22-1810730
493	243049	119823157	22-2036033
494	244036	120553784	22-2261108
495	245025	121287375	22-2485955
496	246016	122023936	22-2710575
497	247009	122763473	22-2934968
498	248004	123505992	22-3159136
499	249001	124251499	22-3383079
500	250000	125000000	22-3606798
501	251001	125751501	22-3830293
502	252004	126506008	22-4053565
503	253009	127263527	22-4276615
504	254016	128024064	22-4499443
505	255025	128787625	22-4722051
506	256036	129554216	22-4944438
507	257049	130323843	22-5166605
508	258064	131096512	22-5388553
509	259081	131872229	22-5610283
510	260100	132651000	22-5831796
511	261121	133432831	22-6053091
512	262144	134217728	22-6274170
513	263169	135005647	22-6495033
514	264196	135796744	22-6715681
515	265225	136590875	22-6936114
516	266256	137388096	22-7156334
517	267289	138188413	22-7376340

565	322624	183250432	23'83:
569	323761	184220009	23'85:
570	324900	185193000	23'87:
571	326041	186169411	23'89:
572	327184	187149248	23'91:
573	328329	188132517	23'93:
574	329476	189119224	23'95:
575	330625	190103875	23'97:
576	331776	191102976	24'00:
577	332929	192100033	24'02:
578	334084	193100552	24'04:
579	335241	194104539	24'06:
580	336400	195112000	24'08:
581	337561	196122941	24'10:
582	338724	197137368	24'12:
583	339889	198155287	24'14:
584	341056	199176704	24'16:
585	342225	200201625	24'18:
586	343396	201230056	24'20:
587	344569	202262003	24'22:
588	345744	203297472	24'24:
589	346921	204336469	24'26:
590	348100	205379000	24'28:
591	349281	206425071	24'31:
592	350464	207474688	24'33:
593	351649	208527857	24'35:
594	352836	209584584	24'37:
595	354025	210644875	24'39:
596	355216	211708736	24'41:
597	356409	212776173	24'43:

648	419904	272097792	25·4551
649	421201	273359449	25·475·
650	422500	274625000	25·4951
651	423801	275894451	25·514·
652	425104	277167808	25·534·
653	426409	278445077	25·5531
654	427716	279726264	25·573·
655	429025	281011375	25·5921
656	430336	282300416	25·612·
657	431649	283593393	25·6321
658	432964	284890312	25·6511
659	434281	286191179	25·6701
660	435600	287496000	25·6901
661	436921	288804781	25·7091
662	438244	290117528	25·7291
663	439569	291434247	25·7481
664	440896	292754944	25·7681
665	442225	294079625	25·7871
666	443556	295408296	25·8061
667	444889	296740963	25·8261
668	446224	298077632	25·8451
669	447561	299418309	25·8650
670	448900	300763000	25·8843
671	450241	302111711	25·9036
672	451584	303464448	25·9229
673	452929	304821217	25·9422
674	454276	306182024	25·9615
675	455625	307546875	25·9807
676	456976	308915776	26·0000
677	458329	310288733	26·0192

727	529984	385828352	26-981
728	531441	387420489	27-000
730	532900	389017000	27-018
731	534361	390617891	27-037
732	535824	392223168	27-055
733	537289	393832837	27-073
734	538756	395446904	27-092
735	540225	397065375	27-110
736	541696	398688256	27-129
737	543169	400315553	27-147
738	544644	401947272	27-166
739	546121	403583419	27-184
740	547600	405224000	27-202
741	549081	406869021	27-221
742	550564	408518488	27-239
743	552049	410172407	27-258
744	553536	411830784	27-276
745	555025	413493625	27-294
746	556516	415160936	27-313
747	558009	416832723	27-331
748	559504	418508992	27-349
749	561001	420189749	27-367
750	562500	421875000	27-386
751	564001	423564751	27-404
752	565504	425259008	27-422
753	567009	426957777	27-440
754	568516	428661064	27-458
755	570025	430368875	27-477
756	571536	432081216	27-495

808	652864	527514112	28-42
809	654481	529475129	28-44
810	656100	531441000	28-46
811	657721	533411731	28-47
812	659344	535387328	28-49
813	660969	537367797	28-51
814	662596	539353144	28-53
815	664225	541343375	28-54
816	665956	543338496	28-56
817	667489	545338513	28-58
818	669124	547343432	28-60
819	670761	549358259	28-61
820	672400	551368000	28-63
821	674041	553387661	28-65
822	675684	555412248	28-67
823	677329	557441767	28-68
824	678976	559476224	28-70
825	680625	561515625	28-72
826	682276	563559976	28-74
827	683929	565609283	28-75
828	685584	567663552	28-77
829	687241	569722789	28-79
830	688900	571787000	28-80
831	690561	573856191	28-82
832	692224	575930368	28-84
833	693889	578009537	28-86
834	695556	580093704	28-87
835	697225	582182875	28-89
836	698896	584277056	28-91
837	700560	586376329	28-93



000	788544	70022
889	790321	70259
890	792100	70496
891	793881	70734
892	795664	70973
893	797449	71212
894	799236	71451
895	801025	71691
896	802816	71932
897	804609	72173
898	806404	72415
899	808201	72657
900	810000	72900
901	811801	73143
902	813604	73387
903	815409	73631
904	817216	73876
905	819025	74121
906	820836	74367
907	822649	74614
908	824464	74861
909	826281	75108
910	828100	75357
911	829921	75605
912	831744	75855
913	833569	76104
914	835396	76355
915	837225	76606
916	839056	76857
917	840889	77100

No.	Square.	Cube.	Sq. Root.	Cube Root.
921	848241	781229961	30·3479818	9·729411
922	850084	783777448	30·3644529	9·732931
923	851929	786330467	30·3809151	9·736418
924	853776	788889024	30·3973683	9·739963
925	855625	791453125	30·4138127	9·743476
926	857476	794022776	30·4302481	9·746986
927	859329	796597983	30·4466747	9·750493
928	861184	799178752	30·4630924	9·753998
929	863041	801765089	30·4795013	9·757500
930	864900	804357000	30·4959014	9·761000
931	866761	806954491	30·5122926	9·764497
932	868624	809557568	30·5286750	9·767992
933	870489	812166237	30·5450487	9·771484
934	872356	814780504	30·5614136	9·774974
935	874225	817400375	30·5777697	9·778462
936	876096	820025856	30·5941171	9·781947
937	877969	822656953	30·6104557	9·785429
938	879844	825293672	30·6267857	9·788909
939	881721	827986019	30·6431069	9·792386
940	883600	830584000	30·6594194	9·795861
941	885481	833237621	30·6757233	9·799334
942	887364	835896888	30·6920185	9·802804
943	889249	838561807	30·7083051	9·806271
944	891136	841232384	30·7245830	9·809736
945	893025	843908625	30·7408523	9·813199
946	894916	846590536	30·7571130	9·816659
947	896809	849278123	30·7733651	9·820117
948	898704	851971392	30·7896086	9·823572
949	900601	854670349	30·8058436	9·827025
950	902500	857375000	30·8220700	9·830476
951	904401	860085351	30·8382879	9·833924
952	906304	862801408	30·8544972	9·837369
953	908209	865523177	30·8706981	9·840813
954	910116	868250664	30·8868904	9·844254
955	912025	870983875	30·9030743	9·847692
956	913936	873722816	30·9192497	9·851128
957	915849	876467493	30·9354166	9·854562
958	917764	879217912	30·9515751	9·857993
959	919681	881974079	30·9677251	9·861422
960	921600	884736000	30·9838668	9·864848



968	937024	907038
969	938961	909853
970	940900	912673
971	942841	915498
972	944784	918330
973	946729	921167
974	948676	924010
975	950625	926859
976	952576	929714
977	954529	932574
978	956484	935441
979	958441	938313
980	960400	941192
981	962361	944076
982	964324	946966
983	966289	949862
984	968256	952763
985	970225	955671
986	972196	958585
987	974169	961504
988	976144	964430
989	978121	967361
990	980100	970299
991	982081	973242
992	984064	976191
993	986049	979146
994	988036	982107
995	990025	985074
996	992016	988047
997	994009	991026

Table of Squares, Cubes, and Fourth Power of Numbers.

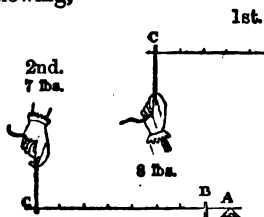
Root.	Square.	Cube.	4th Power.	Root.	Square.	Cube.	4th Power.
1	1	1	1	7	49	343	2401
2	4	8	16	8	64	512	4096
3	9	27	81	9	81	729	6561
4	16	64	256	10	100	1000	10000
5	25	125	625	11	121	1331	14641
6	36	216	1296	12	144	1728	20736
7	49	343	2401	13	169	2197	28561
8	64	512	4096	14	196	2744	37344
9	81	729	6561	15	225	3375	45025
10	100	1000	10000	16	256	4096	53144
11	121	1331	14641	17	289	4913	61505
12	144	1728	20736	18	324	5832	70648
13	169	2197	28561	19	361	6859	80523
14	196	2744	37344	20	400	8000	91600
15	225	3375	45025	21	441	9261	104401
16	256	4096	53144	22	484	10648	119136
17	289	4913	61505	23	529	12167	136025
18	324	5832	70648	24	576	13824	156256
19	361	6859	80523	25	625	15625	177125
20	400	8000	91600	26	676	17700	200000
21	441	9261	104401	27	729	19683	226673
22	484	10648	119136	28	784	21952	257696
23	529	12167	136025	29	841	24389	292421
24	576	13824	156256	30	900	27000	324000
25	625	15625	177125	31	961	29791	358181
26	676	17700	200000	32	1024	32768	398136
27	729	19683	226673	33	1089	35937	436217
28	784	21952	257696	34	1156	39744	473616
29	841	24389	292421	35	1225	43300	510325
30	900	27000	324000	36	1296	46656	546400
31	961	29791	358181	37	1369	50823	581921
32	1024	32768	398136	38	1444	54872	617024
33	1089	35937	436217	39	1521	58809	652721
34	1156	39744	473616	40	1600	62720	689000
35	1225	43300	510325	41	1681	66611	725841
36	1296	46656	546400	42	1764	70488	763236
37	1369	50823	581921	43	1849	74357	801181
38	1444	54872	617024	44	1936	78224	839680
39	1521	58809	652721	45	2025	82089	878725
40	1600	62720	689000	46	2116	85952	918320
41	1681	66611	725841	47	2209	89813	958461
42	1764	70488	763236	48	2304	93680	999136
43	1849	74357	801181	49	2401	97553	1040341
44	1936	78224	839680	50	2500	101440	10819600
45	2025	82089	878725	51	2601	105341	11240801
46	2116	85952	918320	52	2704	109264	11667024
47	2209	89813	958461	53	2809	113209	12108281
48	2304	93680	999136	54	2916	117176	12564576
49	2401	97553	1040341	55	3025	121165	13035925
50	2500	101440	10819600	56	3136	125176	13522336
51	2601	105341	11240801	57	3249	129209	14023801
52	2704	109264	11667024	58	3364	133264	14539424
53	2809	113209	12108281	59	3481	137341	15069301
54	2916	117176	12564576	60	3600	141440	15613600
55	3025	121165	13035925	61	3721	145561	16172401
56	3136	125176	13522336	62	3844	149704	16745824
57	3249	129209	14023801	63	3969	153873	17333881
58	3364	133264	14539424	64	4096	158064	17935600
59	3481	137341	15069301	65	4225	162285	18550925
60	3600	141440	15613600	66	4356	166528	19180864
61	3721	145561	16172401	67	4489	170793	19824421
62	3844	149704	16745824	68	4624	175080	20481600
63	3969	153873	17333881	69	4761	179389	21152401
64	4096	158064	17935600	70	4900	183720	21836800
65	4225	162285	18550925	71	5041	188083	22534921
66	4356	166528	19180864	72	5184	192468	23246736
67	4489	170793	19824421	73	5329	196885	23972281
68	4624	175080	20481600	74	5476	201328	24711576
69	4761	179389	21152401	75	5625	205797	25464625
70	4900	183720	21836800	76	5776	210292	26231424
71	5041	188083	22534921	77	5929	214813	27011961
72	5184	192468	23246736	78	6084	219360	27806256
73	5329	196885	23972281	79	6241	223933	28614401
74	5476	201328	24711576	80	6400	228640	29436800
75	5625	205797	25464625	81	6561	233481	30273441
76	5776	210292	26231424	82	6724	238356	31124336
77	5929	214813	27011961	83	6889	243265	31989481
78	6084	219360	27806256	84	7056	248304	32868864
79	6241	223933	28614401	85	7225	253375	33762425
80	6400	228640	29436800	86	7396	258480	34670176
81	6561	233481	30273441	87	7569	263619	35592081
82	6724	238356	31124336	88	7744	268792	36528144
83	6889	243265	31989481	89	7921	273999	37478361
84	7056	248304	32868864	90	8100	279240	38442700
85	7225	253375	33762425	91	8281	284513	39421181
86	7396	258480	34670176	92	8464	289816	40413824
87	7569	263619	35592081	93	8649	295149	41420641
88	7744	268792	36528144	94	8836	300512	42441736
89	7921	273999	37478361	95	9025	305905	43477125
90	8100	279240	38442700	96	9216	311328	44526816
91	8281	284513	39421181	97	9409	316781	45590801
92	8464	289816	40413824	98	9604	322264	46659184
93	8649	295149	41420641	99	9801	327789	47741961
94	8836	300512	42441736	100	10000	333350	48838400
95	9025	305905	43477125				
96	9216	311328	44526816				
97	9409	316781	45590801				
98	9604	322264	46659184				
99	9801	327789	47741961				
100	10000	333350	48838400				



They are usually accounted *lever*, the *wheel* and *axle*, *plane*, the *wedge*, and the of these comprise the *who inclined plane*,—the wheel a of the first kind, and the pu —the wedge and the screw to that of the inclined plane seems to be the case in thes require, on account of their peculiar rule of estimation different circumstances in wh required to act.

1. THE I

Levers, according to mo following,



are distinguished as being of the first, second, or third kind; and although levers of equal lengths produce different effects, the general principles of estimation in all are the same; namely, the power is to the weight or resistance, as the distance of the one end of the fulcrum is to the distance of the other end to the same point.

In the *first kind*, the power is to the resistance, as the distance A B is to the distance B C.

In the *second*, the power is to the resistance, as the distance A B is to that of A C; and,

In the *third*, the resistance is to the power, as the distance A B is to that of A C.

Rule, first kind.—Divide the longer by the shorter end of the lever from the fulcrum, and the quotient is the effective force that the power supplied is equal to.

Ex. 1. Let the handle of a pump equal 65 inches in length, and 10 inches from the shortest end to centre of motion; what is the amount of effective leverage thereby obtained?

$$65 - 10 = 55, \text{ and } \frac{55}{10} = 5\frac{1}{2} \text{ to } 1.$$

Ex. 2. Required the situation of the fulcrum on which to rest a lever of 15 feet, so that $2\frac{1}{2}$ cwt. placed at one end may equipoise 30 cwt. at the other, the weight of the lever not being taken into account.

$$\frac{15 \times 2.5}{2.5 + 30} = 1.154 \text{ feet from the end on which the 30 cwt. is to be placed.}$$

The common steelyard, or Roman balance, as represented in fig. 1, Plate D, is a lever of the first kind, and so divided that one weight w , moved to or from the axis of motion, will equipoise and there indicate the weight of any article required to be known.

proportion of effect that the power or resistance to be overcome.

Ex. Required the amount of effort produced by a power of 50lbs. on the pump, the length of the lever being distance from ram to fulcrum $4\frac{1}{2}$ inches

8 feet=96 inches, and $\frac{96}{4.5}=8$, or the
are to each other as 8 to 1; hence
upon the ram.

The lever on the safety-valve of the *third kind*, the action of the steam and the weight or spring-balance; but in such application the weight must also be taken into account simply ascertained by such means as fig 2, plate D, where A is a *Safety* to the lever by a light line, immediate of pressure on the valve, and which or otherwise, will indicate the lever point.

This is perhaps the most frequent the third kind of lever to mechanism that in which great nicety is required

APPLICATIONS OF MECHANIC POWERS.

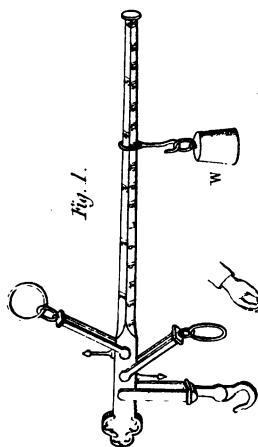


Fig. 1.

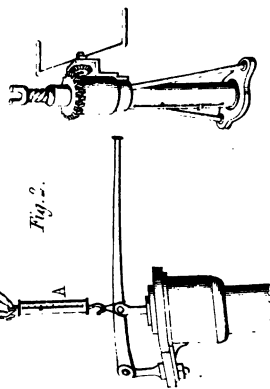
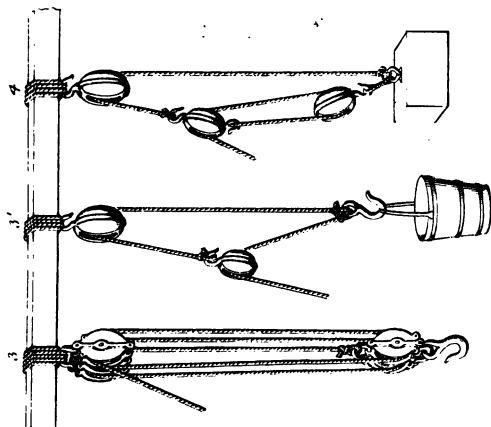


Fig. 2.

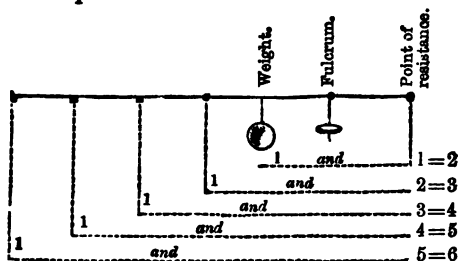


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1. The first part of the document is a list of names and titles, including the names of the authors and the titles of the works. The list is organized in a table with two columns: the first column contains the names of the authors, and the second column contains the titles of the works. The names are listed in alphabetical order, and the titles are listed in the order in which they appear in the document.

istance, as shown in the annexed diagram to illustrate this particular case.



Thus, suppose the weight to be placed on any one of the divisions, it is still the same weight, or 1; but because of the principle of the lever, the resistance is increased equal to the number of times the weight is distant from the fulcrum; consequently the action of the lever tends to press down the valve equal the sum of the weight and resistance, or the number of times the weight is distant from the resistance.

2. THE WHEEL AND PINION, OR CRANE.

The mechanical advantage of the wheel and axle, or crane, is as the velocity of the weight to the velocity of the power; and being only a modification of the first kind of lever, it of course partakes of the same principles.

1. *To determine the amount of effective power produced from a given power by means of a crane with known peculiarities.*

Rule.—Multiply together the diameter of the circle described by the winch, or handle, and the number of revolutions of the pinion to 1 of the wheel; divide the product by the barrel's diameter in equal terms

$$\frac{30 \times 8}{11} = 21.8 \text{ to } 1 \text{ of exertive force; and}$$

2. *Given any two parts of a crane that shall produce any required mechanical effect.*

Rule.—Multiply the two given $\frac{1}{2}$ divide the product by the required $\frac{1}{2}$ the quotient is the dimensions of equal terms of unity.

Ex. Suppose that a crane is required power to effect being as 40 to 1, and pinion 11 to 1 is unavoidably employed, also the throw of each inches; what must be the barrel's diameter the rope or chain must coil?

$$16 \times 2 = 32 \text{ inches diameter of circle d}$$

$$\text{And } \frac{32 \times 11}{40} = 8.8 \text{ inches, the barrel's}$$

3. THE PULLEY.

The principle of the pulley, or the block and tackle, is the distribution of various points of support; the mechanical advantage derived depending entirely upon the number of points of support.

the power is to the weight as the number of cords attached to the lower block; whence the following rules.

1. Divide the weight to be raised by the number of cords leading *to, from, or attached* to the lower block; and the quotient is the power required to produce an equilibrium, provided friction did not exist.

2. Divide the weight to be raised by the power to be applied; the quotient is the number of sheives in, or cords attached to the rising block.

Ex. Required the power necessary to raise a weight of 3000 lbs. by a four and five-sheived block and tackle, the four being the moveable or rising block.

Necessarily there are nine cords leading to and from the rising block.

Consequently $\frac{3000}{9} = 333$ lbs., the power required.

Ex. 2. I require to raise a weight of 1 ton 18 cwt., or 4256 lbs.; the amount of my power to effect this object being 500 lbs., what kind of block and tackle must I of necessity employ?

$\frac{4256}{500} = 8.51$ cords; of necessity there must be 4 sheives or 9 cords in the rising block.

As the effective power of the crane may, by additional wheels and pinions, be increased to any required extent, so may the pulley and tackle be similarly augmented by purchase upon purchase; two of the most useful of such applications being represented in figs. 3 and 4, Plate D, the first of which is known by the term *runner and tackle*, and the second by that of *Spanish burton*.

the rise to so many parts in a certain distance, as 1 in 100, 1 in 200, &c., the perpendicular height to the horizontal length in attaining such numbers being of the same denomination expressed; but it may be necessary that the inclination of a plane, the sine of the height per mile, or the height for ratio, &c., are all synonymous terms.

The advantage gained by the incline when the power acts in a parallel direction to the plane is as the length to the height. *H*. Divide the weight by the ratio of the incline, the quotient equal the power that will support that weight upon the plane. Or, multiply the weight by the height of the plane, and divide by the length,—the quotient is the power.

Ex. Required the power or effort capable of supporting a load of 350 lbs. on a plane of 1 in 12, or 3 feet in height and 36 feet in length.

$$\frac{350}{12} = 29.16 \text{ lbs.}, \text{ or } \frac{350 \times 3}{36} = 29.16 \text{ lbs. power}$$

Note.—The weight multiplied by the length of the incline, the product divided by the height of the incline, equal the power.

Table showing the Resistance opposed to the Motion of Carriages on different Inclinations of Ascending or Descending Planes, whatever part of the insistent weight they are drawn by.

Hundreds.										
Tens.		100	200	300	400	500	600	700	800	900
10	.1	-.01	-.005	-.00333	-.0025	-.002	-.00167	-.00143	-.00125	-.00111
20	.05	-.00909	-.00476	-.00322	-.00244	-.00196	-.00164	-.00141	-.00123	-.0011
30	.0333	-.00833	-.00454	-.00312	-.00238	-.00192	-.00161	-.00139	-.00122	-.00109
40	.025	-.00769	-.00435	-.00303	-.00232	-.00189	-.00159	-.00137	-.0012	-.00107
50	.02	-.00714	-.00417	-.00294	-.00227	-.00185	-.00156	-.00135	-.00119	-.00106
60	.0166	-.00667	-.004	-.00286	-.00222	-.00182	-.00154	-.00133	-.00118	-.00105
70	.0143	-.00625	-.00385	-.00278	-.00217	-.00178	-.00151	-.00131	-.00116	-.00104
80	.0125	-.00588	-.0037	-.0027	-.00213	-.00175	-.00149	-.0013	-.00115	-.00103
90	.0111	-.00555	-.00357	-.00263	-.00208	-.00172	-.00147	-.00128	-.00114	-.00102
		-.00526	-.00345	-.00256	-.00204	-.00169	-.00145	-.00126	-.00112	-.00101

Note.—Although this Table has been calculated particularly for carriages on railway inclines, it may with equal propriety be applied to any other incline, the amount of traction on a level being known.

Added to

Then $\frac{150}{\cdot 00711} = 21097$ lbs. weight drawn up th

2. What weight would a force of 15 down the same plane, the friction on the the same as before ?

Friction on the level = $\cdot 00417$

Gravity of the plane = $\cdot 00294$ subtract

$$\underline{\hspace{1cm}} \\ = \cdot 00123$$

And $\frac{150}{\cdot 00123} = 121915$ lbs. weight drawn down

Example of incline when velocity is taken is

A power of 230 lbs., at a velocity of 7 minute, is to be employed for moving an inclined plane 12 feet in height and 1 length, the least velocity of the weight to per minute; required the greatest weigh power is equal to.

$$\frac{230 \times 75 \times 163}{12 \times 8} = \frac{2811750}{96} = 29288 \text{ lbs., or } 13 \frac{1}{2}$$

TABLE OF INCLINED PLANES,
*Showing the ascent or descent per yard, and the corresponding ascent or descent
 per chain, per mile; and also the ratio.*

Per yard.		Per chain.		Per mile.		Ratio.	
In parts of an in.	In decla. of an inch.	Inches.	Feet.	In parts of an in.	In decla. of an inch.	One in	One in
$\frac{1}{16}$.0156	.344	2.29	$\frac{1}{16}$.4375	2304	82
$\frac{1}{8}$.0208	.458	3.06	$\frac{1}{8}$.5	1728	72
$\frac{3}{16}$.0312	.687	4.58	$\frac{3}{16}$.5625	1152	64
$\frac{1}{4}$.0417	.917	6.11	$\frac{1}{4}$.5833	864	62
$\frac{5}{16}$.0625	1.375	9.17	$\frac{5}{16}$.6	576	60
$\frac{3}{8}$.0833	1.833	12.22	$\frac{3}{8}$.625	432	58
$\frac{1}{2}$.1	2.2	14.67	$\frac{1}{2}$.6667	360	54
$\frac{5}{8}$.125	2.75	18.33	$\frac{5}{8}$.6875	288	52
$\frac{3}{4}$.1667	3.667	24.44	$\frac{3}{4}$.7	216	51
$\frac{7}{8}$.1875	4.125	27.50	$\frac{7}{8}$.75	192	48
$\frac{15}{16}$.2	4.4	29.33	$\frac{15}{16}$.8	180	45
$\frac{1}{1}$.25	5.5	36.67	$\frac{1}{1}$.8125	144	44
$\frac{1}{8}$.3	6.6	44	$\frac{1}{8}$.8333	120	43
$\frac{1}{4}$.3125	6.875	45.83	$\frac{1}{4}$.875	115	41
$\frac{1}{2}$.3333	7.333	48.89	$\frac{1}{2}$.9	108	40
$\frac{3}{4}$.375	8.25	55	$\frac{3}{4}$.9167	96	39
$\frac{7}{8}$.4	8.8	58.67	$\frac{7}{8}$.9375	86	38
$\frac{15}{16}$.4167	9.167	61.11	$\frac{15}{16}$	1	86	36

inclined sides ; the quotient is the force
resistance.

Ex. The breadth of the back or base
being 3 inches, and its inclined sides
required the power necessary to act
so as to separate two substances whose
is equal to 150 lbs.

$$\frac{150 \times 1.5}{10} = 22.5 \text{ lbs.}$$

Note.—When only one of the bodies is moved
breadth of the wedge is taken for the multiplier.

THE SCREW.

The screw, in principle, is that of an
wound around a cylinder which generates
uniform inclination, each revolution produces
or traverse motion equal to the pitch or
distance between two consecutive threads
being the height or angle of inclination
circumference the length of the plane when
not applied ; but the lever being a necessity
of the screw, the circle which is
taken, instead of the screw's circumference

the lever where the power acts, is to the pitch of the screw, so is the force to the resistance.

Ex. 1. Required the effective power obtained by a screw of $\frac{1}{8}$ inch pitch, and moved by a force equal to 50 lbs. at the extremity of a lever 30 inches in length.

$$\frac{30 \times 2 \times 3.1416 \times 50}{.875} = 10760 \text{ lbs.}$$

Ex. 2. Required the power necessary to overcome a resistance equal to 7000 lbs. by a screw of $1\frac{1}{4}$ inch pitch, and moved by a lever 25 inches in length.

$$\frac{7000 \times 1.25}{25 \times 2 \times 3.1416} = 55.73 \text{ lbs. power.}$$

In the case of a screw acting on the periphery of a toothed wheel, the power is to the resistance as the product of the circle's circumference described by the winch or lever, and radius of the wheel, to the product of the screw's pitch, and radius of the axle, or point whence the power is transmitted; but observe, that if the screw consist of more than one helix or thread, the apparent pitch must be increased so many times as there are threads in the screw. *Hence, to find what weight a given power will equipoise:*

Rule.—Multiply together the radius of the wheel, the length of the lever at which the power acts, the magnitude of the power, and the constant number 6.2832; divide the product by the radius of the axle into the pitch of the screw, and the quotient is the weight that the power is equal to.

Ex. What weight will be sustained in equilibrio by a power of 100 lbs. acting at the end of a lever 24 inches in length, the radius of the axle, or point whence the power is transmitted, being 8 inches, the

power and weight.

OF CONTINUOUS CIRCULAR

IN mechanics, circular motion is transferred of *wheels, drums, or pulleys*; and according to driving and driven are of equal or unequal velocities produced so are equal or unequal velocities produced principle on which the following rules are

1. WHEN TIME IS NOT TAKEN INTO

Rule.—Divide the greater diameter, teeth, by the lesser diameter, or number of teeth; the quotient is the number of revolutions the smaller will make for 1 of the greater.

Ex. How many revolutions will a pinion make for 1 of a wheel with 125?

$$125 \div 20 = 6.25, \text{ or } 6\frac{1}{4} \text{ revolution}$$

Note.—Intermediate wheels of whatever diameter

To find the number of revolutions of the last, to 1 of the first, in a train of wheels and pinions.

Rule.—Divide the product of all the teeth in the driving by the product of all the teeth in the driven, and the quotient equal the ratio of velocity required.

Ex. 1. Required the ratio of velocity of the last, to 1 of the first, in the following train of wheels and pinions; viz., *pinions driving*,—the first of which contains 10 teeth, the second 15, and third 18;—*wheels driven*,—first 15 teeth, second 25, and third 32.

$$\frac{10 \times 15 \times 18}{15 \times 25 \times 32} = .225 \text{ of a revolution the wheel will make to 1 of the pinion.}$$

Ex. 2. A wheel of 42 teeth giving motion to one of 12, on which shaft is a pulley of 21 inches diameter, driving one of 6; required the number of revolutions of the last pulley to one of the first wheel.

$$\frac{42 \times 21}{12 \times 6} = 12.25, \text{ or } 12\frac{1}{4} \text{ revolutions.}$$

Note.—Where increase or decrease of velocity is required to be communicated by wheel-work, it has been demonstrated that the number of teeth on each pinion should not be less than 1 to 6 of its wheel, unless there be some other important reason for a higher ratio.

2. WHEN TIME MUST BE REGARDED.

Rule.—Multiply the diameter, or number of teeth in the driver, by its velocity in any given time, and divide the product by the required velocity of the driven; the quotient equal the number of teeth, or diameter of the driven, to produce the velocity required.

Ex. 1. If a wheel containing 84 teeth makes 20 revolutions per minute, how many must another contain to work in contact, and make 60 revolutions in the same time?

$$\frac{84 \times 20}{60} = 28 \text{ teeth.}$$

Ex. 3. required the diameter of
16 revolutions in the same time as
making 36.

$$\frac{24 \times 36}{16} = 54 \text{ inches}$$

*The distance between the centre
two wheels being given, to find their*

Rule.—Divide the greatest velocity
the quotient is the ratio of diameters
bear to each other. Hence, divide
between the centres by the ratio plus
equal the radius of the smaller wheel
the radius thus obtained from the
the centres; the remainder equal to
other.

Ex. The distance of two shafts
centre is 50 inches, and the velocity
revolutions per minute, the other is to
same time; the proper diameters of
pitch lines are required.

$80 \div 25 = 3.2$, ratio of velocity, and $\frac{50}{3.2 + 1}$
of the smaller wheel; then $50 - 11.9 = 38.1$
their diameters are $11.9 \times 2 = 23.8$ and 38.1

attained :—Multiply the given and required velocities together, and the square root of the product is the mean or proportionate velocity.

Ex. Let the given velocity of a wheel containing 54 teeth equal 16 revolutions per minute, and the given diameter of an intermediate pulley equal 25 inches, to obtain a velocity of 81 revolutions in a machine; required the number of teeth in the intermediate wheel, and diameter of the last pulley.

$$\sqrt{81 \times 16} = 36 \text{ mean velocity.}$$

$$\frac{54 \times 16}{36} = 24 \text{ teeth, and } \frac{25 \times 36}{81} = 11.1 \text{ inches, diameter of pulley.}$$

To determine the proportion of wheels for screw-cutting by a Lathe.

In a lathe properly adapted, screws to any degree of pitch, or number of threads in a given length, may be cut by means of a leading screw of any given pitch, accompanied with change wheels and pinions; course pitches being effected generally by means of one wheel and one pinion with a *carrier*, or *intermediate wheel*, which cause no variation or change of motion to take place: hence the following

Rule.—Divide the number of threads in a given length of the screw which is to be cut, by the number of threads in the same length of the leading screw attached to the lathe; and the quotient is the ratio that the wheel on the end of the screw must bear to that on the end of the lathe spindle.

Ex. Let it be required to cut a screw with 5 threads in an inch, the leading screw being of $\frac{1}{2}$ inch pitch, or containing two threads in an inch; what must be the ratio of wheels applied?

$$5 \div 2 = 2.5, \text{ the ratio they must bear to each other.}$$

stud, are commonly designated the *stud-wheel* and *pinion*; but the number and ratio of screw are the same as the rule;—hence, all that is further required upon any 3 wheels at pleasure, the spindle and stud-wheels,—then multiply the number of teeth in the spindle-wheel by the number of teeth in the wheel which is in contact with the spindle-wheel, and by the number of teeth in the wheel which is in contact with the wheel screw; divide the product by the number of teeth in the spindle-wheel, and the number of teeth required in the wheel for the leading screw.

Ex. Suppose a screw is required containing 25 threads in an inch, the spindle before having 2 threads in an inch, and a wheel of 60 teeth is fixed upon the spindle, 20 for the pinion in contact with the spindle-wheel, and 100 for that in contact with the end of the spindle;—required the number of teeth in the wheel for the end of the lead screw.

$$25 \div 2 = 12.5, \text{ and } \frac{60 \times 12.5 \times 20}{100} = 150$$

Or suppose the spindle and screw-

Table of Change Wheels for Screw Cutting, the leading screw being of $\frac{1}{4}$ -inch pitch, or containing 2 threads in an inch.

Number of threads in inch of screw.	Numb. of teeth in		Number of threads in inch of screw.	Number of teeth in				Number of threads in inch of screw.	Number of teeth in			
	Lathe spindle-wheel.	Leading screw-wheel.		Lathe spindle-wheel.	Wheel in contact with spindle-wheel.	Pinion in contact with screw-wheel.	Leading screw-wheel.		Lathe spindle-wheel.	Wheel in contact with spindle-wheel.	Pinion in contact with screw-wheel.	Leading screw-wheel.
1	80	40	$8\frac{1}{2}$	40	55	20	60	19	50	95	20	100
$1\frac{1}{4}$	80	50	$8\frac{1}{2}$	90	85	20	90	$19\frac{1}{2}$	80	120	20	130
$1\frac{1}{2}$	80	60	$8\frac{3}{4}$	60	70	20	75	20	60	100	20	120
$1\frac{3}{4}$	80	70	$9\frac{1}{2}$	90	90	20	95	$20\frac{1}{4}$	40	90	20	90
2	80	90	$9\frac{3}{4}$	40	60	20	65	21	80	120	20	140
$2\frac{1}{4}$	80	90	10	60	75	20	80	22	60	110	20	120
$2\frac{1}{2}$	80	100	$10\frac{1}{2}$	50	70	20	75	$22\frac{1}{2}$	80	120	20	150
$2\frac{3}{4}$	80	110	11	60	55	20	120	$22\frac{3}{4}$	80	130	20	140
3	80	120	12	90	90	20	120	$23\frac{1}{4}$	40	95	20	100
$3\frac{1}{4}$	80	130	$12\frac{3}{4}$	60	85	20	90	24	65	120	20	130
$3\frac{1}{2}$	80	140	13	90	90	20	130	25	60	100	20	150
$3\frac{3}{4}$	80	150	$13\frac{1}{2}$	60	90	20	90	$25\frac{1}{2}$	30	85	20	90
4	40	80	$13\frac{3}{4}$	80	100	20	110	26	70	130	20	140
$4\frac{1}{4}$	40	85	14	90	90	20	140	27	40	90	20	120
$4\frac{1}{2}$	40	90	$14\frac{1}{2}$	60	90	20	95	$27\frac{1}{2}$	40	100	20	110
$4\frac{3}{4}$	40	95	15	90	90	20	150	28	75	140	20	150
5	40	100	16	60	80	20	120	$28\frac{1}{4}$	30	90	20	95
$5\frac{1}{2}$	40	110	$16\frac{1}{2}$	80	100	20	130	30	70	140	20	150
6	40	120	$16\frac{3}{4}$	80	110	20	120	32	30	80	20	120
$6\frac{1}{4}$	40	130	17	45	85	20	90	33	40	110	20	120
7	40	140	$17\frac{1}{2}$	80	100	20	140	34	30	85	20	120
$7\frac{1}{2}$	40	150	18	40	60	20	120	35	60	140	20	150
8	30	120	$18\frac{3}{4}$	80	100	20	150	36	30	90	20	120

Table of the Diameters of Wheels—continued.

Pitch of the teeth in inches.											
$\frac{1}{2}$	$1\frac{1}{2}$	$1\frac{3}{4}$	$1\frac{1}{2}$	$1\frac{1}{4}$	$1\frac{1}{2}$	$1\frac{3}{4}$	$1\frac{1}{2}$	$1\frac{1}{4}$	$1\frac{1}{2}$	$2\frac{1}{4}$	$2\frac{1}{2}$
Diameter at the pitch circle in feet and inches.											
$10\frac{1}{2}$	1	0	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$11\frac{1}{2}$	1	$0\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$11\frac{1}{2}$	1	0	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$11\frac{1}{2}$	1	$1\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$0\frac{1}{2}$	1	$1\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$0\frac{1}{2}$	1	$1\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
1	1	$2\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$1\frac{1}{2}$	1	$2\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$1\frac{1}{2}$	1	$3\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
2	1	$3\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$2\frac{1}{2}$	1	$4\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$2\frac{1}{2}$	1	$4\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
3	1	$4\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$3\frac{1}{2}$	1	$5\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$
$3\frac{1}{2}$	1	$5\frac{1}{2}$	$1\frac{1}{2}$	1	$1\frac{1}{2}$	1	$2\frac{1}{2}$	1	$3\frac{1}{2}$	1	$4\frac{1}{2}$

Table of the Diameters of Wheels—continued.

[illegible]

is alike.

4. That when unguents are interposed, the friction depends more upon the nature of the unguent than upon that of the surfaces of contact, and hence, that the nature of the unguent to be used must be governed by the pressure or resistance. Mr. Rennie found, that with the unguents used for anti-attribution, on axles under a pressure of 5 cwt., the friction did not exceed $\frac{1}{9}$ th of the pressure ; but when softer unguents were used, as oil, hog's-lard, &c., the ratio of the friction to the pressure considerably increased ; from which it was naturally inferred that the consistence of a unguent ought just to prevent the bodies coming in contact with each other.

5. That the friction of metals, without a unguent interposed, varies as their hardness ; harder metals producing less friction than the soft.

6. That without unguents, and within the limits of 32 $\frac{1}{2}$ lbs. pressure per square inch, the friction of metals upon hard metals may very generally be estimated at about $\frac{1}{6}$ th of the whole pressure.

7. That within the limits of their abrasion, the friction of metals is nearly alike ; but from 14

property, repeating the number of times the end of the ram exceeds the of the pump.

Ex. Required the repulsive force of a 6-inch when a power of 50lbs. is applied to the end of lever, which is as 12 to 1 in effect, and the dia of the pump or plunger $\frac{7}{8}$ ths of an inch.

$$\text{Area of ram} = \frac{28 \cdot 2744}{6013} = 47;$$

$$\text{Area of pump} = \frac{6013}{50 \times 12 \times 47} = 28200 \text{ lbs., or 12 tons nearly.}$$

When a body is partly or wholly immersed in or other fluid, the vertical pressure of the fluid to raise the body with a force equal to the weight of the fluid displaced; hence the weight of any placed quantity of a fluid by a buoyant body the weight of that body.

Ex. 1. Suppose a vessel with all its masts, and general equipments, is found to displace cubic feet of sea water, what is the whole weight of the vessel?

$$\begin{array}{l} \text{Sea water average 64 lbs. per cubic foot.} \\ \frac{35000 \times 64}{2240} = 1000 \text{ tons.} \end{array}$$

and this contraction of the stream reduces the area of its section from 1 to .619, or nearly $\frac{2}{3}$ the area of the short parallel tube be attached, the vein of the stream is less contracted, and the area will equal .762 of the area of the tube attached be the frustum of a cone whose greater end is the aperture, the length equal to the diameter of the aperture, and the area of the smaller end to the area of the larger as 1 to 1.6, there will be no contraction of the vein: hence the proper way of making the pipe in this form from a reservoir or head of water, through which the greatest quantity of water according to its area, is required to pass.

To find the velocity of water issuing through a circular orifice at any given depth from the surface.

Rule.—Multiply the square root of the head to the centre of the orifice by 8.1, and the product is the velocity of the issuing fluid in feet per second.

Ex. Required the velocity of water issuing from an orifice under a head of 11 feet from the surface.

$$\sqrt{11} = 3.3166 \times 8.1 = 26.864 \text{ feet, velocity per second}$$

— If the orifice be rectangular

either by making the stream of water a few inches narrower than the wheel, or otherwise.

3. That because of water producing a less efficient power by impulse than gravity, turbines, or machines through which the motion is obtained by reaction, are greatly preferable to undershot, or low breast wheels.

4. That a head* of water is required sufficient to cause the velocity of its flowing to be as 3 to 2 of the wheel; $\frac{1}{4}$ th of the wheel's diameter being an approximate height, near enough for practical purposes.

5. That the effective power of a wheel constructed according to these restrictions is equal to the product of the number of cubic feet, and velocity in feet per minute, multiplied into $\cdot 001325$.

Example for general illustration

Suppose a fall of water 25 feet in height, over which is delivered 112 cubic feet per minute; required the various peculiar requisites for a wheel to be in accordance with the preceding rules.

1st. $25 \times 1\cdot08 = 27$ feet, the wheel's diameter.

2nd. $\sqrt{25} \times 2 = 10$ feet, velocity of the wheel in ft. per second.

Also $27 \times 2\cdot1 = 56\cdot7$, say 57 buckets.

3rd. $27 \div 9 = 3$ feet, head of water required.

4th. $112 \times 10 \times 60 \times \cdot 001325 = 89$ horses' power.

The *turbine* of Fourneyron, in France, and the patented *Water-Mill* of Whitelaw and Stirrat, Scotland, have of late years attracted a considerable share of public attention, their simplicity of construction and asserted effects in like situations being equal to those of the best applied water-wheels. In their manner of construction, they differ, but in principle they are the same; the action of each being created by a centrifugal and tangential force, caused by the weight or impulsion of a column

* By head is meant the distance from the surface of the water to the centre of the wheel.

in a right line with the centre of the wheel.

In 1838 a number of experiments were made in France by Morin, with a view to the more introduction of turbines, and a positive proof of their superior qualities in preference to wheels of the latter kind, which terminated considerably in favour of the former, and from which the following deductions were made:

1. That turbines are equally adapted to small falls of water.

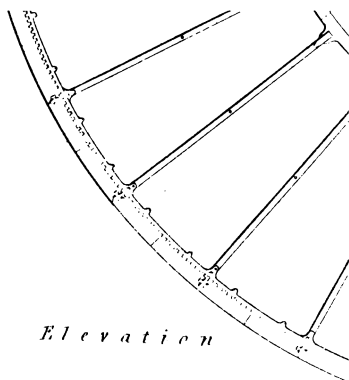
2. That they are capable of transmitting the effect to from 70 to 78 per cent. of the absolute effect.

3. That their velocities may vary very considerably from the maximum effect, without differing sensibly from it.

4. That they will work nearly as effectually drowned to the depth of 5 or 6 feet, as when they are not; consequently, they will make use of the whole fall when placed below the level of extreme low water.

5. That they may receive variable quantities of water without altering the ratio of the power to the effect. Corresponding results have also been obtained by Whitelaw and Stirrat's machine: the same may be said of the one is equally applicable to the other.

General Rule by Mr. Whitelaw, whereby the power of a turbine may be determined from the fall of water.



Elevation



63	20-082	112	35-655	160	50-933	208
64	20-380	113	35-974	161	51-251	209
65	20-698	114	36-292	162	51-569	210
66	21-016	115	36-611	163	51-888	211
67	21-335	116	36-929	164	52-206	212
68	21-653	117	37-247	165	52-524	213
69	21-971	118	37-565	166	52-843	214
70	22-289	119	37-883	167	53-161	215
71	22-607	120	38-202	168	53-479	216
72	22-926	121	38-520	169	53-798	217
73	23-244	122	38-838	170	54-116	218
74	23-562	123	39-156	171	54-434	219
75	23-880	124	39-475	172	54-752	220
76	24-198	125	39-793	173	55-071	221
77	24-517	126	40-111	174	55-389	222
78	24-835	127	40-429	175	55-707	223
79	25-153	128	40-748	176	56-026	224
80	25-471	129	41-066	177	56-344	225
81	25-790	130	41-384	178	56-662	226
82	26-108	131	41-703	179	56-980	227
83	26-426	132	42-021	180	57-299	228
84	26-741	133	42-339	181	57-617	229
85	27-063	134	42-657	182	57-935	230
86	27-381	135	42-976	183	58-253	231
87	27-699	136	43-294	184	58-572	232
88	28-017	137	43-612	185	58-890	233
89	28-336	138	43-931	186	59-209	234
90	28-654	139	44-249	187	59-527	235
91	28-972	140	44-567	188	59-845	236
92	29-290	141	44-885	189	60-163	237
93	29-608	142	45-204	190	60-482	238
94	29-927	143	45-522	191	60-800	239
95	30-245	144	45-840	192	61-118	240
96	30-563	145	46-158	193	61-436	241
97	30-881	146	46-477	194	61-755	242
98	31-200	147	46-795	195	62-073	243
99	31-518	148	47-113	196	62-392	244
100	31-836	149	47-432	197	62-710	245
101	32-155	150	47-750	198		

For cross cutting, round or square mill,
principle of the stone mill, framed, with 1
wheels, &c.

Steel, for wheat, barley, oats, peas, beans, &c
do. do. do.

Sugar, cattle, for the West Indies, &c. The 1
strong iron frame. 5 feet long, and 2 feet di
work in a horizontal position, including the
to work the mill, with the wood arms, sw
for the cattle to draw from, complete

rollers, 4½ feet long, and 2 feet diameter..

do. 4 do. 1½ do. ..

do. 3½ do. 1½ do. ..

do. 3 do. 1½ do. ..

Sugar, for a steam engine,

rollers, 5 feet long, and 2 feet diameter..

do. 4½ do. 2 do. ..

do. 4 do. 2 do. ..

do. 3½ do. 2 do. ..

do. 3 do. 2 do. ..

do. 3 do. 2 do. ..

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2	10	18	8	226
2½	20	18½	8½	239
3	24	22½	9	252
3½	28	26½	9½	267
4	32	31½	10	282
4½	36	35½	10½	297
5	44	40	11	312
5½	50	45½	11½	327
6	57	51	12	342
6½	64	56½		357
7	71	62		372
	78	69		387
	86	76		402
	94	83		417
	102	90		432
	112	98		447
	122	107		462
	132	115		477
	142	124		492
	153			507

shafts, up to 2 inches, square or r
bearings, turned

2 inches to 2½ inches

2½ do. 4 do.

4 do. 6 do.

6 do. 9 do.

9 do. 12 do.

Where shafts are turned
to the bearing at each en
blocks, such additional
measured and charged at
tion to the price of the sh

Shafts, of wood,
elm, of all sizes

fir do.

oak, up to 18 inches

ditto 2 feet

the above includes mo
gudgeons.

measure the largest

the charging dimension

turned

with staves.

MACHINERY, AND LABOUR.

251

MILLWRIGHT'S WORK,

£ s. d.

Water wheel work, &c.,		
oak starts, 8½ by 2	per foot run	0 1 6
floats and back boards of elm, prepared to size		
	per foot super.	0 0 10
over shot wheels, rings, and arms ready made, the		
rings 8 in. wide and 8 in. thick ..	per foot diam.	2 7 0
elm sole boards, risers, and buckets, per foot super.		0 0 10
wrought iron floats bent to order.....	per lb.	0 0 10
Wheels, bevel, of wood, for the bevel, charge additional		
	per foot	0 5 0
windmill brakes, 9 inches wide.....	per foot diam.	1 15 0
maltmill heads, with staves	do.	8 0 0
wallowers, with ditto	do.	8 17 0
spur nuts of elm, of 2 to 4 inch plank	do.	8 10 0
the cogs, in all cases, to be charged extra.		

Wheels, of cast iron, both tooth and mortis, geared, pitched, chipped and filed, the pattern included in the price.

width of cog, pr. ft. diam.		width of cog, per ft. diam.	
1 inch	£3 8 0	8½ inches.....	11 12 6
1½	8 5 0	9	12 0 0
1½	8 10 0	9½	12 5 0
1½	8 15 0	9½	12 10 0
2	4 0 0	9½	12 15 0
2½	4 5 0	10	13 0 0
2½	4 10 0	10½	13 5 0
2½	4 15 0	10½	13 10 0
3	5 0 0	10½	13 15 0
3½	5 5 0	11	14 0 0
3½	5 10 0	11½	14 10 0
3½	5 15 0	11½	15 0 0
4	6 0 0	11½	15 10 0
4½	6 7 6	12	16 0 0
4½	6 15 0	12½	17 0 0
4½	7 2 6	12½	18 0 0
5	7 10 0	12½	19 0 0
5½	7 12 6	13	20 0 0
5½	7 15 0	13½	20 10 0
5½	7 17 6	13½	21 0 0
6	8 0 0	13½	21 10 0
6½	8 5 0	14	22 0 0
6½	8 10 0	14½	22 10 0
6½	8 15 0	14½	23 0 0
7	9 0 0	14½	23 10 0
7½	9 7 6	15	24 0 0
7½	9 15 0	15½	24 10 0
7½	10 2 6	15½	25 0 0
8	10 10 0	15½	25 10 0
8½	10 17 6	16	26 0 0
8½	11 5 0		

Wheels, lantern, made solid, and fitted together in two pieces, or halves, with wrought iron hoops and copper screws, &c.

7 inches deep over all	per foot diam.	7 0 0
8	do.	8 0 0
9	do.	9 0 0

width
 foreign live oak, shanked as before ..
 ditto, above 3 inches wide, extra per
 width
 for wood wheels, not exceeding 12 in.
 addition to the foregoing prices ..
 labour, shanking
 patterns for wheels, all above 18 in.

width of cog, pr. ft. diam.			width of cog,
1 inch	£0	9 6	7½
1½	0	9 9	8
1½	0	10 0	8½
1½	0	10 3	8½
2	0	10 6	8½
2½	0	10 9	9
2½	0	11 0	9½
2½	0	11 3	9½
3	0	11 6	9½
3½	0	11 9	10
3½	0	12 0	10½
3½	0	12 3	10½
4	0	12 6	10½
4½	0	12 9	11
4½	0	13 0	11½
4½	0	13 6	11½
5	0	14 0	11½
5½	0	14 6	12
5½	0	15 0	12½
5½	0	15 6	12½
6	0	16 0	12½
6½	0	16 6	13
6½	0	17 0	13½
6½	0	17 6	13½
7	0	18 0	13½
7½	0	18 6	14
7½	0	19 0	

riggers of wood,
 above 20 inches diameter, single gro
 made of 4-inch elm

10½	8 9 0	18½
11	8 10 0	14
11½	8 12 6		

pitching and trimming, including filing, p. in.
measurement to be taken from the pattern
and not from the wheel.

wheels of wood,

a horse wheel, of any diam., 4 in. thick, per ft

do.	5	do.	do.
do.	6	do.	do.
do.	7	do.	do.
do.	8	do.	do.

The cogs to be charged extra.

PRICES OF PORTABLE STEAM-ENGINE TUBULAR BOILERS COMPLETE

Horse-power.	Diameter of Cylinder.	Length of stroke.
1	3 inches.	6½ inches.
2	4½ "	9 "
3	5½ "	11 "
4	6½ "	13 "
5	7½ "	14 "
7	8½ "	14 "
9	9½ "	16 "
11	10½ "	18 "
13	11½ "	20 "
16	13 "	22 "
20	14½ "	24 "

The following formulæ, with some modification and improvement, are extracted from Nystrom's Mechanics, an American publication designed for the use of engineers. To render them more generally available to the practical workman, they are reduced, at page 268, &c., to the form of verbal rules, each of which is to be employed in connection with the figure to which the number prefixed to the rule refers.

HYDRAULICS.

Let the vessel *A*, Fig I., be kept constantly full of water up to the water line *w*. In two horizontal faces lower than the water line *w*, are made orifices *a* and *a'*, through which the water will pass up vertical nearly to the water line *w*. Omitting the resistance of air, &c., the jet should theoretically reach the water line *w*; practically it reaches $0.967h$.

It is evident that the velocity of the jet through the orifices, must be the velocity due to a body falling the height *h*, according to the law of force of gravity.

Letters denote.

Q = actual quantity of water discharged per second or in the time *t*, in cubic feet.

h = head, or height of water over the orifice.

t = operating time in seconds.

a = area of the orifice in square feet.

m = the coefficient for contraction. (See Table, p. 261).

G = gallons of 277 cubic inches discharged in the time *t*.

V = velocity through the orifice in feet per second.

Example 1. Fig. I. How many gallons of water will be discharged in five minutes, through

Fig. III. n = number of down minute, s = stroke of piston ; the air ves at the pressure of the atmosphere.

Example 2. Fig. III. How many d must be made per minute by the leve pump, to throw up 22 cubic feet of v high, in the time of 8 minutes and the lever $l = 30$ inches, $e = 8$ inches, $F = 20$ pounds ? $8 \times 60 + 15 = 495$ s

$$n = \frac{3630 Q h' e}{t s F l} = \frac{3630 \times 22 \times 18 \times 8}{495 \times 0.6 \times 20 \times 30} = 64.5 \text{ st}$$

Example 3. Fig. XI. A vessel c form is of dimensions $A = 6$ square f $h = 5$ feet. What time will it take t to sink 2 feet, when the orifice $a =$ feet ?

$$t = \frac{A (\sqrt{h} - \sqrt{h'})}{4 \times 64 a} = \frac{6 (\sqrt{5} - \sqrt{3})}{2.56 \times .212}$$

MOTION OF WATER IN PI

Letters denote.

L = extreme length of the pipe in

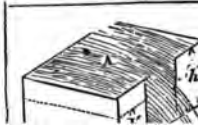
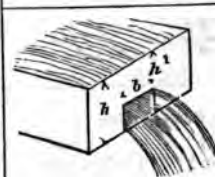
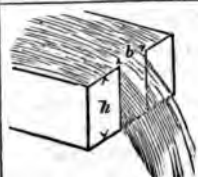
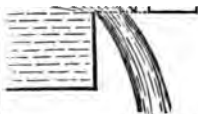
d = inside diameter in feet, and ur

ut the length L .

diameter, and $L=68$ feet long, the head pressure of water being $h=8$ feet?

$$V=48 \sqrt{\frac{0.45 \times 8}{68 + 50 \times 0.45}} = 9.6 \text{ feet per second.}$$

	<p>I.</p> $V = 8.02 \sqrt{h}$ $Q = m a t 8.02 \sqrt{h} = 5.05 a t \sqrt{h}$ $G = 31.5 a t \sqrt{h}, \quad m = 0.63, \quad \text{jet} = 0.967 h,$ $h = \frac{Q^2}{25.5 a^2 t^2}, \quad = h'.$
	<p>II.</p> $V = 1.015 \sqrt{\frac{P}{A}}, \quad Q = a t \sqrt{\frac{P}{A}},$ $G = 6.2 a t \sqrt{\frac{P}{A}}, \quad h' = \frac{P}{64.6 A}.$
	<p>III.</p> $Q = a t \sqrt{\frac{F l}{A e}}, \quad n = \frac{3630 Q h' e}{t s F l},$ $G = 6.2 a t \sqrt{\frac{F l}{A e}}, \quad h' = \frac{F l}{64.6 A e}.$
	<p>IV. <i>Motion of Water in Pipes.</i></p> $V = 48 \sqrt{\frac{d h}{L + 50 d}}, \quad Q = 37.7 d^2 \sqrt{\frac{d h}{L + 50 d}},$ $d = 0.24 \sqrt[5]{\frac{L Q^2}{h}}, \quad h = \frac{Q^2 (L + 50 d)}{1421 d^5}.$
	<p>V. <i>Motion of Water in Pipes.</i></p> $V = 6.86 \sqrt{\frac{d F}{D(L + 50 d)}}, \quad Q = 5.38 d^2 \sqrt{\frac{d F}{D(L + 50 d)}},$ $d = 1.68 \sqrt[5]{\frac{L D Q^2}{F}}, \quad F = \frac{Q^2 D(L + 50 d)}{29 d^5}.$



WEIR.

$Q = k b t$. See Table for W .

$$t = \frac{Q}{k b}, \quad b = \frac{Q}{k t}$$

VIII.

$$Q = 5.35 m b h t \sqrt{h}$$

$$G = 33 m b h t \sqrt{h}$$

$$t = \frac{Q}{5.35 m b h \sqrt{h}}$$

IX.

$$Q = 5.35 m b t (h \sqrt{h} - h'^2)$$

$$G = 33 m b t (h \sqrt{h} - h'^2)$$

$$t = \frac{Q}{5.35 m b (h \sqrt{h} - h'^2)}$$

X.

$$t = \frac{0.95 m A (\sqrt{h} - h')}{b \sqrt{h h'}}$$

A = area of the vessel in sq

Example 5. Fig. VI. Required the quantity of water discharged in a long pipe of $L=135$ feet long, and $d=0.17$ feet, a hand-pump of $D=0.2$ feet in diameter, and the end of the pipe elevated above the piston D ?

$$V = 6.86 \sqrt{\frac{0.17(44 - 49 \times 0.2^2 \times 20)}{0.2(135 + 50 \times 0.17)}} = 1.95 \text{ feet}$$

$$Q = 1.95 \times 5.38 \times 0.2^2 = 0.042 \text{ per second} \times 6 \text{ feet per minute.}$$

$$s = 0.8 \text{ feet the stroke of piston, we shall have}$$

$$n = \frac{2.52}{0.8 \times 0.785 \times 0.2^2} = 100 \text{ strokes per}$$

TABLE FOR WATER FLOWING OVER

This Table is set up from careful experiments on a large scale, and is suited for weirs of various heights.

<i>h.</i> inches.	<i>h.</i> feet.	<i>m.</i>	<i>k.</i>
0.4	0.033	0.424	0.0136
0.8	0.066	0.417	0.0544
1.2	0.100	0.412	0.1251
1.6	0.133	0.407	0.166
2.4	0.200	0.401	0.291
3.2	0.266	0.397	0.444
4.	0.333	0.395	0.631
	0.500	0.393	1.129

Rule. Multiply the width b in feet, of the *weir*, by the coefficient k , and the product is the quantity of water discharged per second, in cubic feet. h is the height as represented by Fig. VII. The width b should be $b > h$.

Example 6. How much water will flow over a weir of $b=5$ feet, $h=0.5$ feet in one minute?

$$Q = k b t = 1.1295 \times 5 \times 60 = 338.35 \text{ cubic feet.}$$

HYDRODYNAMICS.—WATER POWER.

The natural effect concentrated in a fall of water, is equal to the weight of the quantity of water passed through per second multiplied by the vertical space it falls.

Fig. XII. Let Q be the quantity of water which passes through the orifice a in the time $t=1$ second, in cubic feet of 62.5 pounds each.

h = the vertical space the water falls; then the value or natural effect of the fall is at the orifice a ,

$$P = 62.5 Q h, \text{ effects.}$$

But,

$$Q = 5.06 a \sqrt{h}, \text{ then we have}$$

$$P = 315.5 a h \sqrt{h}.$$

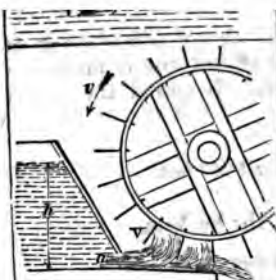
This will be in horse-power,

$$H = 0.573 a h \sqrt{h}, \quad h = \frac{1}{1.07} \sqrt[3]{\frac{H^2}{a^2}},$$

$$H = 0.1134 Q h, \quad h = \frac{H}{0.1134 Q}.$$

Example 1. In a creek passes 18 cubic feet of water per second. How high must that creek be dammed up to produce an effect of 10 horses?

$$h = \frac{10}{0.1134 \times 18} = 4.9 \text{ feet, the answer.}$$



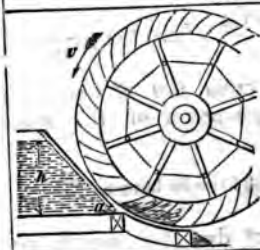
XVII.

Undersh

$$H = \frac{Q v}{454}$$

$$H = \frac{m a v}{86.8}$$

When $V = 2v$, al



XVIII.

Poncelet

$$H = \frac{Q v}{228} (V -$$

$$H = \frac{Q v}{197} (V -$$

$$Q = 8ma \sqrt{h},$$



XIX.

Breast-Wheel

number of seconds, the product is the number of gallons discharged.

For the number of cubic feet discharged in a given number of seconds.—**RULE:** Multiply the area of the orifice in square feet by the number of seconds, and the product by 5.05 times the square root of the head of water.

For the number of gallons discharged in a given number of seconds. Multiply the area of the orifice by the number of seconds, and the product by 31.5 times the square root of the height of the head.

For the height of the head of water from the discharge of a given number of cubic feet in a given time. Divide the number of cubic feet discharged by the number of seconds in that time, and the quotient will be the height in feet.

NOTE.—To allow for the resistance of the water, the height of the head of water should be multiplied by .967; the product is the height of the jet.

II. Velocity.—**RULE:** Let the weight of a column of water which, pressing on the orifice, would produce the jet, be expressed in pounds, and divide the number of these pounds by

Divide the former product by the same quotient will be the height of the jet pressure on A.

RULES FOR THE MOTION OF WATER

IV. For the velocity of delivery.—RULE: Take the inner diameter of the pipe in feet by 10 feet of the head of water above the point of delivery. Add the entire length of the pipe in feet to the square of the inner diameter. Divide the former sum by the sum. Extract the square root of the result and multiply that root by 48.

For the cubic feet delivered in a second.—RULE: Take the square root found above, and multiply it by 37.7 times the square of the diameter of the pipe; the product will be the number of cubic feet discharged in a second.

For the diameter of the pipe.—RULE: Take the square of the number of cubic feet delivered in a second, found as above, by the length of the pipe in feet. Divide the product by the height of the head above delivery; take the fifth root of the result; multiply it by .24; the product will be the diameter of the pipe in feet.

meter, and multiply the sum by the square of the number of cubic feet discharged in a second. Divide the product by 1421 times the fifth power of the diameter; and the quotient will be the height of the head.

V. For the velocity of the discharge.—**RULE:** Multiply the force in pounds acting on the piston by the inner diameter of the pipe. Multiply the length of the pipe increased by 50 times its diameter by the diameter of the piston—all the measures being taken in feet. Divide the former product by the latter, and multiply the square root of the quotient by 6.86; the product will be the velocity per second in feet.

For the cubic feet delivered per second.—**RULE:** Multiply the square root, found as above, by 5.38 times the square of the inner diameter of the pipe in feet; the product will be the number of cubic feet delivered.

For the diameter of the pipe.—**RULE:** Multiply together the length of the pipe, the diameter of the piston, and the square of the number of cubic feet discharged per second. Divide the product by the force in pounds acting on the piston, and multiply the fifth root of the quotient by 1.68; the product will be the diameter in feet.

For the force applied to the piston.—**RULE:** Multiply the length of the pipe increased by 50 times its diameter by the diameter of the piston, and by the square of the number of cubic feet delivered in a second. Multiply the fifth power of the diameter of the pipe by 29. Divide the former product by the latter; the quotient will be the force in pounds acting on the piston.

product by this, and multiply the square root of the quotient by 6.86; the result will be the velocity in feet per second of the issuing water.

For the cubic feet delivered.—**RULE:** Multiply together the velocity determined as above, the area of the inner diameter of the pipe, the time in seconds, and the number 5.38; the result will be the number of cubic feet delivered at that time.

For the height above the end of the pipe the water spouts.—**RULE:** Divide the square of the issuing velocity by 66.5, the quotient will be the height in feet, allowing for the resistance of the air.

Or, multiply the number of strokes per minute by the length of the stroke, and the square of the diameter of the piston: the product by the diameter of the piston: the result by 57.65 times the inner diameter of the pipe.

For the number of strokes of the piston (see ex. 5).—**RULE:** Multiply together the square of the stroke, the square of the diameter of the piston, and the number .785, and divide the result by the number of cubic feet discharged per minute by the pump.

RULES FOR WEIRS (See the Table,

VII. For the cubic feet discharged in

of seconds —

table, and the number 5·35. The product of the five numbers will be the number of seconds discharged.

For the number of gallons discharged. Take the product of the first four multipliers multiplied together in the preceding rule, and multiply by the fifth multiplier there used, multiplier 33; the product of the five numbers will be the number of gallons discharged in the time.

For the time of discharging a given quantity of water from a vessel. — **RULE:** Multiply the height of the water-level above the bottom of the vessel by the square root of that height. Multiply the product by the square root of the area of the aperture, the product from the former. Multiply the product by the width of the aperture, the product will be the number of cubic feet discharged by this aperture in the time. Divide the product by the number 5·35. The quotient will be the number of seconds.

X. For the time in which a body will sink through a given space. — Find the square root of the entire height

area of the surface of the inclosed water in square feet, by the number m from the table, and by the number .95. Multiply the square root of the product of the two heights by the width of the aperture. Divide the former product by the latter, and the quotient will be the number of seconds in the time.

XI. *For the time in which the water level will sink through a given space.*—**RULE:** From the square root of the height of the vessel subtract the square root of the height of the water level after sinking the proposed space. Multiply the remainder by the area of the water surface, and divide the product by four times the area of the orifice multiplied by m taken from the table.

For the number of cubic feet discharged in this time.—**RULE:** Add the two square roots instead of subtracting them as above, and multiply the sum by four times the area of the orifice, by the number of seconds, and by the number m from the table.

Or, multiply the difference of the two heights by the area of the water surface, or of the bottom of the vessel; the product will be the number of cubic feet discharged.

RULES FOR THE SHORT DRAIN.

XII. *For the velocity at the orifice or entrance of the drain.*—**RULE:** Multiply the square root of the height of the water-level above the orifice by 8. Divide 1 by m , taken from the table, subtract from the quotient, and take the square of the remainder; increase this square by 1, and then take the square root of the sum. The before-found

square of it. Add the
height of the orifice above the mouth
and take the square root of the sum.

*For the number of cubic feet discharged
time.*—**RULE**: Multiply together the
orifice, the area of the orifice, the number
in the time, and the number m taken in

NOTE.—The length of this drain is the
square root of the area of the orifice.

RULES FOR THE LONG DRAIN

XIII. *For the velocity at the orifice
the drain.*—**RULE**; As the length of
nothing to do with the velocity with
enters it, the **RULE** will obviously be
given above for the short drain.

*For the velocity with which the water
enters the drain.* **RULE**: To the square of the velocity
water enters the drain, add 64.32
of the point of entrance above the
note the sum. Add the width of
the depth of water flowing along
the length of the drain, 1

RULES FOR THE PARABOLIC VEIN.

XIV. *For the horizontal distance spouted on any plane.*—RULE: Multiply together the height of the water-level above the orifice, and the height of the orifice above the horizontal plane, and take twice the square root of the product.

For the velocity with which the water strikes the horizontal plane.—RULE: Add together the two heights mentioned above, and take eight times the square root of the sum.

For the number of cubic feet discharged in any time.—RULE: Multiply together the area of the orifice, the seconds in the time, the square root of the height of the orifice above the water level, and eight times the number m taken from the table for the contracted vein.

For the height of the head of water above the orifice necessary to cause the water to spout a given distance on a given horizontal plane.—RULE: Divide the square of the given distance by four times the height of the orifice above the given plane; the quotient will be the height of the head.

XV. The rules for the velocity and number of cubic feet discharged are the same as in the former case.

RULES FOR WATER WHEELS, FROM THE FORMULÆ.

XVI. *For the horse-power of the under-shot wheel in mid stream.*—RULE: Subtract the velocity of the wheel from the velocity of the stream. Multiply the square of the remainder by the area of the float and the velocity of the wheel. Divide the product by 200; the quotient will be the horse-power.

For the horse-power when the wheel moves with

issuing stream and that of the
velocity, and also by the number of
water acting on the wheel per second
product by 454, the quotient will be
power. **RULE 2:** Multiply the diff
velocities by the velocity of the whee
the aperture, the square root of the
head of water, and the number m ta
table for the vein, and divide the produ

*For the horse-power when the v
issuing stream is double that of the w*
Multiply together the area of the
height of the head, and the square
height. Divide the product by .47
will be the horse-power.

XVIII. *For the horse-power when
head of water exceeds five feet.*—R
the difference of the velocities by the
wheel and the number of cubic feet
upon it per second; and divide the

When the height of the head is less
RULE: Proceed as above, using, ho
ber 197 for the divisor instead of 2
of cubic feet of wa

and divide the product by 21·5. Add the height of the head above the lowest bucket to the result, multiply the sum by the number of cubic feet acting on the buckets in a sec., and divide the result by 13·7.

For the number of revolutions per minute.—

RULE: Divide 100 by the diameter of the wheel, or distance between the centres of pressure of opposite buckets. Add 35 to the quotient, and the sum will express the number of revolutions per minute.

RULES FOR THE SAW-MILL WHEEL.

XXIII. *For the horse-power.—***RULE:** Multiply the difference between the velocity of the water acting on the wheel and the velocity of the wheel itself by the latter velocity, and by the number of cubic feet acting on the buckets in a sec. Divide the result by 200; the quotient will be the horse-power.

*For the proper diameter of the wheel.—***RULE:** Multiply the square root of the height of the head of water above the lowest bucket by 100, and divide the product by the number of revolutions per minute.

Effects produced by water in an aëriform state.

When water in a vessel is subjected to the action of fire, it readily imbibes the heat of which the fire is the cause, and sooner or later attains a temperature of 212° Fahrenheit. If at this temperature the water be not enclosed, but exposed to atmospheric pressure, ebullition will take place, and steam will ascend through the water, carrying with it the superabundant heat. Water, in attaining the aëriform state, thus obeys the same laws under every degree of pressure; but as the pressure is augmented, so is the indicated temperature proportionately raised; hence the various densities of steam, and degrees of elastic force.

15	6.80	30.60	77.8	216.3	81.9	102.4	1
16	7.26	32.64	829	219.6	83.3	104.2	1
17	7.71	34.68	880	222.7	84.7	105.9	1
18	8.16	36.72	932	225.6	86.0	107.6	1
19	8.62	38.76	984	228.5	87.3	109.2	1
20	9.07	40.80	1.037	231.2	88.5	110.7	1
21	9.52	42.84	1.089	233.8	89.7	112.1	1
22	9.98	44.88	1.140	236.3	90.8	113.5	1
23	10.43	46.92	1.192	238.7	91.9	114.8	1
24	10.88	48.96	1.244	241.0	93.0	116.1	1
25	11.34	51.00	1.296	243.3	93.9	117.4	1
26	11.79	53.04	1.348	245.5	94.9	118.6	
27	12.25	55.08	1.400	247.6	95.8	119.8	
28	12.70	57.12	1.452	249.6	96.7	120.9	
29	13.15	59.16	1.503	251.6	97.6	122.0	
30	13.61	61.21	1.555	253.6	98.5	123.1	
31	14.06	63.24	1.607	255.5	99.3	124.2	
32	14.51	65.28	1.659	257.3	100.1	125.2	
33	14.97	67.32	1.711	259.1	100.9	126.2	
34	15.42	69.36	1.763	260.9	101.7	127.2	
35	15.87	71.40	1.814	262.6	102.5	128.1	
36	16.33	73.44	1.866	264.3	103.2	129.1	
37	16.78	75.48	1.918	265.9	104.0	129.9	
38	17.23	77.52	1.970	267.5	104.7	130.8	
39	17.69	79.56	2.022	269.1	105.4	131.7	
40	18.14	81.60	2.074	270.6	106.0	132.6	
41	18.59	83.64	2.126	272.1	106.7	133.4	
42	19.05	85.68	2.178	273.6	107.4	134.2	
43	19.50	87.72	2.229	275.0	108.0	135.0	
44	19.96	89.76	2.281	276.4	108.6	135.8	

The preceding Table is peculiarly adapted for estimating the power of steam engines on the condensing principle, because in such the effective force of the steam is the difference between the total force and the resisting vapour retained in the condenser. The following Table is more adapted for estimating the effects of non-condensing engines, as, in such, the atmospheric pressure is not generally taken into account, engines of this principle being supposed to work in a medium; or, the atmospheric pressure on the boiler, to cause a greater density of steam, is equal to the resisting atmosphere which the effluent steam has to contend with on leaving the cylinder.

Table of the Elastic Force of Steam, the Pressure of the Atmosphere not being included.

Elastic Force in			Temperature in degrees of Fahr.	Volume of Steam of Water being 1.	Cubic in. of Water in a cubic foot of Steam.
Atmosphere.	Lbs. & sq. in.	in. of Merc.			
1.19	2.5	5.15	220	1496	1.14
1.22	3	6.18	222	1453	1.18
1.29	4	8.24	225	1366	1.25
1.36	5	10.3	228	1282	1.33
1.70	10	20.6	240	1044	1.64
2.04	15	30.9	251	883	1.93
2.38	20	41.2	260	767	2.23
2.72	25	51.5	268	678	2.52
3.06	30	61.8	275	609	2.81
3.40	35	72.1	282	553	3.09
3.74	40	82.4	288	506	3.38
4.08	45	92.7	294	468	3.66
4.42	50	103.0	299	435	3.93
4.76	55	113.3	304	407	4.20
5.10	60	123.6	309	382	4.48

Steam, independent of the heat indicated by an immersed thermometer, also contains heat that can

istence
produced on various
weight of steam at 212° , be
water at 62° , the result is water at 178°
each of the nine parts of water has received from
steam 116.6° of heat, and consequently the steam
diffused or given out $116.6 \times 9 = 1049.4$ — 3°
 1016° of heat which it must have contained. If
it is ascertained by experiment, that if one gal
water be transformed into steam at 212° , ar
steam allowed to mix with water at 52° , th
will be raised to the boiling point, or 212° .
these and other experiments, it is ascertained
latent heat in steam varies from 21°
ratio of accumulation advancing from 21°
steam becomes more dense and of grea
force: hence the severity of a scald by ste
by boiling water.

It is because of the latent heat in stea
in an aëriform state, that it becomes of s
service in *heating, boiling, drying, &c.*
ing of buildings, its *economy, efficien*
plicity of application, are alike acknow
steam being simply conducted through
ments by pipes, by extent of circula
latent heat being thus given t
tation. In boiling, advantage

Steam is also of great utility as a productive source of motive power; and in this respect its properties are *elastic force*, *expansive force*, and *reduction by condensation*. Elastic force signifies the whole urgency or power the steam is capable of exerting with undiminished effect. By expansive force is generally understood the amount of diminishing effect of the steam on the piston of a steam engine, reckoning from that point of the stroke where the steam of uniform elastic force is cut off; but it is more properly the force which steam is capable of exerting when expanded to a known number of times its original bulk. And

Condensation, here understood, is the abstraction or reduction of heat by another body, and consequently not properly a contained property of the steam, but an effect produced by combined agency, in which steam is the principal; because any colder body will extract the heat and produce condensation, but steam cannot be so beneficially replaced by any other fluid capable of maintaining equal results.

The rules formed by experimenters as corresponding with the results of their experiments on the elastic force of steam at given temperatures vary, but approximate so closely that the following rule, because of being simple, may in practice be taken in preference to any other.

Rule.—To the temperature of the steam in degrees of Fahrenheit, add 100, divide the sum by 177, and the 6th power of the quotient equal the force in inches of mercury.

Ex. Required the force of steam corresponding to a temperature of 312°.

$$\frac{312+100}{177} = 2.3277^6 = 159 \text{ inches of mercury.}$$

When steam of a uniform elastic force is (throughout the whole ascent or descent of th the amount of effect produced is as the qu steam expended. But let the steam be sh any portion of the stroke, say, for instance half, it expands by degrees until the termin the stroke, and then exerts half its origin; hence an accumulation of effect in proportio quantity of steam.

Rule.—Divide the length of the stroke by tance or space into which the dense steam is a and find the hyperbolic logarithm of the quo which add 1, and the sum is the ratio of the

Ex. Suppose an engine with a stroke of 6 f the steam cut off when the piston has moved 2; required the ratio of gain by uniform and sive force.

$6 \div 2 = 3$; hyperbolic logarithm of 3 = 1.0986 + 1 ratio of effect; that is, supposing the whole effe steam to be 3, the effect by the steam being on $\frac{1}{3} = 2.0986$.

Again, let the greatest elastic force of steam cylinder of an engine equal 48lbs. per square and let it be cut off from entering the cylinde the piston has moved $4\frac{1}{2}$ inches. the whole

Table of Hyperbolic Logarithms.

No.	Logrthm.	No.	Logrthm.	No.	Logrthm.	No.	Logrthm.
1 $\frac{1}{4}$	22314	3 $\frac{1}{4}$	1.25276	5 $\frac{1}{4}$	1.74919	8	2.07944
1 $\frac{1}{2}$	40546	3 $\frac{1}{2}$	1.32175	6	1.79175	8 $\frac{1}{2}$	2.14006
1 $\frac{3}{4}$	55961	4	1.38629	6 $\frac{1}{4}$	1.83258	9	2.19722
2	69314	4 $\frac{1}{4}$	1.44691	6 $\frac{1}{2}$	1.87180	9 $\frac{1}{2}$	2.25129
2 $\frac{1}{4}$	81093	4 $\frac{1}{2}$	1.50507	6 $\frac{3}{4}$	1.90954	10	2.30258
2 $\frac{1}{2}$	91629	4 $\frac{3}{4}$	1.55814	7	1.94591	12	2.48490
2 $\frac{3}{4}$	1.01160	5	1.60943	7 $\frac{1}{4}$	1.98100	14	2.63905
3	1.09861	5 $\frac{1}{4}$	1.65822	7 $\frac{1}{2}$	2.01490	16	2.77258
3 $\frac{1}{4}$	1.17865	5 $\frac{1}{2}$	1.70474	7 $\frac{3}{4}$	2.04769	18	2.89037

In regard to the other case of expansion: When the temperature is constant the bulk is inversely as the pressure: thus, Suppose steam at 30 lbs. per square inch, required its bulk to that of original bulk, when expanded so as to retain a pressure equal to that of the atmosphere, or 15 lbs.

$$\frac{15+30}{15} = 3 \text{ times its original bulk.}$$

Condensation of steam for motive purposes, generally, is effected by cold water, the quantity of which may be estimated by the following rule. From 1000 plus the temperature of the steam, subtract the required temperature of the condensed water, divide the remainder by the temperature of the condensed water minus the temperature of the cold or condensing water, and the quotient equal the number of times that the quantity, for condensation, must exceed that by which the steam is formed.

Ex. Required the ratio or quantity of water for condensation to 1 of water for the formation of steam, the temperature of the steam being 220°, and the required temperature of condensed water 180°.

$$\frac{1000 + 220 - 180}{180 - 52} = 8 \text{ times the quantity.}$$

Salts in sea water.		3.03
Sulphate of soda	In common water.	81.5
Sulphate of iron		64
Alum		52
Sulphate of lime		45
Sulphate of magnesia ...		57.5
Muriate of soda		80
Nitrate of soda.....		60
Acetate of soda.....		60

Elastic Force of Steam in Inches of Me

Common water	}	boiling point, 212° F.	{	elastic fo
Sea water				
		at		212 "
Common water	}	boiling point, 216° F.	{	elastic fo
Sea water				
		at		216 "
Common water	}	boiling point, 220° F.	{	elastic fo
Sea water				
		at		200 "

Hence the propriety of procuring, for sta
in its purest state.

3. Effects produced by air in its natura in a rarefied state.

The weight or pressure of the atmosphe

2	·136	·0210	-	
2½	·172	·0276	8½	2·314
2¾	·212	·0340	8¾	2·456
3	·257	·0412	9	2·603
3½	·306	·0490	9½	2·754
3¾	·359	·0576	9¾	2·909
4	·416	·0668	10	3·068
4½	·478	·0766	10½	3·232
4¾	·544	·0872	10¾	3·400
5	·614	·0985	11	3·572
5½	·688	·1104	11½	3·748
5¾	·767	·1230	11¾	3·929
6	·850	·1363	12	4·114
6½	·937	·1503	12½	4·303
6¾	1·028	·1649	13	4·496
7	1·124	·1803	13½	4·694
7½	1·224	·1963	14	4·896
7¾	1·328	·2130	14½	5·112
8	1·436	·2304	15	5·346
8½	1·549	·2489	15½	5·596
8¾	1·666	·2672	16	5·864
9	1·787	·2866	16½	6·150
9½	1·912	·3067	17	6·454
9¾	2·042	·3275	17½	6·776
			18	7·116

Examples illustrative of the Utility of the

1. Required the quantity of water lifted by the bucket of a 9½-inch pump,

1	1.47	.005	} Hardly perceptible
2	2.93	.020	
3	4.40	.044	} Just perceptible
4	5.87	.079	
5	7.33	.123	} Gentle pleasant
10	14.67	.492	
15	22.00	1.107	} Pleasant brisk
20	29.34	1.968	
25	36.67	3.075	} Very brisk.
30	44.01	4.429	
35	51.34	6.027	} High winds.
40	58.68	7.873	
45	66.01	9.963	} Very high.
50	73.35	12.300	
60	88.02	17.715	A storm or tem.
80	117.36	31.490	A great storm.
			A hurricane.

In order to gain the greatest amount of the impulsive effect to produce rotary or circular motion by the sails of a wind-mill, the total surface of sails presented to the wind ought to be about $\frac{2}{3}$ of the circle's surface which is formed by their motion and each sail angled to the plane of motion as follows: the whip or back being divided into six equal parts.

Distance from centre of motion	1	2	3	4	5	6	} Same
Angle with plane of motion...	18°	19	18	16	12½	7	
<i>By G. Porrester. Liverpool</i>	21°	21	18	14	9	3

per square inch above the pressure of ...

$$\frac{375 \times 4.5 \times 224}{1232} = 295 \text{ square feet nearly; the fire-gr}$$

in accordance with the following rule.

Multiply the number of square feet of heat face by .12, the product equal the area of fire in square feet, thus :

$$295 \times .12 = 35.4 \text{ square feet of furnace-bar.}$$

Note.—By effective heating surface is meant horizontal faces over fire, flame, or heated air; vertical or side requiring about $1\frac{1}{4}$ ft. to equal in effect 1 of horizontal

2. To determine the proper dimensions for a shaped boiler, when the amount of effective surface in square feet is obtained by the 1 rule.

1. The bottom surface equal half the whole
2. The length of the boiler equal twice the root of bottom surface.
3. The width equal one-fourth the length
4. The height equal one-third the length

Ex. Required the dimensions for a boiler waggon form that may present an effective surface of 295 square feet.

... of 147.5 square

.

per square inch, equal 217·8, for
add about $\frac{1}{4}$ th of the quotient, or 217·8, for
vertical surface, equal 1960·2 square feet
engine,—thus nearly corresponding with the
quantity of heating surface.

Note.—In the four boilers there are 608 brass tub
in length and 3 inches in diameter. The length of
place is 5 feet 10 inches, and breadth 2 feet 10 ;
·56 of a square foot of fire-bar to each cubic foot o
capacity, and ·16 of a square foot of tube apertur
square foot of fire-bar, the openings of the tu
reduced by the thickness of the tube hoops. The
of each chimney, of which there are two, is 3 feet

Locomotive Boilers, in the manner of t
struction, are a class which, of necessity, de
utmost degree of qualified attention, becau
great pressures they are required to sustain
unavoidably narrow limits in which such vas
of steam are required to be generated.

In boilers of this description, it is of
essential consequence that the water spa
fire-box be of a sufficient width, say, on the
sides, not less than $2\frac{1}{2}$ to 3 inches, and in
where the tendency of the fire is urged by
of the blast-pipe, at least $3\frac{1}{2}$ inches.

The boiler which I have selected for i

Specified particulars relative to the Boiler and Engine.

Diameter of cylinders	14 inches.
Length of stroke	18 "
Lap of the valve	1 "
Diameter of driving wheels	5½ feet.
Length of internal fire-box	2 feet 11½ inches.
Width of ditto	3 " 5 "
Length of cylindrical part of boiler	8 " 8 "
Diameter of ditto	8 " 4½ "
Length of tubes	8 " 11½ "
Number of tubes	133, of brass.
Interior diameter of ditto	1½ inches.
Diameter of blast-pipe	4 "

About 112 lbs. of coke consumed in this boiler vaporate 84 gallons of water; and from 20 to 25 lbs. of coke are consumed per mile.

Heating Powers of Combustible Substances.

Species of combustible.	Lbs. of water heated from 32° to 212°.	Lbs. of boiling water evaporated by 1 lb. of fuel.	Lbs. of atmospheric air to each lb. of fuel.
Wood in its ordinary state	26	4.72	4.47
Wood charcoal.....	73	13.37	11.46
Coal	60	10.90	9.26
Coke	65	11.81	11.46
Peat	30	5.45	4.60
Peat charcoal	64	11.63	9.86

In regard to the giving of an order for a steam engine of any required number of horses' power, it has been argued and ultimately decided, that in a commercial point of view the order is not sufficiently completed by the dimensions of cylinder, boiler, &c. being of ample magnitude to produce the specified dynamical effect in horses' power; and not unless corresponding with the established custom by Boulton and Watt, or that of other manufacturers of equally well known respectability: hence, generally, the fol-



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THE Improved Steam Hammer, of which
ontispiece is an accurate engraving, manufact
Paragon Works, near South Queensferry, Scot
have much pleasure, by the aid of a friend, of
describing :

These Hammers are made of all sizes from 7
upwards, and are self-acting or can be wrought
hand; and the great advantages of these hammer
their substantiality, simplicity, and almost imp
pability of getting deranged in any of their p
combined with great moderation in price. The
Valve is of a peculiar description, for besides bei
balance valve, thereby reducing the friction on
face to the lowest possible point, it is so arra
that after the steam has been admitted to the u
side of the piston to raise the hammer, the
steam (before it is allowed to exhaust to th
mosphere) is led to the upper side of the pisto
thereby an addition to the blow or impetus is
to the hammer, from one-third to one-fifth
than its actual weight or gravity: this is ac
by using a very thick piston rod, the area of
piston rod is deducted from the under area
thereby showing the area of the upper

and if you are working with 30 lb steam, you have 585 lb minus expansion in favour of the upper side of your piston to bring down the hammer. The Piston is solid (*no packing*): the Piston Rod is of unusual thickness, of malleable iron, as is also the cross head, and these with the hammer and hammer-face make up the weight required. As mentioned, the Hammer is self-acting, and this is arranged as follows: upon the cross head there is a conical roller (case-hardened), which roller acts upon a spiral incline, also case-hardened, and bolted to a socket which is moved up and down by a hand wheel having attached to it a double-threaded screw working in the socket: this socket has a feather, and is moved up and down by the hand wheel upon a wiper shaft; thus the spiral incline is lowered or raised: the roller on the cross head acting upon the incline causes the wiper shaft to oscillate, and the shaft having a link connecting it to the valve spindle, shuts off the steam from the hammer. Then upon the hammer coming in contact with the work upon the anvil, be it thick and thin alternately; there is a plumper rod, as we term it, working vertically between two guides fixed to cross head or hammer: this plumper rod has a head somewhat larger in diameter than the diameter of the rod; betwixt this head and the upper guide there is a spiral spring which is sufficiently strong to support the weight of this plumper rod and to raise and retain it at its usual position: in this plumper rod there is a slot cut, into which one end of a bell crank is introduced; the other end of this bell crank, whose axis or centre is upon the cross head, plays up and down $\frac{1}{2}$ inch clear of what we term the kicker bar; but so soon as the hammer strikes any substance on the anvil and comes to rest,

When the steam under the hammer, which instantly raises the incline shutting it off and throwing in the and thus the hammer rises and falls, increasing and diminishing the number of strokes per according to the fall you wish to give your h

LOGARITHMS.

LOGARITHMS literally signify *ratios of numbers*; hence Logarithmic Tables may be various, but those in common use for the facilitating of arithmetical operations generally are of the following corresponding progressions, viz.

Arithmetical, 0, 1, 2, 3, &c., or series of logarithms.
Geometrical, 1, 10, 100, 1000, &c., or ratio of numbers.

And thus it may be perceived, that if the log. of 10 be 1, the log. of any number less than 10 must consist wholly of decimals, because increasing by a decimal ratio. Again, if the log. of 100 be 2, the log. of any intermediate number between 10 and 100 must be 1, with so many decimals annexed; and in like manner, the log. of any intermediate number between 100 and 1000 must be 2, with decimals annexed proportionally, as before.

APPLICATION AND UTILITY OF COMMON LOGARITHMIC TABLES.

The whole numbers of the series of logarithms, as 1, 2, 3, &c., are called the indices, or characteristics of the logarithm, and which must be added to the logarithm obtained by the Table, in proportion to the number of figures contained in the given sum. Thus, suppose the logarithm be required for a sum of only two figures, the index is 1; if of three figures, the index is 2; and if of four figures, the index is 3, &c., being always a number less by unity than the number of figures the given sum contains.

The index of a decimal number denotes the significant figure from the decimal and is marked with the sign thus —, to dis- it from a whole number.

Ex. The index of $\cdot 32549$ is —1, because significant figure is the first decimal.

The index of $\cdot 032549$ is —2, because significant figure is the second decimal.

The index of $\cdot 0032549$ is —3, because significant figure is the third decimal, and any other sum.

If the given sum for which the logarithm required contains or consists of both integers and decimals, the index is determined by the integers without having any regard to the other.

1. *To find the logarithm of any whole number under 100.*

Look for the number under N in the first column of any Logarithmic Table; then immediately opposite to it is the logarithm required, with its proper index. Thus, the log. of 64 is 1.806180, and the log. of 65 is 1.857332.

2. *To find the logarithm of any number*

figure, and in a line with the three figures in the column on the left, with its proper index, is the logarithm required. Thus, the log. of 450 is 2.653213, and the log. of 7464 is 3.872972. Or, the log. of 378.5 is 2.578066, and that of .7854 is -1.895091 .

3. To find the number indicated by a given logarithm.

Look for the decimal part of the given logarithm in the different columns, and if it cannot be found exactly, take the next less. Then under N in the left-hand column, and in a line with the logarithm found, are three figures of the number required, and on the top of the column in which the found logarithm stands is one figure more; place the decimal point as indicated by the logarithmic index, which determines the sum, properly valued, as required.

If the logarithm cannot be found exactly in the Tables, subtract from it the next less that can be found, and divide the remainder by the tabular difference; the quotient will be the rest of the figures of the given number, which, being annexed to the tabular number already found, is the proper number required.

Ex. Required the number answering to the logarithm 3.233568.

Given logarithm = 3.233568

Next less is the log. of 1712 ... = 3.233504

Remainder $\frac{64}{253}$

Tab. Diff. = 253, and $\frac{64}{253} = .25$

Hence the number required = 1712.25.

For practical purposes in mechanics, logarithms are seldom resorted to, unless for the raising of the powers of numbers or extraction of their roots: these

Ex. 1. Required the square or second power of 25·791.

Log. of 25·791 = 1·411468

Multiplied by 2, the power required.

Logarithm 2·822936, indicated number or square required = 665·175.

Ex. 2. What is the cube of 30·7146 ?

Logarithm = 1·487345

Multiplied by 3, the power required.

Logarithm 4·462035, indicated number or cube required = 28975·7.

Ex. 3. Required the square root of 365.

Log. = $\frac{2·562293}{2}$ = 1·281146, indicated number or square root = 19·105.

Ex. 4. Find the cube root of 12345.

Log. = $\frac{4·091491}{3}$ = 1·363830, indicated number or cube root = 23·1116.

Table of Logarithms from 1 to 100.

N.	Log.	N.	Log.	N.	Log.	N.	Log.
1	0.000000	26	1.414973	51	1.707570	76	1.880814
2	0.301030	27	1.431364	52	1.716003	77	1.886491
3	0.477121	28	1.447158	53	1.724276	78	1.892095
4	0.602060	29	1.462398	54	1.732394	79	1.897627
5	0.698970	30	1.477121	55	1.740363	80	1.903090
6	0.778151	31	1.491362	56	1.748188	81	1.908485
7	0.845098	32	1.505150	57	1.755875	82	1.913814
8	0.903090	33	1.518514	58	1.763428	83	1.919078
9	0.954243	34	1.531479	59	1.770852	84	1.924279
10	1.000000	35	1.544068	60	1.778151	85	1.929419
11	1.041393	36	1.556303	61	1.785330	86	1.934498
12	1.079181	37	1.568202	62	1.792392	87	1.939519
13	1.113943	38	1.579784	63	1.799341	88	1.944483
14	1.146128	39	1.591065	64	1.806180	89	1.949390
15	1.176091	40	1.602060	65	1.812913	90	1.954243
16	1.204120	41	1.612784	66	1.819544	91	1.959041
17	1.230449	42	1.623249	67	1.826075	92	1.963788
18	1.255273	43	1.633468	68	1.832509	93	1.968483
19	1.278754	44	1.643453	69	1.838849	94	1.973128
20	1.301030	45	1.653213	70	1.845098	95	1.977724
21	1.322219	46	1.662758	71	1.851258	96	1.982271
22	1.342423	47	1.672098	72	1.857332	97	1.986772
23	1.361728	48	1.681241	73	1.863323	98	1.991226
24	1.380211	49	1.690196	74	1.869232	99	1.995635
25	1.397940	50	1.698970	75	1.875061	100	2.000000

Note.—For accurate Tables of Logarithms of a convenient size, see Tables of Logarithms in Mr. Weale's Rudimentary Series, being Vols. 94 and 95 of that series.

Under the following Tables more generally useful.

inches multiplied by .04328, or the areas in feet multiplied by number of imperial gallons at 1 foot in depth.

feet multiplied by .03704, the product equal the number of sq. ft.

inches multiplied by the length or thickness in inches, and the weight in lbs. of cast iron.

metre, or unit of solid measure, equal 35.31716 English cubic feet. Also of capacity, equal 61.028 English cubic inches, or about .453 of a

Dia. in inch.	Length in inch.	sq. mea.
$\frac{1}{8}$.196	.0039
$\frac{1}{4}$.392	.0122
$\frac{3}{8}$.589	.0270
$\frac{1}{2}$.785	.0490
$\frac{5}{8}$.981	.0768
$\frac{3}{4}$	1.178	.1104
$\frac{7}{8}$	1.374	.1500
1	1.570	.1963
$1\frac{1}{8}$	1.767	.2488
$1\frac{1}{4}$	1.963	.3068
$1\frac{3}{8}$	2.159	.3711
$1\frac{1}{2}$	2.356	.4411
$1\frac{5}{8}$	2.552	.5180
$1\frac{3}{4}$	2.748	.6019
$1\frac{7}{8}$	2.945	.6919
2 in.	3	.7854
$2\frac{1}{8}$	3	.99
$2\frac{1}{4}$	3	1.22
$2\frac{3}{8}$	4	1.41
$2\frac{1}{2}$	4	1.7
$2\frac{5}{8}$	5	2.0
$2\frac{3}{4}$	5	2.4
$2\frac{7}{8}$	5	2.8
3 in.	6	3.
$3\frac{1}{8}$	6	3.
$3\frac{1}{4}$	7	3
$3\frac{3}{8}$	7	4

AREAS OF CIRCLES.

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Dia. in inch.	Circum.in ft. in.	Area in sq. inch.	Area in sq. feet.	Dia. in inch.	Circum.in ft. in.	Area in sq. inch.	Area in sq. feet.
4 in.	1 0 $\frac{1}{8}$	12.566	.0879	9 in.	2 4 $\frac{1}{2}$	63.617	.4453
4 $\frac{1}{8}$	1 0 $\frac{1}{4}$	13.364	.0935	9 $\frac{1}{8}$	2 4 $\frac{3}{8}$	65.396	.4577
4 $\frac{1}{4}$	1 1 $\frac{1}{8}$	14.186	.0993	9 $\frac{1}{4}$	2 5	67.200	.4704
4 $\frac{3}{8}$	1 1 $\frac{1}{4}$	15.033	.1052	9 $\frac{3}{8}$	2 5 $\frac{1}{8}$	69.029	.4832
4 $\frac{1}{2}$	1 2 $\frac{1}{8}$	15.904	.1113	9 $\frac{1}{2}$	2 5 $\frac{1}{4}$	70.882	.4961
4 $\frac{5}{8}$	1 2 $\frac{1}{4}$	16.800	.1176	9 $\frac{5}{8}$	2 6 $\frac{1}{8}$	72.759	.5093
4 $\frac{3}{4}$	1 2 $\frac{3}{8}$	17.720	.1240	9 $\frac{3}{4}$	2 6 $\frac{1}{4}$	74.662	.5226
4 $\frac{7}{8}$	1 3 $\frac{1}{8}$	18.665	.1306	9 $\frac{7}{8}$	2 7	76.588	.5361
5 in.	1 3 $\frac{3}{8}$	19.635	.1374	10 in.	2 7 $\frac{3}{8}$	78.540	.5497
5 $\frac{1}{8}$	1 4 $\frac{1}{8}$	20.629	.1444	10 $\frac{1}{8}$	2 7 $\frac{1}{4}$	80.515	.5636
5 $\frac{1}{4}$	1 4 $\frac{1}{4}$	21.647	.1515	10 $\frac{1}{4}$	2 8 $\frac{1}{8}$	82.516	.5776
5 $\frac{3}{8}$	1 4 $\frac{3}{8}$	22.690	.1588	10 $\frac{3}{8}$	2 8 $\frac{1}{4}$	84.540	.5917
5 $\frac{1}{2}$	1 5 $\frac{1}{8}$	23.758	.1663	10 $\frac{1}{2}$	2 8 $\frac{3}{8}$	86.590	.6061
5 $\frac{5}{8}$	1 5 $\frac{1}{4}$	24.850	.1739	10 $\frac{5}{8}$	2 9 $\frac{1}{8}$	88.664	.6206
5 $\frac{3}{4}$	1 6	25.967	.1817	10 $\frac{3}{4}$	2 9 $\frac{1}{4}$	90.762	.6353
5 $\frac{7}{8}$	1 6 $\frac{1}{8}$	27.108	.1897	10 $\frac{7}{8}$	2 10 $\frac{1}{8}$	92.885	.6499
6 in.	1 6 $\frac{3}{8}$	28.274	.1979	11 in.	2 10 $\frac{1}{4}$	95.033	.6652
6 $\frac{1}{8}$	1 7 $\frac{1}{8}$	29.464	.2062	11 $\frac{1}{8}$	2 10 $\frac{3}{8}$	97.205	.6804
6 $\frac{1}{4}$	1 7 $\frac{1}{4}$	30.679	.2147	11 $\frac{1}{4}$	2 11 $\frac{1}{8}$	99.402	.6958
6 $\frac{3}{8}$	1 8	31.919	.2234	11 $\frac{3}{8}$	2 11 $\frac{3}{8}$	101.623	.7113
6 $\frac{1}{2}$	1 8 $\frac{1}{8}$	33.183	.2322	11 $\frac{1}{2}$	3 0 $\frac{1}{8}$	103.869	.7270
6 $\frac{5}{8}$	1 8 $\frac{1}{4}$	34.471	.2412	11 $\frac{5}{8}$	3 0 $\frac{3}{8}$	106.139	.7429
6 $\frac{3}{4}$	1 9 $\frac{1}{8}$	35.784	.2504	11 $\frac{3}{4}$	3 0 $\frac{7}{8}$	108.434	.7590
6 $\frac{7}{8}$	1 9 $\frac{1}{4}$	37.122	.2598	11 $\frac{7}{8}$	3 1 $\frac{1}{8}$	110.753	.7752
7 in.	1 10	38.484	.2693	12 in.	3 1 $\frac{3}{8}$	113.097	.7916
7 $\frac{1}{8}$	1 10 $\frac{1}{8}$	39.871	.2791	12 $\frac{1}{8}$	3 2	115.466	.8082
7 $\frac{1}{4}$	1 10 $\frac{1}{4}$	41.282	.2889	12 $\frac{1}{4}$	3 2 $\frac{1}{8}$	117.859	.8250
7 $\frac{3}{8}$	1 11 $\frac{1}{8}$	42.718	.2990	12 $\frac{3}{8}$	3 2 $\frac{3}{8}$	120.276	.8419
7 $\frac{1}{2}$	1 11 $\frac{1}{4}$	44.178	.3092	12 $\frac{1}{2}$	3 3 $\frac{1}{8}$	122.718	.8590
7 $\frac{5}{8}$	1 11 $\frac{3}{8}$	45.663	.3196	12 $\frac{5}{8}$	3 3 $\frac{3}{8}$	125.185	.8762
7 $\frac{3}{4}$	2 0 $\frac{1}{8}$	47.173	.3299	12 $\frac{3}{4}$	3 4	127.676	.8937
7 $\frac{7}{8}$	2 0 $\frac{1}{4}$	48.707	.3409	12 $\frac{7}{8}$	3 4 $\frac{1}{8}$	130.192	.9113
8 in.	2 1 $\frac{1}{8}$	50.265	.3518	13 in.	3 4 $\frac{3}{8}$	132.732	.9291
8 $\frac{1}{8}$	2 1 $\frac{1}{4}$	51.848	.3629	13 $\frac{1}{8}$	3 5 $\frac{1}{8}$	135.297	.9470
8 $\frac{1}{4}$	2 1 $\frac{3}{8}$	53.456	.3741	13 $\frac{1}{4}$	3 5 $\frac{3}{8}$	137.886	.9642
8 $\frac{3}{8}$	2 2 $\frac{1}{8}$	55.088	.3856	13 $\frac{3}{8}$	3 6	140.500	.9835
8 $\frac{1}{2}$	2 2 $\frac{1}{4}$	56.745	.3972	13 $\frac{1}{2}$	3 6 $\frac{1}{8}$	143.139	1.0019
8 $\frac{5}{8}$	2 3	58.426	.4089	13 $\frac{5}{8}$	3 6 $\frac{3}{8}$	145.802	1.0206
8 $\frac{3}{4}$	2 3 $\frac{1}{8}$	60.132	.4209	13 $\frac{3}{4}$	3 7 $\frac{1}{8}$	148.489	1.0294
8 $\frac{7}{8}$	2 3 $\frac{1}{4}$	61.862	.4330	13 $\frac{7}{8}$	3 7 $\frac{3}{8}$	151.201	1.0384

14 $\frac{1}{2}$	3 9 $\frac{1}{2}$	162-295	1-1500	19 $\frac{1}{2}$	5 1 $\frac{1}{2}$	29
14 $\frac{1}{2}$	3 9 $\frac{1}{2}$	165-130	1-1569	19 $\frac{1}{2}$	5 1 $\frac{1}{2}$	30
14 $\frac{1}{2}$	3 9 $\frac{1}{2}$	167-989	1-1749	19 $\frac{1}{2}$	5 2	30
14 $\frac{1}{2}$	3 10 $\frac{1}{2}$	170-873	1-1961	19 $\frac{1}{2}$	5 2 $\frac{1}{2}$	31
14 $\frac{1}{2}$	3 10 $\frac{1}{2}$	173-782	1-2164	19 $\frac{1}{2}$	5 2 $\frac{1}{2}$	31
15	3 11 $\frac{1}{2}$	176-715	1-2370	20	5 2 $\frac{1}{2}$	31
15 $\frac{1}{2}$	3 11 $\frac{1}{2}$	179-672	1-2577	20 $\frac{1}{2}$	5 3 $\frac{1}{2}$	31
15 $\frac{1}{2}$	3 11 $\frac{1}{2}$	182-654	1-2785	20 $\frac{1}{2}$	5 3 $\frac{1}{2}$	32
15 $\frac{1}{2}$	4 0 $\frac{1}{2}$	185-661	1-2996	20 $\frac{1}{2}$	5 4	32
15 $\frac{1}{2}$	4 0 $\frac{1}{2}$	188-692	1-3208	20 $\frac{1}{2}$	5 4 $\frac{1}{2}$	32
15 $\frac{1}{2}$	4 1	191-748	1-3422	20 $\frac{1}{2}$	5 4 $\frac{1}{2}$	32
15 $\frac{1}{2}$	4 1 $\frac{1}{2}$	194-828	1-3637	20 $\frac{1}{2}$	5 5 $\frac{1}{2}$	32
15 $\frac{1}{2}$	4 1 $\frac{1}{2}$	197-933	1-3855	20 $\frac{1}{2}$	5 5 $\frac{1}{2}$	32
16	4 2 $\frac{1}{2}$	201-062	1-4074	21	5 5 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 2 $\frac{1}{2}$	204-216	1-4295	21 $\frac{1}{2}$	5 6 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 3	207-394	1-4517	21 $\frac{1}{2}$	5 6 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 3 $\frac{1}{2}$	210-597	1-4741	21 $\frac{1}{2}$	5 7 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 3 $\frac{1}{2}$	213-825	1-4967	21 $\frac{1}{2}$	5 7 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 4 $\frac{1}{2}$	217-077	1-5195	21 $\frac{1}{2}$	5 7 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 4 $\frac{1}{2}$	220-353	1-5424	21 $\frac{1}{2}$	5 8 $\frac{1}{2}$	32
16 $\frac{1}{2}$	4 5	223-654	1-5655	21 $\frac{1}{2}$	5 8 $\frac{1}{2}$	32
17	4 5 $\frac{1}{2}$	226-980	1-5888	22	5 9 $\frac{1}{2}$	32
17 $\frac{1}{2}$	4 5 $\frac{1}{2}$	230-330	1-6123	22 $\frac{1}{2}$	5 9 $\frac{1}{2}$	32
17 $\frac{1}{2}$	4 6 $\frac{1}{2}$	233-705	1-6359	22 $\frac{1}{2}$	5 9 $\frac{1}{2}$	32
17 $\frac{1}{2}$	4 6 $\frac{1}{2}$	237-104	1-6597	22 $\frac{1}{2}$	5 10 $\frac{1}{2}$	32
17 $\frac{1}{2}$	4 6 $\frac{1}{2}$	240-528	1-6836	22 $\frac{1}{2}$	5 10 $\frac{1}{2}$	32
17 $\frac{1}{2}$	4 7 $\frac{1}{2}$	243-977	1-7078	22 $\frac{1}{2}$	5 11	32

AREAS OF CIRCLES.

313

Dia. in ft. in.	Circum. in ft. in.	Area in sq. inch.	Area in sq. feet.	Dia. in ft. in.	Circum. in ft. in.	Area in sq. inch.	Area in sq. feet.
2 0	6 3 $\frac{1}{2}$	452.390	3.1418	2 10	8 10 $\frac{1}{2}$	907.922	6.3051
2 0 $\frac{1}{2}$	6 4 $\frac{1}{2}$	461.864	3.2075	2 10 $\frac{1}{2}$	8 11 $\frac{1}{2}$	921.323	6.3981
2 0 $\frac{1}{2}$	6 4 $\frac{1}{2}$	471.436	3.2731	2 10 $\frac{1}{2}$	9 0 $\frac{1}{2}$	934.822	6.4911
2 0 $\frac{3}{4}$	6 5 $\frac{1}{4}$	481.106	3.3410	2 10 $\frac{3}{4}$	9 1 $\frac{1}{2}$	948.419	6.5863
2 1	6 6 $\frac{1}{2}$	490.875	3.4081	2 11	9 1 $\frac{1}{2}$	962.115	6.6815
2 1 $\frac{1}{4}$	6 7 $\frac{1}{4}$	500.741	3.4775	2 11 $\frac{1}{4}$	9 2 $\frac{1}{4}$	975.908	6.7772
2 1 $\frac{1}{2}$	6 8 $\frac{1}{2}$	510.706	3.5468	2 11 $\frac{1}{2}$	9 3 $\frac{1}{2}$	989.800	6.8738
2 1 $\frac{3}{4}$	6 8 $\frac{3}{4}$	520.769	3.6101	2 11 $\frac{3}{4}$	9 4 $\frac{1}{2}$	1003.79	6.9701
2 2	6 9 $\frac{1}{2}$	530.930	3.6870	3 0	9 5	1017.87	7.0688
2 2 $\frac{1}{4}$	6 10 $\frac{1}{4}$	541.189	3.7583	3 0 $\frac{1}{4}$	9 5 $\frac{1}{4}$	1032.06	7.1671
2 2 $\frac{1}{2}$	6 11 $\frac{1}{2}$	551.547	3.8302	3 0 $\frac{1}{2}$	9 6 $\frac{1}{2}$	1046.35	7.2664
2 2 $\frac{3}{4}$	7 0	562.002	3.9042	3 0 $\frac{3}{4}$	9 7 $\frac{1}{4}$	1060.73	7.3662
2 3	7 0 $\frac{1}{2}$	572.556	3.9761	3 1	9 8 $\frac{1}{4}$	1075.21	7.4661
2 3 $\frac{1}{4}$	7 1 $\frac{1}{4}$	583.208	4.0500	3 1 $\frac{1}{4}$	9 9	1089.79	7.5671
2 3 $\frac{1}{2}$	7 2 $\frac{1}{2}$	593.958	4.1241	3 1 $\frac{1}{2}$	9 9 $\frac{1}{2}$	1104.46	7.6691
2 3 $\frac{3}{4}$	7 3 $\frac{1}{4}$	604.807	4.2000	3 1 $\frac{3}{4}$	9 10 $\frac{1}{4}$	1119.24	7.7791
2 4	7 3 $\frac{3}{4}$	615.753	4.2760	3 2	9 11 $\frac{1}{4}$	1134.12	7.8681
2 4 $\frac{1}{4}$	7 4 $\frac{1}{4}$	626.798	4.3521	3 2 $\frac{1}{4}$	10 0 $\frac{1}{4}$	1149.09	7.9791
2 4 $\frac{1}{2}$	7 5 $\frac{1}{4}$	637.941	4.4302	3 2 $\frac{1}{2}$	10 0 $\frac{1}{2}$	1164.16	8.0846
2 4 $\frac{3}{4}$	7 6 $\frac{1}{4}$	649.182	4.5083	3 2 $\frac{3}{4}$	10 1 $\frac{1}{4}$	1179.32	8.1891
2 5	7 7	660.521	4.5861	3 3	10 2 $\frac{1}{4}$	1194.59	8.2951
2 5 $\frac{1}{4}$	7 7 $\frac{1}{4}$	671.958	4.6665	3 3 $\frac{1}{4}$	10 3 $\frac{1}{4}$	1209.95	8.4026
2 5 $\frac{1}{2}$	7 8 $\frac{1}{4}$	683.494	4.7467	3 3 $\frac{1}{2}$	10 4	1225.42	8.5091
2 5 $\frac{3}{4}$	7 9 $\frac{1}{4}$	695.128	4.8274	3 3 $\frac{3}{4}$	10 4 $\frac{1}{4}$	1240.98	8.6171
2 6	7 10 $\frac{1}{4}$	706.860	4.9081	3 4	10 5 $\frac{1}{4}$	1256.64	8.7269
2 6 $\frac{1}{4}$	7 11	718.690	4.9901	3 4 $\frac{1}{4}$	10 6 $\frac{1}{4}$	1272.39	8.8361
2 6 $\frac{1}{2}$	7 11 $\frac{1}{4}$	730.618	5.0731	3 4 $\frac{1}{2}$	10 7 $\frac{1}{4}$	1288.25	8.9462
2 6 $\frac{3}{4}$	8 0 $\frac{1}{4}$	742.644	5.1573	3 4 $\frac{3}{4}$	10 8	1304.20	9.0561
2 7	8 1 $\frac{1}{4}$	754.769	5.2278	3 5	10 8 $\frac{1}{4}$	1320.25	9.1686
2 7 $\frac{1}{4}$	8 2 $\frac{1}{4}$	766.992	5.3264	3 5 $\frac{1}{4}$	10 9 $\frac{1}{4}$	1336.40	9.2112
2 7 $\frac{1}{2}$	8 2 $\frac{3}{4}$	779.313	5.4112	3 5 $\frac{1}{2}$	10 10 $\frac{1}{4}$	1352.65	9.3936
2 7 $\frac{3}{4}$	8 3 $\frac{1}{4}$	791.732	5.4982	3 5 $\frac{3}{4}$	10 11 $\frac{1}{4}$	1369.00	9.5061
2 8	8 4 $\frac{1}{4}$	804.249	5.5850	3 6	10 11 $\frac{3}{4}$	1385.44	9.6212
2 8 $\frac{1}{4}$	8 5 $\frac{1}{4}$	816.865	5.6729	3 6 $\frac{1}{4}$	11 0 $\frac{1}{4}$	1401.98	9.7364
2 8 $\frac{1}{2}$	8 6 $\frac{1}{4}$	829.578	5.7601	3 6 $\frac{1}{2}$	11 1 $\frac{1}{4}$	1418.62	9.8518
2 8 $\frac{3}{4}$	8 6 $\frac{3}{4}$	842.390	5.8491	3 6 $\frac{3}{4}$	11 2 $\frac{1}{4}$	1435.36	9.9671
2 9	8 7 $\frac{1}{4}$	855.300	5.9398	3 7	11 3	1452.20	10.084
2 9 $\frac{1}{4}$	8 8 $\frac{1}{4}$	868.308	6.0291	3 7 $\frac{1}{4}$	11 3 $\frac{1}{4}$	1469.14	10.202
2 9 $\frac{1}{2}$	8 9 $\frac{1}{4}$	881.415	6.1201	3 7 $\frac{1}{2}$	11 4 $\frac{1}{4}$	1486.17	10.320
2 9 $\frac{3}{4}$	8 10	894.619	6.2129	3 7 $\frac{3}{4}$	11 5 $\frac{1}{4}$	1503.30	10.439

3 9	11 9 $\frac{3}{4}$	1590·43	11·044	4 7	14 4 $\frac{1}{2}$
3 9 $\frac{1}{4}$	11 10 $\frac{1}{4}$	1608·15	11·167	4 7 $\frac{1}{4}$	14 5 $\frac{1}{4}$
3 9 $\frac{1}{2}$	11 10 $\frac{3}{8}$	1625·97	11·291	4 7 $\frac{1}{2}$	14 6 $\frac{1}{8}$
3 9 $\frac{3}{4}$	11 11 $\frac{1}{4}$	1643·89	11·415	4 7 $\frac{3}{4}$	14 7 $\frac{1}{2}$
3 10	12 0 $\frac{1}{2}$	1661·90	11·534	4 8	14 7 $\frac{3}{4}$
3 10 $\frac{1}{4}$	12 1 $\frac{1}{4}$	1680·02	11·666	4 8 $\frac{1}{4}$	14 8 $\frac{1}{4}$
3 10 $\frac{1}{2}$	12 2	1698·23	11·793	4 8 $\frac{1}{2}$	14 9 $\frac{1}{2}$
3 10 $\frac{3}{4}$	12 2 $\frac{3}{4}$	1716·54	11·920	4 8 $\frac{3}{4}$	14 10 $\frac{1}{4}$
3 11	12 3 $\frac{1}{8}$	1734·94	12·048	4 9	14 11
3 11 $\frac{1}{4}$	12 4 $\frac{1}{8}$	1753·45	12·176	4 9 $\frac{1}{4}$	14 11 $\frac{1}{4}$
3 11 $\frac{1}{2}$	12 5 $\frac{1}{4}$	1772·05	12·305	4 9 $\frac{1}{2}$	15 0 $\frac{1}{8}$
3 11 $\frac{3}{4}$	12 6	1790·76	12·435	4 9 $\frac{3}{4}$	15 1 $\frac{1}{8}$
4 0	12 6 $\frac{3}{4}$	1809·56	12·566	4 10	15 2 $\frac{1}{4}$
4 0 $\frac{1}{4}$	12 7 $\frac{1}{4}$	1828·46	12·697	4 10 $\frac{1}{4}$	15 2 $\frac{3}{4}$
4 0 $\frac{1}{2}$	12 8 $\frac{1}{2}$	1847·45	12·829	4 10 $\frac{1}{2}$	15 3 $\frac{1}{4}$
4 0 $\frac{3}{4}$	12 9 $\frac{1}{4}$	1866·55	12·962	4 10 $\frac{3}{4}$	15 4 $\frac{1}{4}$
4 1	12 9 $\frac{3}{4}$	1885·74	13·095	4 11	15 5 $\frac{1}{4}$
4 1 $\frac{1}{4}$	12 10 $\frac{3}{4}$	1905·03	13·229	4 11 $\frac{1}{4}$	15 6 $\frac{1}{8}$
4 1 $\frac{1}{2}$	12 11 $\frac{1}{2}$	1924·42	13·364	4 11 $\frac{1}{2}$	15 6 $\frac{3}{4}$
4 1 $\frac{3}{4}$	13 0 $\frac{1}{4}$	1943·91	13·499	4 11 $\frac{3}{4}$	15 7 $\frac{1}{4}$
4 2	13 1	1963·50	13·635	5 0	15 8 $\frac{1}{4}$
4 2 $\frac{1}{4}$	13 1 $\frac{1}{4}$	1983·18	13·772	5 0 $\frac{1}{4}$	15 9 $\frac{1}{4}$
4 2 $\frac{1}{2}$	13 2 $\frac{1}{2}$	2002·96	13·909	5 0 $\frac{1}{2}$	15 10
4 2 $\frac{3}{4}$	13 3 $\frac{1}{4}$	2022·84	14·047	5 0 $\frac{3}{4}$	15 10 $\frac{3}{4}$
4 3	13 4 $\frac{1}{4}$	2042·82	14·186	5 1	15 11 $\frac{1}{8}$
4 3 $\frac{1}{4}$	13 5	2062·90	14·325	5 1 $\frac{1}{4}$	16 0 $\frac{3}{8}$
4 3 $\frac{1}{2}$	13 5 $\frac{1}{2}$	2083·07	14·465	5 1 $\frac{1}{2}$	16 1 $\frac{1}{4}$

AREAS OF CIRCLES.

315

Dia. in ft. in.	Circum. in ft. in.	Area in sq. inch.	Area in sq. feet.	Dia. in ft. in.	Circum. in ft. in.	Area in sq. inch.	Area in sq. feet.
5 4	16 9	3216.99	22.333	6 2	19 4½	4300.85	29.867
5 4½	16 9½	3242.17	22.515	6 2½	19 5½	4329.95	30.069
5 4¾	16 10½	3267.46	22.621	6 2½	19 6	4359.16	30.271
5 4¾	16 11½	3292.83	22.866	6 2¾	19 6½	4388.47	30.475
5 5	17 0½	3318.31	23.043	6 3	19 7½	4417.87	30.679
5 5½	17 0½	3343.88	23.221	6 3½	19 8½	4447.37	30.884
5 5½	17 1½	3369.56	23.330	6 3½	19 9½	4476.97	31.090
5 5¾	17 2½	3395.33	23.578	6 3¾	19 9½	4506.67	31.296
5 6	17 3½	3421.20	23.758	6 4	19 10½	4536.47	31.503
5 6½	17 4½	3447.16	23.938	6 4½	19 11½	4566.36	31.710
5 6½	17 4½	3473.23	24.119	6 4½	20 0½	4596.35	31.919
5 6¾	17 5½	3499.39	24.301	6 4¾	20 1½	4626.44	32.114
5 7	17 6½	3525.66	24.483	6 5	20 1½	4656.63	32.337
5 7½	17 7½	3552.01	24.666	6 5½	20 2½	4686.92	32.548
5 7½	17 8	3578.47	24.850	6 5½	20 3½	4717.30	32.759
5 7¾	17 8½	3605.03	25.034	6 5¾	20 4½	4747.79	32.970
5 8	17 9½	3631.68	25.220	6 6	20 5	4778.37	33.183
5 8½	17 10½	3658.44	25.405	6 6½	20 5½	4809.05	33.396
5 8½	17 11½	3685.29	25.592	6 6½	20 6½	4839.83	33.619
5 8¾	17 11½	3712.24	25.779	6 6¾	20 7½	4870.70	33.824
5 9	18 0½	3739.28	25.964	6 7	20 8	4901.68	34.039
5 9½	18 1½	3766.43	26.155	6 7½	20 8½	4932.75	34.255
5 9½	18 2½	3793.67	26.344	6 7½	20 9½	4963.92	34.471
5 9¾	18 3½	3821.02	26.534	6 7¾	20 10½	4995.19	34.688
5 10	18 3½	3848.46	26.725	6 8	20 11½	5026.26	34.906
5 10½	18 4½	3875.99	26.916	6 8½	21 0½	5058.02	35.125
5 10½	18 5½	3903.63	27.108	6 8½	21 0½	5089.58	35.344
5 10¾	18 6½	3931.36	27.301	6 8¾	21 1½	5121.24	35.564
5 11	18 7	3959.20	27.494	6 9	21 2½	5153.00	35.784
5 11½	18 7½	3987.13	27.688	6 9½	21 3½	5184.86	36.006
5 11½	18 8½	4015.16	27.883	6 9½	21 4	5216.82	36.227
5 11¾	18 9½	4043.28	28.078	6 9¾	21 4½	5248.87	36.450
6 0	18 10½	4071.51	28.274	6 10	21 5½	5281.02	36.674
6 0½	18 10½	4099.83	28.471	6 10½	21 6½	5313.27	36.897
6 0½	18 11½	4128.25	28.668	6 10½	21 7½	5345.62	37.122
6 0¾	19 0½	4156.77	28.866	6 10¾	21 7½	5378.07	37.347
6 1	19 1½	4185.39	29.065	6 11	21 8½	5410.62	37.573
6 1½	19 2½	4214.11	29.264	6 11½	21 9½	5443.26	37.700
6 1½	19 2½	4242.92	29.466	6 11½	21 10½	5476.00	38.027
6 1¾	19 3½	4271.83	29.665	6 11¾	21 11	5508.84	38.254

2	22	6½	40-3388	2	31	11½	
3	22	9½	41-2825	3	32	2½	
4	23	0½	42-2367	4	32	5½	
5	23	2½	43-2022	5	32	8½	
6	23	6¾	44-1787	6	32	11½	
7	23	11	45-1656	7	33	2½	
8	24	1½	46-1638	8	33	6½	
9	24	4½	47-1730	9	33	9½	
10	24	7½	48-1926	10	34	0½	
11	24	10½	49-2236	11	34	3½	
8	0	25	1½	11	0	34	6½
1	25	4½	51-3178	1	34	9½	
2	25	7½	52-3816	2	35	0½	
3	25	11	53-4562	3	35	4½	
4	26	2½	54-5412	4	35	7½	
5	26	5½	55-6377	5	35	10½	
6	26	8½	56-7451	6	36	1	
7	26	11½	57-8628	7	36	4	
8	27	2¾	58-9920	8	36	7	
9	27	5¾	60-1321	9	36	10	
10	27	9	61-2826	10	37	2	
11	28	0½	62-4445	11	37	5	
9	0	28	3½	12	0	37	1
1	28	6½	64-8006	1	37	1	
2	28	9½	65-9951	2	38		

dia. in & in.	Circum. in ft. and in.	Area in feet.	dia. in ft. & in.	Circum. in ft. and in.	Area in feet.
3 0	40 10	132.7326	16 0	50 3 $\frac{1}{2}$	201.0624
1	41 1 $\frac{1}{2}$	134.4391	1	50 6 $\frac{1}{2}$	203.1615
2	41 4 $\frac{1}{2}$	136.1574	2	50 9 $\frac{1}{2}$	205.2726
3	41 7 $\frac{1}{2}$	137.8867	3	51 0 $\frac{1}{2}$	207.3946
4	41 10 $\frac{1}{2}$	139.6260	4	51 3 $\frac{1}{2}$	209.5264
5	42 1 $\frac{1}{2}$	141.3771	5	51 6 $\frac{1}{2}$	211.6703
6	42 4 $\frac{1}{2}$	143.1391	6	51 10	213.8251
7	42 8	144.9111	7	52 1 $\frac{1}{2}$	215.9896
8	42 11 $\frac{1}{2}$	146.6949	8	52 4 $\frac{1}{2}$	218.1662
9	43 2 $\frac{1}{2}$	148.4896	9	52 7 $\frac{1}{2}$	220.3537
10	43 5 $\frac{1}{2}$	150.2943	10	52 10 $\frac{1}{2}$	222.5510
11	43 8 $\frac{1}{2}$	152.1109	11	53 1 $\frac{1}{2}$	224.7603
4 0	43 11 $\frac{1}{2}$	153.9384	17 0	53 4 $\frac{1}{2}$	226.9806
1	44 2 $\frac{1}{2}$	155.7758	1	53 8	229.2105
2	44 6	157.6250	2	53 11 $\frac{1}{2}$	231.4625
3	44 9 $\frac{1}{2}$	159.4852	3	54 2 $\frac{1}{2}$	233.7055
4	45 0 $\frac{1}{2}$	161.3553	4	54 5 $\frac{1}{2}$	235.9692
5	45 3 $\frac{1}{2}$	163.2373	5	54 8 $\frac{1}{2}$	238.2430
6	45 6 $\frac{1}{2}$	165.1303	6	54 11 $\frac{1}{2}$	240.5287
7	45 9 $\frac{1}{2}$	167.0331	7	55 2 $\frac{1}{2}$	242.8241
8	46 0 $\frac{1}{2}$	168.9479	8	55 6	245.1316
9	46 4	170.8735	9	55 9 $\frac{1}{2}$	247.4500
10	46 7 $\frac{1}{2}$	172.8091	10	56 0 $\frac{1}{2}$	249.7781
11	46 11 $\frac{1}{2}$	174.7565	11	56 3 $\frac{1}{2}$	252.1184
5 0	47 1 $\frac{1}{2}$	176.7150	18 0	56 6 $\frac{1}{2}$	254.4696
1	47 4 $\frac{1}{2}$	178.6832	1	56 9 $\frac{1}{2}$	256.8303
2	47 7 $\frac{1}{2}$	180.6634	2	57 0 $\frac{1}{2}$	259.2033
3	47 10 $\frac{1}{2}$	182.6545	3	57 4	261.5872
4	48 2 $\frac{1}{2}$	184.6555	4	57 7 $\frac{1}{2}$	263.9807
5	48 5 $\frac{1}{2}$	186.6684	5	57 10 $\frac{1}{2}$	266.3864
6	48 8 $\frac{1}{2}$	188.6923	6	58 1 $\frac{1}{2}$	268.8031
7	48 11 $\frac{1}{2}$	190.7260	7	58 4 $\frac{1}{2}$	271.2293
8	49 2 $\frac{1}{2}$	192.7716	8	58 7 $\frac{1}{2}$	273.6678
9	49 5 $\frac{1}{2}$	194.8282	9	58 10 $\frac{1}{2}$	276.1171
10	49 8 $\frac{1}{2}$	196.8946	10	59 2	278.5761
11	50 0	198.9730	11	59 5 $\frac{1}{2}$	281.0472

212	100	80	176	80	62	139
211	99·4	79·5	175	79·4	63·5	138
210	98·8	79·1	174	78·8	63·1	138
209	98·3	78·6	173	78·3	62·6	137
208	97·7	78·2	172	77·7	62·2	136
207	97·2	77·7	171	77·2	61·7	135
206	96·6	77·3	170	76·6	61·3	134
205	96·1	76·8	169	76·1	60·8	133
204	95·5	76·4	168	75·5	60·4	132
203	95	76	167	75	60	131
202	94·4	75·5	166	74·4	59·5	130
201	93·8	75·1	165	73·8	59·1	129
200	93·3	74·6	164	73·3	58·6	128
199	92·7	74·2	163	72·7	58·2	127
198	92·2	73·7	162	72·2	57·7	126
197	91·6	73·3	161	71·6	57·3	125
196	91·1	72·8	160	71·1	56·8	124
195	90·5	72·4	159	70·5	56·4	123
194	90	72	158	70	56	122
193	89·4	71·5	157	69·4	55·5	121
192	88·8	71·1	156	68·8	55·1	120
191	88·3	70·6	155	68·3	54·6	119
190	87·7	70·2	154	67·7	54·2	118
189	87·2	69·7	153	67·2	53·7	117
188	86·6	69·3	152	66·6	53·3	116
187	86·1	68·8	151	66·1	52·8	115
186	85·5	68·4	150	65·5	52·4	114

Degrees of			Degrees of			Degrees of		
Fah.	Cent.	Reau.	Fah.	Cent.	Reau.	Fah.	Cent.	Reau.
104	40	32	65	18.3	14.6	26	— 3.3	— 2.6
103	39.4	31.5	64	17.7	14.2	25	— 3.8	— 3.1
102	38.8	31.1	63	17.2	13.7	24	— 4.4	— 3.5
101	38.3	30.6	62	16.6	13.3	23	— 5	— 4
100	37.7	30.2	61	16.1	12.8	22	— 5.5	— 4.4
99	37.2	29.7	60	15.5	12.4	21	— 6.1	— 4.8
98	36.6	29.3	59	15	12	20	— 6.6	— 5.3
97	36.1	28.8	58	14.4	11.5	19	— 7.2	— 5.7
96	35.5	28.4	57	13.8	11.1	18	— 7.7	— 6.2
95	35	28	56	13.3	10.6	17	— 8.3	— 6.6
94	34.4	27.5	55	12.7	10.2	16	— 8.8	— 7.1
93	33.8	27.1	54	12.2	9.7	15	— 9.4	— 7.5
92	33.3	26.6	53	11.6	9.3	14	— 10	— 8
91	32.7	26.2	52	11.1	8.8	13	— 10.5	— 8.4
90	32.2	25.7	51	10.5	8.4	12	— 11.1	— 8.8
89	31.6	25.3	50	10	8	11	— 11.6	— 9.3
88	31.1	24.8	49	9.4	7.5	10	— 12.2	— 9.7
87	30.5	24.4	48	8.8	7.1	9	— 12.7	— 10.2
86	30	24	47	8.3	6.6	8	— 13.3	— 10.6
85	29.4	23.5	46	7.7	6.2	7	— 13.8	— 11.1
84	28.8	23.1	45	7.2	5.7	6	— 14.4	— 11.5
83	28.3	22.6	44	6.6	5.3	5	— 15	— 12
82	27.7	22.2	43	6.1	4.8	4	— 15.5	— 12.4
81	27.2	21.7	42	5.5	4.4	3	— 16.1	— 12.8
80	26.6	21.3	41	5	4	2	— 16.6	— 13.3
79	26.1	20.8	40	4.4	3.5	1	— 17.2	— 13.7
78	25.5	20.4	39	3.8	3.1	zero.	— 17.7	— 14.2
77	25	20	38	3.3	2.6	— 1	— 18.3	— 14.6
76	24.4	19.5	37	2.7	2.2	— 2	— 18.8	— 15.1
75	23.8	19.1	36	2.2	1.7	— 3	— 19.4	— 15.5
74	23.3	18.6	35	1.6	1.3	— 4	— 20	— 16
73	22.7	18.2	34	1.1	0.8	— 5	— 20.5	— 16.4
72	22.2	17.7	33	0.5	0.4	— 6	— 21.1	— 16.8
71	21.6	17.3	32	zero.	zero.	— 7	— 21.6	— 17.3
70	21.1	16.8	31	— 0.5	— 0.4	— 8	— 22.2	— 17.7
69	20.5	16.4	30	— 1.1	— 0.8	— 9	— 22.7	— 18.2
68	20	16	29	— 1.6	— 1.3	— 10	— 23.3	— 18.6
67	19.4	15.5	28	— 2.2	— 1.7	— 11	— 23.8	— 19.1
66	18.8	15.1	27	— 2.7	— 2.2	— 12	— 24.4	— 19.5

15	26.1	21.3	24	31.1	24.8	32	3
16	26.6	21.3	24	31.1	24.8	32	3
17	27.2	21.7	25	31.6	25.3	33	3
18	27.7	22.2	26	32.2	25.7	34	3
19	28.3	22.6	27	32.7	26.2	35	3
20	28.8	23.1	28	33.3	26.6		

Relative Indications of Temperature by Fahrenheit, Centigrade, and Reaumur's Thermometrically tabulated.

Degrees of			METALS, ETC.
Fah.	Cent.	Reau.	
2786	1530	1224	Cast Iron melts.
2500	1371	1097	Cast Steel "
2016	1102	882	Gold "
1996	1091	873	Copper, Cast "
1900	1038	830	Gun Metal "
1873	1023	818	Silver "
1869	1020	816	Brass "
810	432	345	Antimony "
700	371	297	Zinc "
594	312	250	Lead "
476	247	197	Bismuth "
442	228	182	Tin "
		88	Sulphur "

RELATIVE INDICATIONS OF TEMPERATURE. 321

Degrees of			
Fah.	Cent.	Reau.	
210	98·8	79·1	ALLOYS. Bismuth 8, tin 3, lead 5, melts. Bismuth 15, tin 4, lead 8, and cadmium 3, „
138	58·8	47·1	
			LIQUIDS.
662	350	280	Mercury boils.
600	315·5	252·4	Linseed oil „
590	310	248	Sulphuric acid „
560	293	235	Oil, turpentine „
98	36·6	29·3	Ether and water in a vacuum „
212	100	80	Fresh water boils, barometer 30 inches at sea level.
213·2	100·6	80·5	Common sea-water containing $\frac{1}{2}$ salt, boils under atmos- pheric pressure.
214·4	101·3	81	Sea-water containing $\frac{2}{3}$ boils.
215·5	102	81·6	„ „ $\frac{2}{3}$ „
216·7	102·6	82	„ „ $\frac{2}{3}$ „
217·9	103·2	82·6	„ „ $\frac{2}{3}$ „
219·1	104	83·2	„ „ $\frac{2}{3}$ „
220·3	104·5	83·6	„ „ $\frac{2}{3}$ „
			NOTE. —Relative to steam- boilers at sea, as a general rule no deposit of salt takes place up to 216·7 degrees of atmospheric boiling.
			FREEZING.
32	0	0	Freezing-point of Fah., and zero of Cent. and Reau.
28	— 2·2	— 1·7	Vinegar „freezes.
27½	— 2·5	— 2	Sea-water „
20	— 6·6	— 5·3	Strong Wines „
14	— 10	— 8	Turpentine „
1	— 17·2	— 13·7	Sulphuric acid „
0	— 17·7	— 14·2	Zero of Fahrenheit

1. Subtract .002 from 100.

$$\begin{array}{r} 100 \\ - .002 \\ \hline 99.998 \text{ Answer.} \end{array}$$

2. Find the value of $24.004 - .987516$.

$$\begin{array}{r} 24.004 \\ - .987516 \\ \hline 23.016484 \text{ Answer.} \end{array}$$

3. Multiply .0001 by .001. As there always be as many decimals in the product there are in the factors, the product here is .0000001.

4. Multiply .03 by 2, by .001 and by 6.

$.03 \times 2 \times .001 \times 6 = .00036$, the product consists of five decimal places, because those in the factors make number.

Express as decimals,

$$\frac{7}{10} = .7, \frac{3}{100} = .03, \frac{37}{100000} = .00037.$$

... of iron is in length 8 feet, a

6. What weight on the end of a lever 8 feet in length, will exert a force equal to 100 lbs. on the other end, 6 inches being the distance of the fulcrum from the 100 lbs?

The arm of the power is 96 in. — 6 in. = 90 in. therefore $100 \times 6 \div 90 = 6.667$ lbs. the weight required.

7. What are the solid contents and superficial surface of a cylindrical boiler with spherical ends, the boiler being 4 feet in diameter and the cylindrical part 10 feet in length?

$$4 \times 4 \times .7854 \times 10 = 125.664 \text{ contents of cylindrical part.}$$

$$4 \times 4 \times 4 \times .5236 = 33.5104 + 125.664 = 159.1744 \text{ total amount of cubic feet.}$$

then, $4 \times 3.1416 \times 10 = 125.664$ surface of cylinder.

$$4 \times 3.1416 \times 4 = 50.2656 + 125.664 = 175.9296 \text{ total surface in square feet.}$$

8. What quantity of coals will a bunker contain that is 16 feet long, 6.5 feet wide, and 18 feet in height, allowing 45 cubic feet capacity per ton?

$$16 \times 6.5 \times 18 = 1872 \div 45 = 41.6 \text{ tons.}$$

9. Required the necessary weight to be attached on the end of a lever for an overflow valve of 5 inches diameter, the pressure of steam in the boiler being 10 lbs. per square inch, the length of the lever 42 inches, and the fulcrum 6 inches from the centre of the valve.

$$5^2 \times .7854 \times 10 \times 6 = 1178.1000 \div 42 = 28.05 \text{ lbs.}$$

10. The diameter of the screw shaft of a 100 horse-power engine is 6 inches, what should be the diameter when the power is 400 horses?

$$6 \times 6 = 36 \times 4, \text{ and } \sqrt{144} = 12 \text{ inches diameter.}$$

10 cwt. of copper.

and $1887 \text{ lbs.} \times 11 \div 111 = 187 \text{ lbs. of tin.}$

12. The consumption of coal is 60 cwt per hour, and the rate of the ship 10 knots full; what will be the consumption at 8 knots, and what distance will 400 tons of coals carry under these circumstances?

$10^3 = 1000$ and $8^3 = 512$. $512 \times 60 \div 1000 = 30\cdot72$
per hour at 8 knots.

Then if $30\cdot72$ gives 8 knots, what will 400×20

Ans. 8000 cwt.

Then $8000 \times 8 \div 30\cdot72 = 2083\cdot3$ knots the distance.

13. A safety valve is 6 inches diameter; what weight must be placed upon it to equal 12 lb per square inch?

$6^2 \times \cdot7854 \times 12 = 339\cdot2928 \text{ lbs.}$

14. The pitch of a screw propeller is 1 foot; the number of revolutions 80 per minute; find the rate of the screw in knots per hour, supposing 1 knot or nautical mile equal 6080 English feet.

16. What should be the diameter of the piston of an indicator, the area of which is one fourth of a square inch ?

$$\frac{\cdot 25000000}{\cdot 7854} = \sqrt{\cdot 3183} = \cdot 561 \text{ of an inch.}$$

17. A piece of boiler-plate (iron) is 7 feet long, 6 feet broad, and $\frac{5}{8}$ inch in thickness, how many cubic feet does it contain, and what is its weight at 25 lbs. per square foot ?

$$84 \times 72 \times \cdot 625 = 3780\ 000 \div 1728 = 2\ 187 \text{ cubic feet.}$$

$$\text{or, } 7 \times 6 \times \cdot 052 = 2\ 184 \text{ cubic feet.}$$

$$7 \times 6 \times 25 = 1050 \div 112 = 9 \text{ cwts. 1 qr. 14 lbs.}$$

18. What weight on the end of a lever 12 feet in length will equipoise 2 tons on the other end, the fulcrum being distant 6 inches from the weight to be equipoised, and the weight of the lever not taken into account ?

$$4480 \times 6 = 26880 \div 138 = 194\ 7 \text{ lbs.}$$

19. A boiler has 1800 tubes, $2\frac{1}{8}$ inches diameter and 6 feet 6 inches long, what is the total amount of heating surface, and what the horse power at 15 square feet of heating surface per horse power ; also, what is the amount of smoke draught through the boiler by tubes, the metal of the tubes being $\frac{1}{8}$ of an inch in thickness.

$$2\ 5 \times 8\ 1416 \times 78 \times 1800 = \frac{1102701\ 6}{144} \times \frac{7657\ 65}{15} = 510$$

horses power.

$$\text{and } 2\ 25^3 \times \cdot 7854 \times 1800 = 7056\ 8 \div 144 = 49 \text{ sq. feet.}$$

Thickness of plates in part of an inch.	Multipliers.	Diameters of Rivets.	Lengths of rivets from heads.	Distance of rivets from centre to centre.	Breadth of lap for six joints.
$\frac{1}{8}$	19	38	88	1.25	1.25
$\frac{1}{4}$	25	5	1.13	1.5 6	1.5 6
$\frac{3}{8}$	31	63	1.38	1.63	1.88
$\frac{1}{2}$	38	75 2	1.63 4.5	1.75 5	2 5
$\frac{5}{8}$	5	81	2.25	2	2.25
$\frac{3}{4}$	63	94 1.5	2.75	2.5 4	2.75 4
$\frac{7}{8}$	75	1.13	3.25	3	3.25

The numbers on the right, in the several columns first two, namely, the numbers 2, 1.5, 4.5, 6, 5, 4, 4.5, are used as multipliers, as in the following example.

Let the thickness of plate equal $\frac{3}{8}$ or .375

$$\begin{aligned}
 &\left\{ \begin{array}{l} \times 2 = .75 \text{ or } \frac{3}{4} \text{ the diameter of rivets.} \\ \times 4.5 = 1.688 \text{ or } 1\frac{1}{4} \text{ length of rivets.} \\ \times 5 = 1.875 \text{ or } 1\frac{7}{8} \text{ distance from centre to rivets.} \\ \times 5.5 = 2.063 \text{ or 2 inches breadth of lap rivets.} \\ \times 5.5 = 2.063 + \frac{3}{8} \text{ rds or } 1.375 = 3.448 \text{ or } 3\frac{1}{2} \text{ inches of rivets.} \end{array} \right. \\
 &\text{.375}
 \end{aligned}$$

Conversion of cwt., qrs., and lbs. into lbs.

We terminate this work with the following compendious method of converting cwt., qrs., and lbs. into lbs.

RULE.—If there are cwt., only, repeat the number under itself. Below the first figure on the right put a 0, and then the figures of the same number, thus pushing those figures one place to the left. Again, commencing with two 0's, repeat the number a third time, the figures being one more place to the left, and then add up. If there be also qrs. and lbs. write the equivalent to them in lbs. under the whole before adding up, thus:—

234 cwt.	234 cwt. 3 qrs. 25 lbs.
234	234
2340	2340
23400	23400
<hr/>	<hr/>
26208 lbs.	109 = 3 qrs. 25 lbs.
	<hr/>
	26317 lbs.

Should there be tons as well, add 20 times the number of tons to the cwt. and then proceed with the result as above.

* * The foregoing method is selected out of a great variety of similar short processes, from a work entitled, "Intuitive Calculations," by Daniel O'Gorman. 23rd Edition.

NOTE (A), Page 79.

THE circumference of a circle of 1 inch in diameter is 3.1416 inches. In the calculation at p. 79, the decimal part of this latter number, namely .1416, is converted into *eighths* by multiplying it by 8, the product being 1.1328 eighths. The integral portion of these eighths, namely 1, is alone retained, and the decimals rejected, as of no practical moment. But the several successive eighths may be deduced, one after another, from the first result, more readily by continually adding the number 3.1416, thus:

Diameter.		Circumference.	
1 in.....	3 in. and 1.1328 eighths.	3.1416	
		<hr/>	
1½	3 "	4.2744	"
		3.1416	
		<hr/>	
1½	3 "	7.4160	"
		3.1416	
		<hr/>	
1½	4 "	2.5576	"
		3.1416	
		<hr/>	
1½	4 "	5.6992	"
		3.1416	

1½ 5	„	7.1240	„
			3.1416	„
2 6	„	2.2656	„

and so on. The integers of the several results are alone retained. Of course the results against the diameters 1½, 1¾, 2 eighths, 2 eighths, 2 eighths, are tabulated ½, ½, ½. It is proper that any individual number in the Table may be found independent of the other numbers by multiplying 3.1416 by the diameter. Thus (taking the diameter at 2 ft. 10½ in., and multiplying by the feet and inches separately, we have

3.1416	½ of 3.1416 =	.7854
2	10	3
For 2 ft. = 6.2832 ft.	31.416	2.3562 = three-f
For 10½ in. = 2.814	2.356	
9.097 ft.	18)33.773 in.	
12		
1.164 in.	2.814 ft., for 10½ in.	
8		
1.312 eighths.	Hence 9 ft. 1½ in. = circumferen	

The practical man may readily infer the value of the Table for calculation.

NOTE (B), Page 107.

The successive numbers in the Table may be obtained in a manner similar to that exhibited in the preceding Note; thus:

Diameter.	Circumference.
3 ft. 0 in.	8 ft. 9 in., and 4.1856 eighths
	2.9312

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